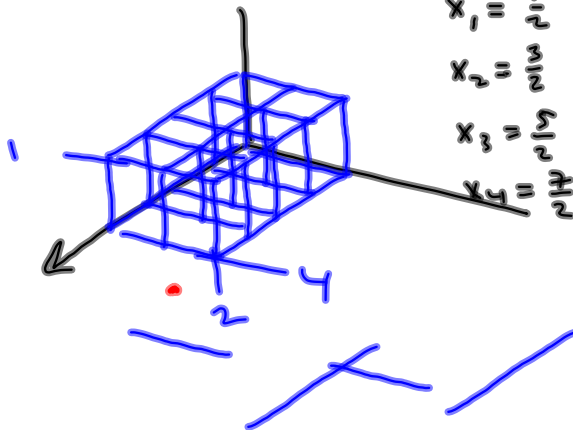


16.6 #26

$$\mathcal{B} = \{ (x, y, z) \mid 0 \leq x \leq 4, 0 \leq y \leq 2, 0 \leq z \leq 1 \}$$



$$x_1 = \frac{1}{2}$$

$$x_2 = \frac{3}{2}$$

$$x_3 = \frac{5}{2}$$

$$x_4 = \frac{7}{2}$$

$$y_1 = \frac{1}{2} \quad z_1 = \frac{1}{2}$$

$$y_2 = \frac{3}{2}$$

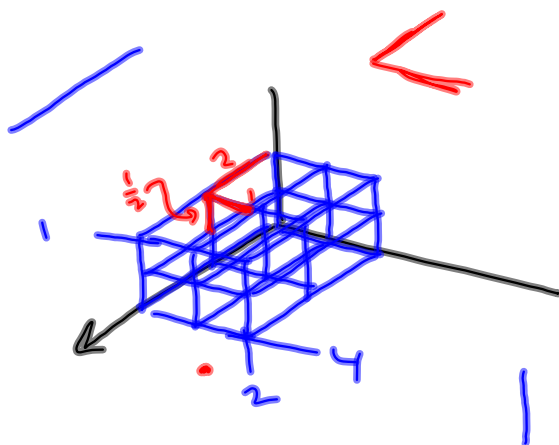
That's what
I thought

$$x_i = \frac{2i-1}{2}, \quad i=1, \dots, 4$$

$$y_j = \frac{2j-1}{2}, \quad j=1, \dots, 2$$

$$z_k = \frac{2k-1}{2}, \quad k=1$$

$$\iiint_{\mathcal{B}} \sin(xy^2z^3) dV$$



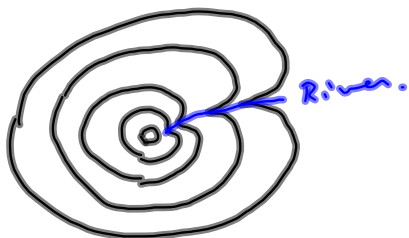
Book way

$$\begin{array}{lll} x_1 = 1 & y_1 = \frac{1}{2} & z_1 = \frac{1}{4} \\ x_2 = 3 & y_2 = \frac{3}{2} & z_2 = \frac{3}{4} \end{array}$$

$$\Delta V = 1$$

$$\sum_{k=1}^2 \sum_{j=1}^2 \sum_{i=1}^2 \sin \left((2i-1) \left(\frac{2j-1}{2} \right)^2 \left(\frac{2k-1}{4} \right)^3 \right) \cdot 1$$

16.1 A sketch? See Gradient?

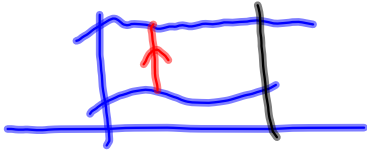


16.2 Fubini: stuff Evaluate

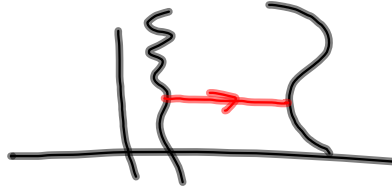
$$\iint_{\mathcal{R}} \quad \& \quad \iiint_{\mathcal{E}} \quad \text{on rectangular domains.}$$

$$\mathcal{R} = [a, b] \times [c, d] \quad \mathcal{E} = [a, b] \times [c, d] \times [e, f]$$

16.3 Type I, II



$$\iint f \, dy \, dx$$

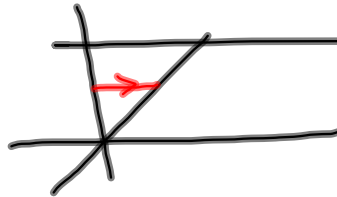
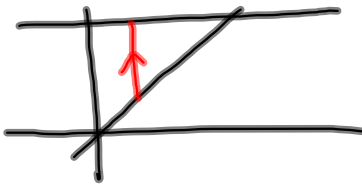


$$\iint f \, dx \, dy$$

Maybe a "do it I & II way".

#48

$$\int_0^1 \int_x^1 e^{\frac{x}{y}} \, dy \, dx = \int_0^1 \int_0^y e^{\frac{x}{y}} \, dx \, dy$$



$$= \int_0^1 \int_0^y y e^{\frac{x}{y}} \cdot \frac{1}{y} \, dx \, dy = \int_0^1 \left[y e^{\frac{x}{y}} \right]_{x=0}^{x=y} \, dy$$

$$u = \frac{x}{y} \quad du = \frac{1}{y} \, dx$$

y is constant

$$= \int_0^1 [y e^{-y}] \, dy$$

$$= \int_0^1 (e-1) y \, dy = \frac{1}{2}(e-1) [y^2]_0^1 = \frac{1}{2}(e-1)$$

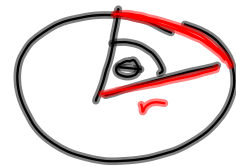
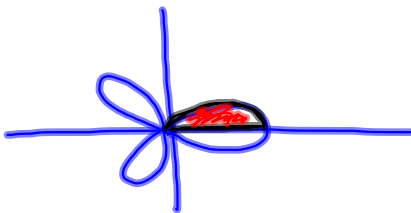
16.4 Polar coordinates.

Area of one loop of $r = \cos(3\theta)$

old way:

$$A = \frac{1}{2} r^2 \theta$$

$$A = \frac{1}{2} f(\theta)^2 \cdot \theta$$



$$\cos 3\theta = 0 \quad \text{②}$$

$$3\theta = \frac{\pi}{2}$$

$$\theta = \frac{\pi}{6}$$

$$A = 2 \cdot \frac{1}{2} \int_0^{\frac{\pi}{6}} \cos^2(3\theta) d\theta = \frac{\pi}{12}$$

16.4 way: Find the volume over the region of $f(r, \theta) = \cos(3\theta)$

$$\int_{-\frac{\pi}{6}}^{\frac{\pi}{6}} \int_0^{\cos(3\theta)} r dr d\theta$$

