

1–4 Verify that the Divergence Theorem is true for the vector field \mathbf{F} on the region E .

2. $\mathbf{F}(x, y, z) = x^2 \mathbf{i} + xy \mathbf{j} + z \mathbf{k}$,

E is the solid bounded by the paraboloid $z = 4 - x^2 - y^2$ and the xy -plane

5–15 Use the Divergence Theorem to calculate the surface integral $\iint_S \mathbf{F} \cdot d\mathbf{S}$; that is, calculate the flux of \mathbf{F} across S .

5. $\mathbf{F}(x, y, z) = e^x \sin y \mathbf{i} + e^x \cos y \mathbf{j} + yz^2 \mathbf{k}$,

S is the surface of the box bounded by the planes $x = 0$, $x = 1$, $y = 0$, $y = 1$, $z = 0$, and $z = 2$

8. $\mathbf{F}(x, y, z) = x^3y \mathbf{i} - x^2y^2 \mathbf{j} - x^2yz \mathbf{k}$,

S is the surface of the solid bounded by the hyperboloid $x^2 + y^2 - z^2 = 1$ and the planes $z = -2$ and $z = 2$

9. $\mathbf{F}(x, y, z) = xy \sin z \mathbf{i} + \cos(xz) \mathbf{j} + y \cos z \mathbf{k}$,

S is the ellipsoid $x^2/a^2 + y^2/b^2 + z^2/c^2 = 1$

10. $\mathbf{F}(x, y, z) = x^2y \mathbf{i} + xy^2 \mathbf{j} + 2xyz \mathbf{k}$,

S is the surface of the tetrahedron bounded by the planes $x = 0$, $y = 0$, $z = 0$, and $x + 2y + z = 2$