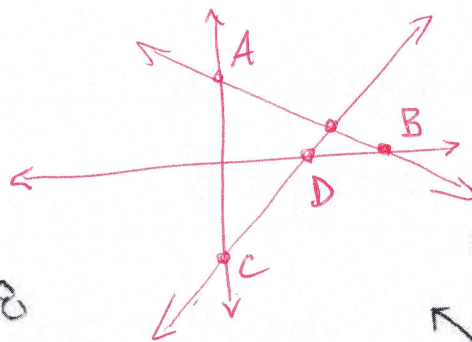


1A) $2x + 5y = 20$
 $3x - 2y = 18$

$\frac{44.5}{70}$



$2x + 5y = 20$

~~$x + y = 4$~~

x	y
0	4

(0,4) A

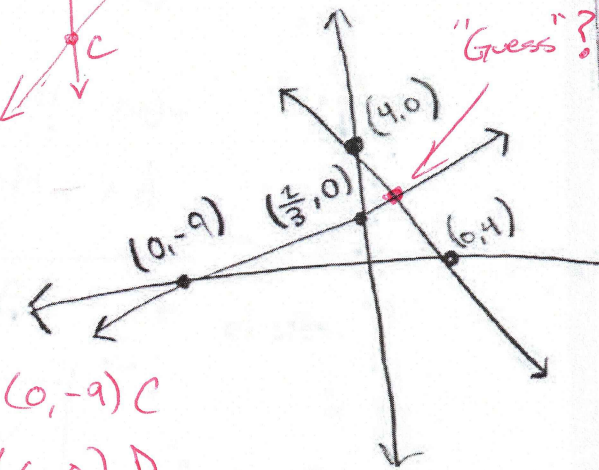
~~10~~ ~~4~~ 0 $\leadsto$ (10,0) B

$3x - 2y = 18$

~~$x + y = -9$~~

x	y
0	-9

~~6~~ ~~2~~ 0 $\leadsto$ (0,-9) C
 (6,0) D



"Guess"?

+7

1B)

$3x - 2y = 18$

"-2" goes away on this side

$-2y = -3x - 18$

Sign change ok, but no "-2" change on this side?

$y = 3x + 18$

$2x + 5y = 2x + 5(3x + 18) = 20$

$2x + 15x + 90 = 17x + 90 = 20$

$17x = 110$

$x = \frac{110}{17} = 6.47$

$y = 3(6) + 18 = 36$

Should come out to

$y = \frac{24}{19}$

$x = \frac{130}{19}$

~~$36 = y$~~

+6

1C. $2x + 5y = 20$
 $3x - 2y = 18$

-3 E1

$$-6x - 15y = -60$$

2 E2

$$6x + 4y = 36$$

$$\hline -19y = -24$$

$$y = +\frac{24}{19}$$

wrong *how??* *right*

$$2x + 5y = 2x + 5\left(-\frac{24}{19}\right) = 2x + \frac{60}{19} = 20$$

$$\frac{2x}{1} \cdot \frac{19}{19} + \frac{60}{19} = \frac{20}{1} \cdot \frac{19}{19}$$

$$\cancel{\frac{160}{19}} = x$$

$$2x + 5y = 20$$

$$2x + 5\left(\frac{24}{19}\right) = 20$$

$$2x = 20 - \frac{120}{19}$$

$$2x = \frac{380 - 120}{19}$$

$$= \frac{260}{19}$$

$$\Rightarrow x = \frac{130}{19}$$

+8

$$\begin{aligned} 2. \quad & 2x - 2y + z = -13 \\ & 3x - 5y - z = -21 \\ & x - 2z = 7 \end{aligned}$$

$$\begin{aligned} -2x - 2y + z &= 13 \\ 3x + 5y - z &= -21 \end{aligned}$$

$$-z = -8$$

$$\boxed{z = 8}$$

$$-3 \quad 2x - 2y + z = -13$$

$$x - 2z = 7$$

$$\boxed{z = 6}$$

+5

$$\begin{aligned} 3. \quad & 7x + 17y + 27z = 36 \\ & 2x + 5y + 8z = 8 \\ & x + 2y + 3z = 6 \end{aligned}$$

$$x + 2y + 3z = 6$$

$$3x + 17y + 27z = 36$$

$$2x + 5y + 8z = 8$$

$$\begin{pmatrix} x + 2y + 3z = 6 \\ 3x + 17y + 27z = 36 \end{pmatrix}$$

$$\boxed{19y + 2z = 36}$$

$$x + 2y + 3z = 6$$

$$19y + 2z = 36$$

$$3y + z = 20$$

z is free

$$y = -2z - 4$$

$$x = z + 14$$

$$3x + 17y + 27z = 36$$

$$-2x - 15y + 25z = 28$$

$$-2x + 12y - 22z = 8$$

$$\boxed{3y + z = 20}$$

$$x + 2y + 3z = 6$$

$$19y + 2z = 36$$

$$0 = 0!$$

+6

3B.

$$z=0 \rightarrow (x, y, z) = (14, -4, 2) \quad 2 \neq 0$$

$$z=1 \rightarrow (x, y, z) = \left(\frac{8(1) + 30}{3}, \frac{2-6}{3}, -1 \right) = \left(\frac{38}{3}, \frac{-4}{3}, -1 \right)$$

$$z=-1 \rightarrow (x, y, z) = \left(\frac{8(-1) + 30}{3}, \frac{-2-6}{3}, 1 \right) = \left(\frac{22}{3}, \frac{-8}{3}, 1 \right)$$

4.

$$\begin{aligned} x + 2y + 3z &= 6 \\ 3x + 17y + 27z &= 30 \\ 2x + 5y + 8z &= 8 \end{aligned}$$

$$\begin{aligned} &\rightarrow x + 2y + 3z = 6 \quad \text{OK} \\ &\rightarrow 3y + 2z = 30 \quad \text{how?!} \\ &\rightarrow 0 = 8? \end{aligned}$$

This system is absurd because $0=8$ makes no sense. The problem is similar to problem #3 but #3's second equation equals 8 while this one equals 3.

+7.5