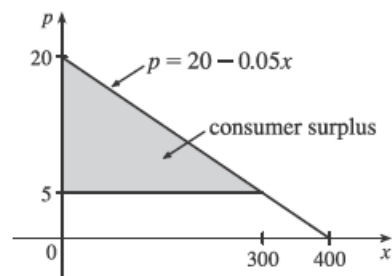


## 9.4 Solutions

$$\begin{aligned}
 4. \text{ Consumer surplus} &= \int_0^{300} [p(x) - p(300)] dx \\
 &= \int_0^{300} [20 - 0.05x - (5)] dx \\
 &= \int_0^{300} (15 - 0.05x) dx = [15x - 0.025x^2]_0^{300} \\
 &= 4500 - 2250 = \$2250
 \end{aligned}$$



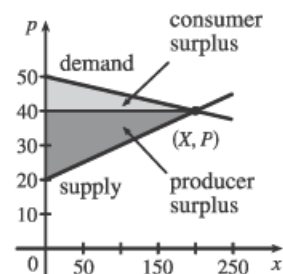
$$7. P = p_S(x) \Rightarrow 400 = 200 + 0.2x^{3/2} \Rightarrow 200 = 0.2x^{3/2} \Rightarrow 1000 = x^{3/2} \Rightarrow x = 1000^{2/3} = 100.$$

$$\begin{aligned}
 \text{Producer surplus} &= \int_0^{100} [P - p_S(x)] dx = \int_0^{100} [400 - (200 + 0.2x^{3/2})] dx = \int_0^{100} \left(200 - \frac{1}{5}x^{3/2}\right) dx \\
 &= \left[200x - \frac{2}{25}x^{5/2}\right]_0^{100} = 20,000 - 8,000 = \$12,000
 \end{aligned}$$

$$8. p = 50 - \frac{1}{20}x \text{ and } p = 20 + \frac{1}{10}x \text{ intersect at } p = 40 \text{ and } x = 200.$$

$$\text{Consumer surplus} = \int_0^{200} \left(50 - \frac{1}{20}x - 40\right) dx = \left[10x - \frac{1}{40}x^2\right]_0^{200} = \$1000$$

$$\text{Producer surplus} = \int_0^{200} \left(40 - 20 - \frac{1}{10}x\right) dx = \left[20x - \frac{1}{20}x^2\right]_0^{200} = \$2000$$



$$13. N = \int_a^b Ax^{-k} dx = A \left[ \frac{x^{-k+1}}{-k+1} \right]_a^b = \frac{A}{1-k} (b^{1-k} - a^{1-k}).$$

$$\text{Similarly, } \int_a^b Ax^{1-k} dx = A \left[ \frac{x^{2-k}}{2-k} \right]_a^b = \frac{A}{2-k} (b^{2-k} - a^{2-k}).$$

$$\text{Thus, } \bar{x} = \frac{1}{N} \int_a^b Ax^{1-k} dx = \frac{[A/(2-k)](b^{2-k} - a^{2-k})}{[A/(1-k)](b^{1-k} - a^{1-k})} = \frac{(1-k)(b^{2-k} - a^{2-k})}{(2-k)(b^{1-k} - a^{1-k})}.$$

$$15. F = \frac{\pi PR^4}{8\eta l} = \frac{\pi(4000)(0.008)^4}{8(0.027)(2)} \approx 1.19 \times 10^{-4} \text{ cm}^3/\text{s}$$

18. As in Example 2, we will estimate the cardiac output using Simpson's Rule with  $\Delta t = (20 - 0)/10 = 2$ .

$$\begin{aligned}
 \int_0^{20} c(t) dt &\approx \frac{2}{3}[c(0) + 4c(2) + 2c(4) + 4c(6) + 2c(8) + 4c(10) + 2c(12) + 4c(14) + 2c(16) + 4c(18) + c(20)] \\
 &= \frac{2}{3}[0 + 4(2.4) + 2(5.1) + 4(7.8) + 2(7.6) + 4(5.4) + 2(3.9) + 4(2.3) + 2(1.6) + 4(0.7) + 0] \\
 &= \frac{2}{3}(110.8) \approx 73.87 \text{ mg} \cdot \text{s}/\text{L}
 \end{aligned}$$

$$\text{Therefore, } F \approx \frac{A}{73.87} = \frac{8}{73.87} \approx 0.1083 \text{ L/s or } 6.498 \text{ L/min.}$$