

MAT 1340

WP # 4

Cachero

4/21/23

$$\begin{cases} 1. \ 2x + 5y = 20 \\ \quad 3x - 2y = 18 \end{cases}$$

$\frac{51}{70}$

first way

$$5y = 20 - 2x$$

$$3x - 2y = 18$$

$$\frac{5y}{5} = \frac{20}{5} + \frac{-2x}{5}$$

$$3x - 2y = 18 \checkmark$$

$$y = \frac{20}{5} + \frac{-2x}{5}$$

$$3x - 2y = 18$$

$$y = 4 - \frac{2x}{5}$$

$$3x - 2y = 18$$

$$-2y = 18 - 3x$$

$$y = 4 - \frac{2x}{5} \rightarrow \frac{-2y}{-2} = \frac{18}{-2} + \frac{-3x}{-2}$$

$$y = 4 - \frac{2x}{5}$$

→

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2nd way = Substitution

$$\begin{aligned} 2x &= 20 - 5y \\ 3x - 2y &= 18 \end{aligned}$$

divide each term by 2 & simplify

$$\frac{2x}{2} = \frac{20}{2} + \frac{-5y}{2}$$

$$3x - 2y = 18 \rightarrow \text{Simplify left side} \rightarrow \text{cancel common factor}$$

$$\frac{2x}{2} = \frac{20}{2} + \frac{-5y}{2}$$

$$3x - 2y = 18 \rightarrow \text{divide } x \text{ by } 1$$

$$x = \frac{20}{2} + \frac{-5y}{2}$$

$$3x - 2y = 18 \rightarrow \text{Simplify R side} \\ \text{divide by 20 by 2}$$

$$x = 10 + \frac{-5y}{2}$$

$$3x - 2y = 18 \rightarrow \text{Replace all occurrences of } x \text{ with } 10 - \frac{5y}{2} \text{ in each equation}$$

$$3\left(10 - \frac{5y}{2}\right) - 2y = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{simplify}$$

$$3\left(10 - \frac{5y}{2}\right) - 2y$$

$$3 \cdot 10 + 3\left(-\frac{5y}{2}\right) - 2y = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow$$

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Cachen

multiply 3 by 10

$$30 + 3\left(-\frac{5y}{2}\right) - 2y = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{multiply by } 3\left(-\frac{5y}{2}\right)$$

$$30 - 3\frac{5y}{2} - 2y = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{combine } 3 \& \frac{5y}{2}$$

$$30 + \frac{-3(5y)}{2} - 2y = 18 \quad x = 10 - \frac{5y}{2}$$

$$\text{multiply 5 by } -3 \quad 30 + \frac{-15y}{2} - 2y = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{move negative in front of fraction}$$

$$30 - 15y - 2y = 18$$

$$x = 10 - \frac{5y}{2}$$

$$\rightarrow \frac{30 + -15y - 2y \cdot 2}{2} = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{Simplify}$$

$$30 - \frac{19y}{2} = 18$$

$$x = 10 - \frac{5y}{2} \rightarrow \text{solve for } y$$

$$30 - \frac{19y}{2} = 18 \quad \left(y = \frac{24}{19}\right) \quad x = 10 - \frac{5y}{2}$$

$$x = 10 - \frac{5\left(\frac{24}{19}\right)}{2}$$

$$x = 10 - \frac{60}{19}, \quad x = 10 \cdot \frac{19}{19} - \frac{60}{19}, \quad x = \frac{10 \cdot 19}{19} - \frac{60}{19} = \frac{130}{19}$$

$$x = \frac{130}{19}, \quad y = \frac{24}{19}$$

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3rd way:

$$2x + 5y = 20, 3x - 2y = 18$$

$$(-3) \cdot (2x + 5y) = (-3)(20)$$

$$(2) \cdot (3x - 2y) = (2)(18) \rightarrow \text{simplify}$$

$$\left. \begin{array}{l} -6x - 15y = -60 \\ 6x - 4y = 36 \end{array} \right\} \text{add the two equations together to eliminate } x$$

$$\frac{-6x - 15y = -60}{6x - 4y = 36} \rightarrow -19y = -24 \rightarrow \text{divide each term by } -19 \text{ \& simp.}$$

$$\frac{-19y}{-19} = \frac{-24}{-19} = y = \frac{24}{19}$$

$$-6x - 15\left(\frac{24}{19}\right) = -60$$

$$-15\left(\frac{24}{19}\right) = -6x + \frac{-15 \cdot 24}{19} = -60$$

multiply -15 by 24

$$-6x + \frac{-360}{19} = -60$$

$$-6x - \frac{360}{19} = -60 \rightarrow \text{Add } \frac{360}{19} \text{ to both sides}$$

$$-6x = -60 + \frac{360}{19} \rightarrow -6x = -60 \cdot \frac{19}{19} + \frac{360}{19}$$

$$\text{Combine } -60 \text{ \& } \frac{19}{19}. -6x = \frac{-60 \cdot 19}{19} + \frac{360}{19}$$

$$-6x = \frac{-60 \cdot 19 + 360}{19} = -6x = \frac{-780}{19}$$

(5)

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Checked

Continued...

$$-6x = \frac{-780}{19}$$

- move the negative
in front of the
fraction.

$$-6x = \frac{-780}{19}$$

Divide each term in $-6x = -\frac{780}{19}$ by -6

$$x = \frac{130}{19} \quad y = \frac{24}{19}$$

+10

6

wp#4

$$\begin{aligned} (2) \quad & 2x - 2y + z = -13 \quad - \\ & 3x - 5y - z = -21 \quad - \\ & x - 2z = 7 \quad - \end{aligned}$$

If went wrong kinda early

$2x - 2y + z = -13$ } eliminate x
 $3x - 5y - z = -21$ }
 $(-3) \cdot (2x - 2y) = (-3)(-15), (2) \cdot (3x - 5y) = (2)(-19)$
 Simplify $\rightarrow -6x + 6y = 45$ } Add together
 $6x - 10y = -38$ } to eliminate x.
 $-4y = 7$

$3x - 5y - z = -21$ } move all
 $x - 2z = 7$ } terms containing variables to the left

$$3x - 5y = -19, x - 2z = 7$$

$$3x - 5y = -19, (-3) \cdot (x - 2z) = (-3)(7) \rightarrow \text{simplify}$$

$$\begin{aligned} x &= \frac{1}{5} \\ y &= 5 \\ z &= -\frac{17}{5} \end{aligned}$$

$$\begin{aligned} 3x - 5y &= -19 \\ -3x + &= -21 \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{array}{l} \text{add together} \\ \text{eliminate } x \end{array}$$

$$6z - 5y = -40 \quad +6$$

$$\begin{aligned} -4y &= 7 \\ -5y + 6z &= -40 \end{aligned} \rightarrow \begin{cases} z = -\frac{65}{8} \\ y = -\frac{7}{4} \end{cases} \quad x = -\frac{37}{4}$$

(7)

3.

$$7x + 17y + 27z = 30$$

$$2x + 5y + 8z = 8$$

$$x + 2y + 3z = 6$$

$$\left. \begin{array}{l} 7x + 17y + 27z = 30 \\ 2x + 5y + 8z = 8 \end{array} \right\} \text{eliminate } x$$

$$(-2) \cdot (7x + 17y + 27z) = (-2)(30)$$

$$(7) \cdot (2x + 5y + 8z) = (7)(8) \rightarrow \text{simplify}$$

$$-14x - 34y - 54z = -60$$

$$14x + 35y + 56z = 56$$

$$- \quad \underline{\quad \quad \quad} \quad \underline{y + 2z = -4}$$

$$\left. \begin{array}{l} 2x + 5y + 8z = 8 \\ x + 2y + 3z = 6 \end{array} \right\} \begin{array}{l} (-2) \cdot (x + 2y + 3z) = (-2)(6) \\ \text{simplify} \end{array}$$

$$2x + 5y + 8z = 8$$

$$-2x - 4y - 6z = -12$$

$$\underline{0 = 0}$$

one more step

and you have \rightarrow the "y"

$$\underline{y + 2z = -4}$$

a) wanted $x =$ and $y =$ in terms of z , z is free

ie: $y = -2z - 4$, $x = z + 14$, $z = z$

b) I do not see any work relating to part b.

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(Cachere)

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$$\begin{aligned} 7x + 17y + 27z &= 30 \\ \textcircled{4.} \quad 2x + 5y + 8z &= 3 \\ x + 2y + 3z &= 6 \end{aligned}$$

1. move all terms not containing x to the R side

$$\begin{aligned} x + 3z &= 6 - 2y && \text{Subtract } 3z \\ 7x + 17y + 27z &= 30 \\ 2x + 5y + 8z &= 3 \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{aligned} x &= 6 - 2y - 3z \\ 7x + 17y + 27z &= 30 \\ 2x + 5y + 8z &= 3 \end{aligned}$$

Replace all occurrences of x with $6 - 2y - 3z$

$$7(6 - 2y - 3z) + 17y + 27z = 30$$

$$x = 6 - 2y - 3z$$

$$2x + 5y + 8z = 3 \rightarrow \text{simplify left side} \quad 4z + 3y + 6z = 30$$

$$2x + 5y + 8z = 3 \quad \left\{ \begin{array}{l} x = 6 - 2y - 3z \\ 2x + 5y + 8z = 3 \end{array} \right.$$

Replace all occurrences of x with $6 - 2y - 3z$. $2(6 - 2y - 3z) + 5y + 8z = 3$ with

$$4z + 3y + 6z = 30$$

$$x = 6 - 2y - 3z \rightarrow \text{simplify L side}$$

$$2(6 - 2y - 3z) + 5y + 8z$$

$$12 + y + 2z = 3$$

$$4z + 3y + 6z = 30$$

$$x = 6 - 2y - 3z$$

Subtract 12 from both sides

$$\rightarrow y + 2z = 3 - 12$$

$$4z + 3y + 6z = 30$$

$$x = 6 - 2y - 3z$$

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Continued...

Subtract $2z$ from both sides

$$\begin{array}{l} y = 3 - 12 - 2z \\ 4z + 3y + 6z = 30 \\ x = 6 - 2y - 3z \end{array} \left. \begin{array}{l} \text{Subtract } 12 \text{ from } 3 \\ y = -9 - 2z \\ 4z + 3y + 6z = 30 \\ x = 6 - 2y - 3z \end{array} \right\}$$

Replace all occurrences of y with $-9 - 2z$
in each equation

$$x = 24 + z$$

$15 = 30 \rightarrow 15 = 30$ is not true it is absurd

~~$y = -9 - 2z$~~ there is no solution.

+10