

$$|R_5(x)| \leq \frac{M}{6!} |x|^6, \text{ where } M \geq \max_{x \in [-0.8, 0.8]} |f^{(6)}(x)| = 3984.88... \quad 3984.881097$$

$\sinh(x)$ is odd & increasing

$$\sinh(-0.8) = -\sinh(0.8) \text{ and so } \max_{x \in [-0.8, 0.8]} |f^{(6)}(x)| = |f^{(6)}(0.8)|$$

$$f^{(6)}(x) = 729 \sinh(3x)$$

$$\sinh(x) = \frac{e^x - e^{-x}}{2}$$

$$\sin(x) = \frac{e^{ix} - e^{-ix}}{2i} \leftarrow \text{Forget the "i"}$$

$$\cosh(x) = \frac{e^x + e^{-x}}{2}$$

$$\cos(x) = \frac{e^{ix} + e^{-ix}}{2}$$

$$P(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_0$$

$$= (x-r_1) (a_n x^{n-1} + b_{n-2} x^{n-2} + b_{n-3} x^{n-3} + \dots + b_0)$$

$$= (x-r_2)(x-r_1) (a_n x^{n-2} + c_{n-3} x^{n-3} + \dots + c_0)$$

⋮

$$= a_n (x-r_n)(x-r_{n-1}) \dots (x-r_2)(x-r_1)$$

Fundamental
Theorem of
Algebra
APPLIED

n
TIMES

Split into
linear factors

$$(1)(4)(7) \rightarrow \text{Add } 3 \rightarrow 3n + C$$

$$n=4$$

$$3(4) + C = 7$$

$$C = -5$$

$$(1)(4)(7) \dots (3n-5)$$