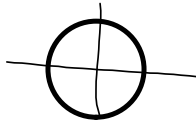
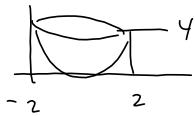


3.  $\mathbf{F}(x, y, z) = x^2z^2 \mathbf{i} + y^2z^2 \mathbf{j} + xyz \mathbf{k}$ ,

$S$  is the part of the paraboloid  $z = x^2 + y^2$  that lies inside the cylinder  $x^2 + y^2 = 4$ , oriented upward

$$\int_C \mathbf{F} \cdot d\mathbf{r} = \left( \iint_S \text{curl } \mathbf{F} \cdot d\mathbf{S} \right)$$

Evaluate this using Stokes'



$$\int_0^{2\pi}$$

$$d\mathbf{r} = \mathbf{r}'(t) dt = \langle -2, 2, 0 \rangle$$

$$\langle x^2z^2, y^2z^2, xyz \rangle$$

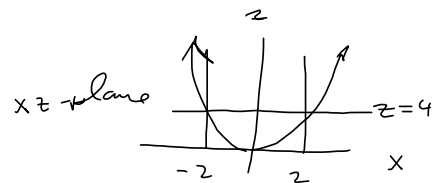
$$\mathbf{F}(\mathbf{r}(\theta)) = \langle 4\cos^2\theta \cdot 4^2, 4\sin^2\theta \cdot 4^2, 4\sin\theta \cos\theta \cdot 4 \rangle$$

$$\int_0^{2\pi} \langle 64\cos^2\theta, 64\sin^2\theta, 16\sin\theta \cos\theta \rangle \cdot \langle -2\sin\theta, 2\cos\theta, 0 \rangle d\theta$$

$$= \int_0^{2\pi} (-128\cos^2\theta \sin\theta + 128\sin^2\theta \cos\theta) d\theta$$

$$= 128 \int_0^{2\pi} ((\cos^2\theta)(-\sin\theta) + \sin^2\theta \cos\theta) d\theta$$

$$= 128 \left[ \frac{\cos^3\theta}{3} + \frac{\sin^3\theta}{3} \right]_0^{2\pi} = 128 \left( \frac{1}{3} - \frac{1}{3} \right) = 0!$$



$$\mathbf{F} = \langle 2\cos\theta, 2\sin\theta, 0 \rangle$$

$$\mathbf{F}' = \langle -2\sin\theta, 2\cos\theta, 0 \rangle$$

$$? \|\mathbf{F}'\| = \sqrt{4\sin^2\theta + 4\cos^2\theta} = 2$$