

§ 2.1 #8, 20,

$$\textcircled{20} \frac{f(T) - f(2)}{T - 2} = \frac{\frac{1}{T} - \frac{1}{2}}{T - 2} = \frac{\frac{2-T}{2T}}{T-2}$$

$$= \frac{2-T}{2T(T-2)} = \frac{-(T-2)}{2T(T-2)} = -\frac{1}{2T} \xrightarrow{T \rightarrow 2} -\frac{1}{4}$$

$\uparrow$   
 lin STUFF  
 $T \rightarrow 2$

$$\textcircled{8} f(x) = 5 - x^2, P(1, 4)$$

$$\frac{f(1+h) - f(1)}{h} = \frac{5 - (1+h)^2 - (5 - 1^2)}{h} = \frac{5 - (1+2h+h^2) - 4}{h}$$

$$= \frac{5 - 1 - 2h - h^2 - 4}{h} = \frac{-2h - h^2}{h} = \frac{h(-2-h)}{h} = -2-h$$

$$h \rightarrow 0 \rightarrow \boxed{-2 = m + a} = f'(1)$$

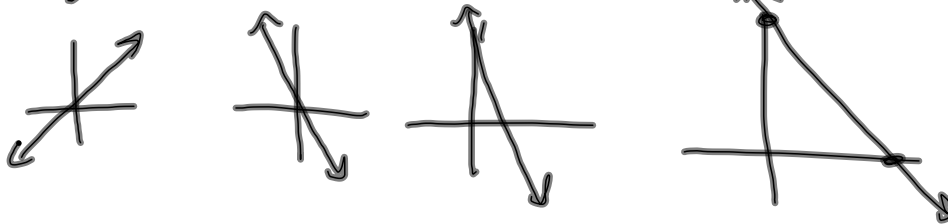
$$y = m(x - x_1) + y_1$$

$$y = m + a(x - x_1) + y_1$$

$$y = f'(x_1)(x - x_1) + f(x_1)$$

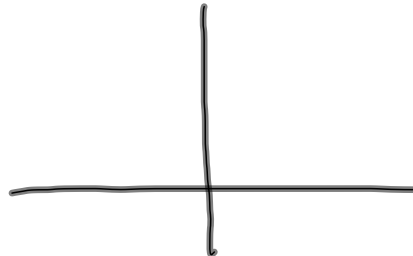
$$\boxed{y = -2(x - 1) + 4}$$

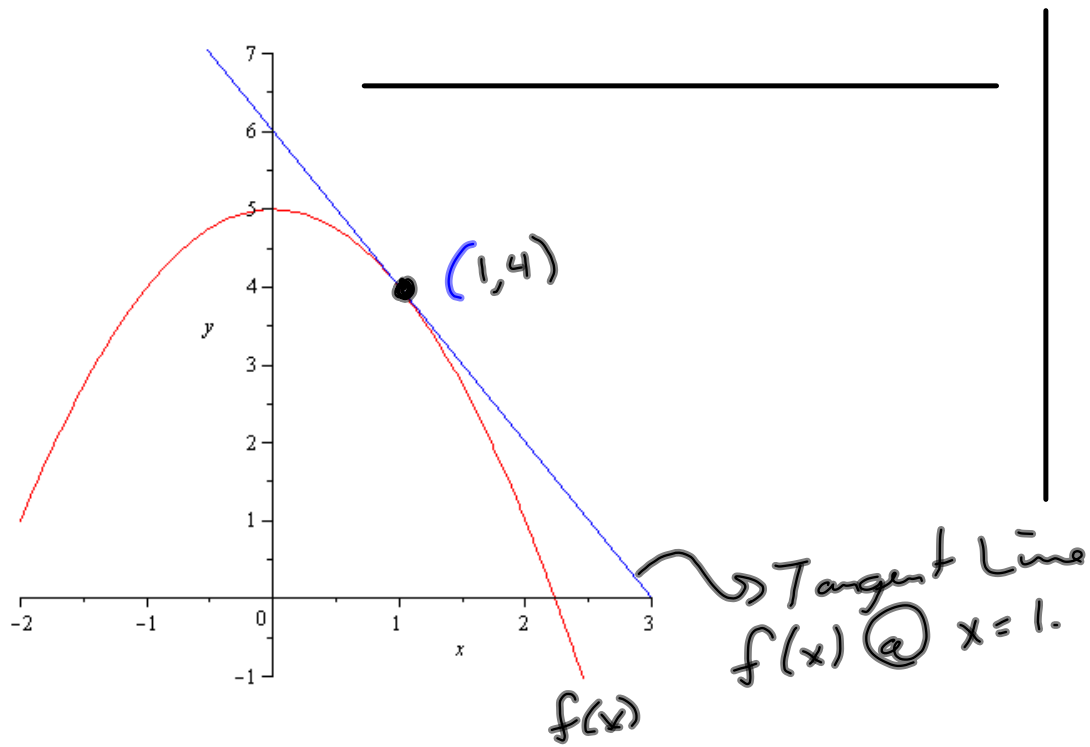
$$y = x \rightarrow -2x \rightarrow -2(x - 1) \rightarrow -2(x - 1) + 4$$

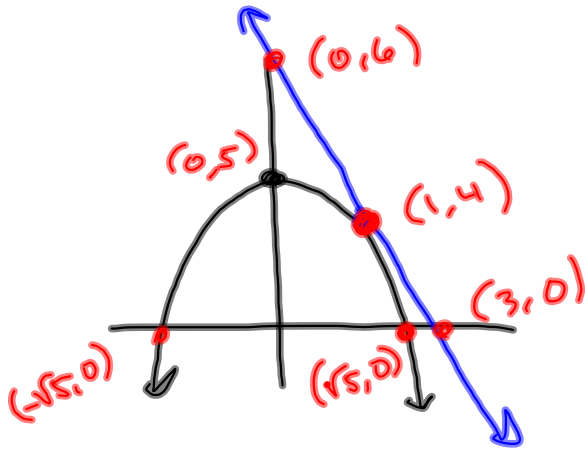


$$y = -2x + 2 + 4$$

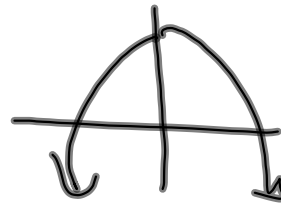
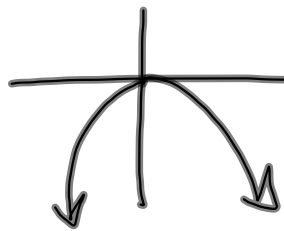
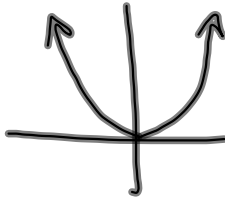
$$y = -2x + 6$$







$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$   
 $x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(4)}}{2(1)}$   
 $x = \frac{2 \pm \sqrt{4 - 16}}{2}$   
 $x = \frac{2 \pm \sqrt{-12}}{2}$   
 $x = \frac{2 \pm 2i\sqrt{3}}{2}$   
 $x = 1 \pm i\sqrt{3}$



$5 - x^2 = 0$

$5 = x^2$

$\sqrt{5} = \sqrt{x^2} = |x|$

$|x| = 5$

$x = \sqrt{5}$  OR  $x = -\sqrt{5}$   
 $x = \pm\sqrt{5}$

*Love this class.*

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$2ax = -b \pm \sqrt{b^2 - 4ac}$

$2ax + b = \pm \sqrt{b^2 - 4ac}$

$|2ax + b| = \sqrt{b^2 - 4ac}$

$(2ax + b)^2 = b^2 - 4ac$

$(\sqrt{x})^2 = x$

$\sqrt{x^2} = |x|$

$\sqrt{\sin^2 x} = |\sin x|$

$\sqrt{(-3)^2} = 3$   
 $\sqrt{9} = 3$

$$\lim_{x \rightarrow -3} \frac{x+3}{x^2+4x+3} = \lim_{x \rightarrow -3} \frac{x+3}{(x+1)(x+3)}$$

$$= \lim_{x \rightarrow -3} \frac{1}{x+1} = \frac{1}{-3+1} = -\frac{1}{2}$$

Evaluating Limits empirically (Digitally) by plugging in values is a good check, but not really legit.

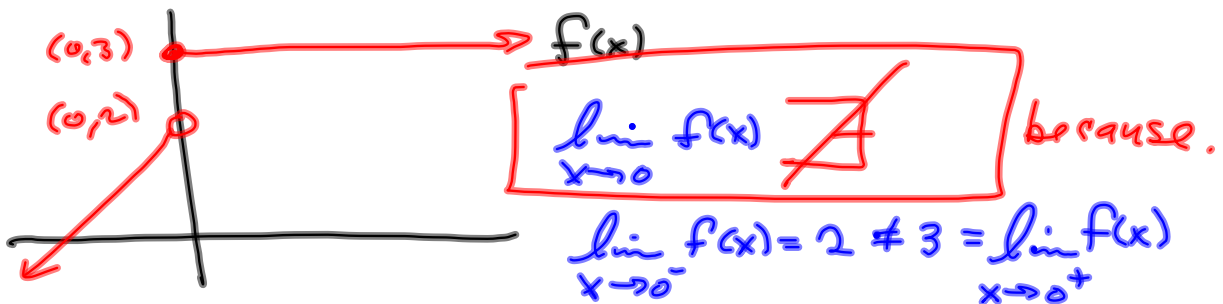
$$\lim_{h \rightarrow 0} \left( \frac{\sqrt{x+h} - \sqrt{x}}{h} \right) \cdot \left( \frac{\sqrt{x+h} + \sqrt{x}}{\sqrt{x+h} + \sqrt{x}} \right) \text{ etc.}$$

#55 §2.2

Given  $\lim_{x \rightarrow b} f(x) = 7$ ,  $\lim_{x \rightarrow b} g(x) = -3 \implies$

(a)  $\lim_{x \rightarrow b} (f(x) + g(x)) = 7 + (-3) = 4$ , etc.

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S'2.2 Due Monday

S'2.3 Due Wednesday

Shorthand S'2.3

$\exists$  - There is or There exists.

$\implies$  - Implies

$\exists$  - such that or so that

$\forall$  - For all or For each or For every.

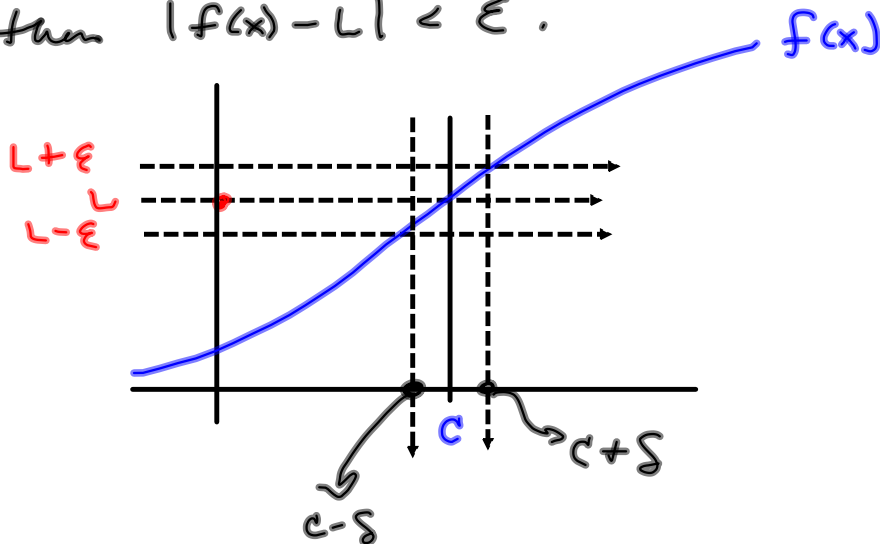
FORMAL DEFINITION OF  
LIMIT

$\mathbb{R}$  - reals  
 $\mathbb{N}$  - naturals  
 $\mathbb{Z}$  - integers

The limit, as  $x$  approaches  $c$ , of  $f(x)$  is  $L$  is written

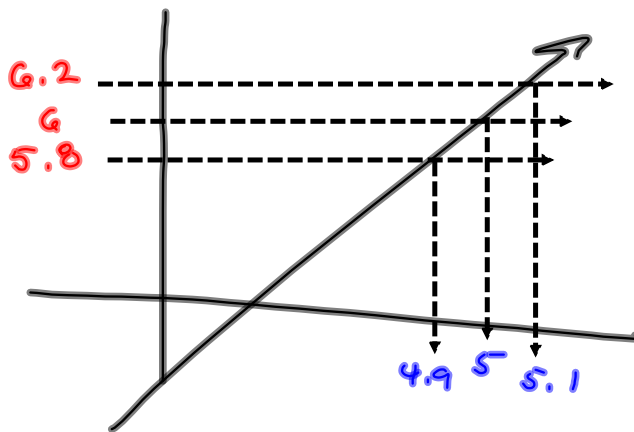
$$\lim_{x \rightarrow c} f(x) = L, \text{ which means}$$

Given  $\epsilon > 0$ ,  $\exists \delta > 0 \exists$  if  $0 < |x - c| < \delta$ , then  $|f(x) - L| < \epsilon$ .



§ 2.3 # 7

$f(x)$  pictured



$$f(x) = 2x - 4$$

$$x_0 = 5$$

$$L = 6$$

$$\epsilon = 0.2$$

Find  $\delta \ni \forall x$  with  $0 < |x - x_0| < \delta$ ,  
we have  $|f(x) - L| < \epsilon$

$\delta = 0.1$  keeps us in the window.