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Do all your work and put all your answers WITH your work, CIRCLED, on the white paper provided. All I want on this sheet is your NAME! Spend no more than 2 minutes on any single problem on your first pass through the test. If you don't finish a problem in 2 or 3 minutes, start a fresh sheet of paper for the next problem, and so on.

Formatting should be the same as homework, only you don't need to re-state the question, because the question's attached to your test!

1. The function $f(x)=x^{2}-7 x-15$ is 1-to-1 on the restricted domain $D=\left[\frac{7}{2}, \infty\right)$.
a. (10 pts) Find the inverse function $f^{-1}(x)$. State its domain and range.
b. (5 pts) Find $\left(f^{-1}\right)^{\prime}(5)$, directly, by differentiating your answer for part a.
c. (5 pts) Find $\left(f^{-1}\right)^{\prime}(5)$ by applying a theorem regarding derivatives of inverse functions.
2. (5 pts each) Find the derivative with respect to $x$. All "-1" powers refer to function inverses, not reciprocals.
a. $y=3 \cdot 2^{\sin (x)}$
b. $y=\ln \left(\frac{\sqrt[5]{x^{2}-3 x}}{\sin ^{3}(x)}\right)$
c. $y=\log _{5}\left(\tan \left(x^{2}\right)\right)$
d. $y=\left[7 x^{3}-5 x\right]^{\cos (x)}$
e. $\quad \begin{gathered}y=\cos (x) \cdot \sin ^{-1}\left(5 x^{3}-7 x\right) \text { or } \\ \cos (x) \cdot \arcsin \left(5 x^{3}-7 x\right)\end{gathered}$
f. $\quad y=\sin (x) \cdot \cosh ^{-1}\left(5 x^{3}-7 x\right)$
3. (5 pts each) Evaluate the integrals
a. $\int \sec ^{2}(x) \cdot e^{\tan (x)} d x$
b. $\int \frac{d x}{5 x \sqrt{x^{2}-36}}$
4. (5 pts each) Simplify the following.
a. $\sec \left(\tan ^{-1}\left(\sqrt{9 x^{2}-100}\right)\right)$
b. $\sin ^{-1}\left(\sin \left(\frac{5 \pi}{4}\right)\right)$. I think you're OK on the domains, after class talk.
5. ( 10 pts ) The doubling time of an investment is 10 years. Assuming interest compounds continuously, what is the rate of interest?
6. (5 pts each) Evaluate the following limits:
a. $\lim _{x \rightarrow \infty}\left(1+\frac{3}{x}\right)^{5 x}$
b. $\lim _{x \rightarrow 0}\left(\frac{e^{2 x}-1}{\sin (x)}\right)$
c. $\lim _{x \rightarrow \frac{\pi^{-}}{2}}(\sec (x)-\tan (x))$

Bonus:

1. Find the volume of the solid of revolution obtained by revolving the function $y=\sqrt{x}$ about the $y$-axis in 2 ways:
a. (10 pts) Shell Method
b. (10 pts) Disk Method
