

Rolle's:

Given: f cont^s on $[a,b]$,
 f diff^l on (a,b) , and $f(a) = f(b) = L$

$\Rightarrow \exists c \in (a,b) \ni f'(c) = 0$

Pf If $f(x) = L \forall x \in (a,b)$,
 then we're done. $f'(c) = 0 \forall c \in (a,b)$

If $f(x) > L$ anywhere, then f has
 an abs max in $[a,b]$, and it's not
 (a) a or b , so, by Fermat, $f'(c) = 0$ somewhere
 in (a,b)

If $f(x) < L$ anywhere, then f has an abs
 min^{*} in $[a,b]$ and it's not (a) a or b

By Fermat, $f'(c) = 0$

* at some $x = c$, i.e., $f(c)$ is a m.m.

