

$$(fg)' = f'g + fg'$$

$$-fg' = f'g - (fg)'$$

$$fg' = (fg)' - f'g$$

$$\int fg' = \int (fg)' - \int f'g$$

$$\int fg' = fg - \int f'g$$

$$\int u dv = uv - \int v du$$

$u$  = something we can differentiate  
(that preferably disappears after awhile)  
 $x^n = u$

$dv$  = something we can anti-differentiate

$$\int x \sin x \, dx$$

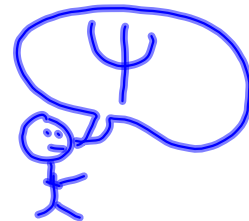
$$\int x e^x \, dx$$

$$u = x, \, dv = \sin x \, dx$$

$$du = dx, \, v = -\cos x$$

$$uv - \int v \, du = -x \cos x + \int \cos x \, dx$$

$$= \boxed{-x \cos x + \sin x + C}$$



$$\int \ln x \, dx$$

$$u = \ln x \quad du = \frac{1}{x} dx$$

$$dv = dx \quad v = x$$

$$\Rightarrow uv - \int v \, du = x \ln x - \int x \cdot \frac{1}{x} dx$$

$$= \boxed{x \ln x - x + C}$$

$$\int x^2 e^x dx \text{ requires two IBPs.}$$

$$u = x^2 \quad du = 2x dx$$

$$dv = e^x dx \quad v = e^x \quad \text{etc.}$$

## TABULAR METHOD

$$\int x^2 e^x dx$$

	u		dv	
①	$x^2$	+	$e^x$	
②	$2x$	-	$e^x$	
③	$2$	+	$e^x$	
	$0$	-	$e^x$	Done

→

$$\int x^2 e^x dx = x^2 e^x - 2x e^x + 2e^x + C$$

$$\int e^x \sin x \, dx$$

u		dv
sin x	+	e <sup>x</sup>
cos x	-	e <sup>x</sup>
-sin x	+	e <sup>x</sup>
-cos x	-	e <sup>x</sup>
sin x	+	e <sup>x</sup>
cos x	-	e <sup>x</sup>

$$\Rightarrow \int e^x \sin x \, dx = e^x \sin x - e^x \cos x - \int e^x \sin x \, dx \dots$$

Let  $u = \sin x$ ,  $du = \cos x \, dx$   
 $dv = e^x \, dx$ ,  $v = e^x$

$$\Rightarrow uv - \int v \, du = e^x \sin x - \int e^x \cos x \, dx$$

$u = \cos x$   $du = -\sin x \, dx$   
 $dv = e^x \, dx$   $v = e^x$

$$\Rightarrow e^x \sin x - [e^x \cos x + \int e^x \sin x \, dx] = \int e^x \sin x \, dx$$

$$* \int e^x \sin x \, dx = e^x \sin x - e^x \cos x - \int e^x \sin x \, dx + C$$

$$2 \int e^x \sin x \, dx = e^x \sin x - e^x \cos x + C$$

$$* \int e^x \sin x \, dx = \frac{e^x \sin x - e^x \cos x}{2} + C_1$$

where  $C = \frac{C_1}{2}$

Pg 439 What am I missing?

$$\int \cos^3 x \, dx$$

M2  $\cos^2 x$  8.2 way

$$= \int (1 - \sin^2 x) \cos x \, dx$$

$$= \int \cos x \, dx - \int \sin^2 x \cos x \, dx$$

$u^2 \cdot du$

$$= \sin x - \frac{\sin^3 x}{\frac{3}{3}} + C$$

SB.1 way

$$\int \cos^3 x \, dx = \int \cos^2 x \cos x \, dx$$

$$u = \cos^2 x \quad du = -2\cos x \sin x \, dx$$

$$dv = \cos x \, dx \quad v = \sin x$$

$$\Rightarrow uv - \int v \, du = \cos^2 x \sin x + 2 \int \sin^2 x \cos x \, dx$$

$$= \sin x \cos^2 x + \frac{2}{3} \sin^3 x + C$$

(1 - sin<sup>2</sup>x)

$$= \sin x - \frac{\sin^3 x}{3} + C$$

Book got

$$\frac{\sin x \cos^2 x}{3} + \frac{2}{3} \sin x + C$$

$$= \frac{\sin x - \sin^3 x}{3} + \frac{2}{3} \sin x + C$$

$$= \frac{\sin x}{3} - \frac{1}{3} \sin^3 x + C$$



OK. Book is OK  
I'm OK  
you're OK.

Homework :

 $2n$ 

1

$$\int \cos^5 x \, dx$$

$$\int \cos^6 x \, dx$$

ODD: Let  $du = \cos x \, dx$   
 (or  $\sin x \, dx$ , when  
 $\sin^{2n+1}(x) \, dx$ )

Even:

$$\sin^2 x = \frac{1 - \cos(2x)}{2}$$

$$\cos^2 x = \frac{1 + \cos(2x)}{2}$$

and write  $\cos^{2n} x$  as

$$(1 - \sin^2 x)^n \quad \rightarrow (\cos^2 x)^n$$

$$\int \cos^5 x \sin^2 x \, dx$$

$$= \int \sin^2 x \underbrace{(1 - \sin^2 x)^2}_{\cos^4 x} \cos x \, dx$$

$$\cos^4 x = (\cos^2 x)^2 = (\cos x)^2)^2$$

$$\downarrow$$

$$(1 - \sin^2 x)^2$$

= .

§ 8.1  
# 26, 32, 40, 54