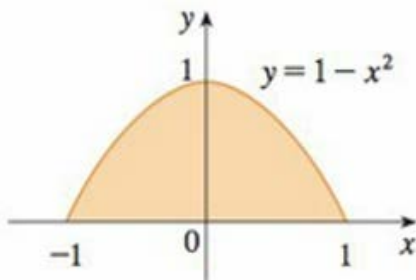
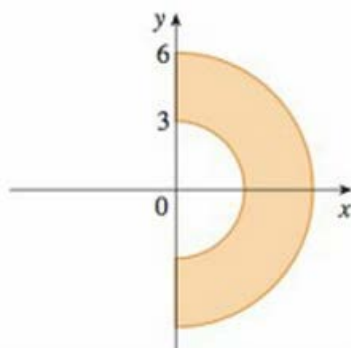


1–4 A region R is shown. Decide whether to use polar coordinates or rectangular coordinates and write $\iint_R f(x, y) dA$ as an iterated integral, where f is an arbitrary continuous function on R .

2.



4.



7–14 Evaluate the given integral by changing to polar coordinates.

8. $\iint_R (x + y) dA$, where R is the region that lies to the left of the y -axis between the circles $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$

11. $\iint_D e^{-x^2-y^2} dA$, where D is the region bounded by the semicircle $x = \sqrt{4 - y^2}$ and the y -axis

15–18 Use a double integral to find the area of the region.

15. One loop of the rose $r = \cos 3\theta$

18. The region inside the cardioid $r = 1 + \cos \theta$ and outside the circle $r = 3 \cos \theta$

29–32 Evaluate the iterated integral by converting to polar coordinates.

32. $\int_0^2 \int_0^{\sqrt{2x-x^2}} \sqrt{x^2 + y^2} dy dx$

36. (a) We define the improper integral (over the entire plane \mathbb{R}^2)

$$\begin{aligned} I &= \iint_{\mathbb{R}^2} e^{-(x^2+y^2)} dA = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-(x^2+y^2)} dy dx \\ &= \lim_{a \rightarrow \infty} \iint_{D_a} e^{-(x^2+y^2)} dA \end{aligned}$$

where D_a is the disk with radius a and center the origin. Show that

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-(x^2+y^2)} dA = \pi$$