1.1 EXERCISES

1. If $f(x) = x + \sqrt{2-x}$ and $g(u) = u + \sqrt{2-u}$, is it true that f = g?

2. If

$$f(x) = \frac{x^2 - x}{x - 1}$$
 and $g(x) = x$ $\mathcal{O}(g) = \mathcal{R} = (-\infty, \infty)$

is it true that
$$f = g$$
?

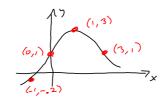
$$f(x) = \begin{cases} f(x) = x \\ f(x) = x \end{cases} = \begin{cases} f(x) = x \\ f(x) = x \end{cases}$$

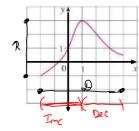
$$f(x) = \begin{cases} f(x) = x \\ f(x) = x \end{cases}$$

$$f(x) = \begin{cases} f(x) = x \\ f(x) = x \end{cases}$$

$$f(x) = \begin{cases} f(x) = x \\ f(x) = x \end{cases}$$

- 3. The graph of a function f is given.
 - (a) State the value of f(1).
 - (b) Estimate the value of f(-1).
 - (c) For what values of x is f(x) = 1?
 - (d) Estimate the value of x such that f(x) = 0.
 - (e) State the domain and range of f.
 - (f) On what interval is f increasing?

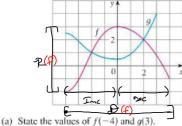




- (2) F(1)=3
- (b) f(-1) = -,2

(c)
$$f(x)=1 \Rightarrow x \approx 0,3$$

(d) $x \approx -1.6 \Rightarrow f(x)=0$

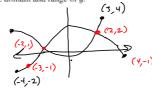


- (b) For what values of x is f(x) = g(x)?

The graphs of f and g are given.

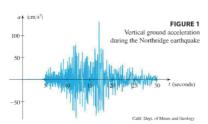
(b)
$$f(x) = g(x) \Rightarrow x = -2,2$$
(c) $f(x) = -1 \Rightarrow x \in \{-3,4\}$
(d) $f(x) = (-4,4) \Rightarrow x \in \{-3,4\}$
(f) $f(x) = (-4,4) \Rightarrow x \in \{-3,4\}$
(f) $f(x) = (-4,4) \Rightarrow x \in \{-3,4\}$

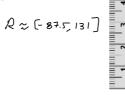
- (c) Estimate the solution of the equation f(x) = -1.
- (d) On what interval is f decreasing?
- (e) State the domain and range of f.
- (f) State the domain and range of g.



- (c) f(x)=-1 -> x & \ \ -3,4\}

5. Figure 1 was recorded by an instrument operated by the California Department of Mines and Geology at the University Hospital of the University of Southern California in Los Angeles. Use it to estimate the range of the vertical ground acceleration function at USC during the Northridge earthquake.





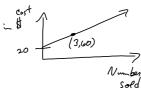
6. In this section we discussed examples of ordinary, everyday functions: Population is a function of time, postage cost is a function of weight, water temperature is a function of time. Give three other examples of functions from everyday life that are described verbally. What can you say about the domain and range of each of your functions? If possible, sketch a rough graph of each function.

Child's height as a function of age.

peed.

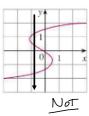
Fine as a function of speed.

Cost as a function of the number sold.

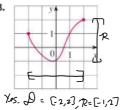


7–10 Determine whether the curve is the graph of a function of *x*. If it is, state the domain and range of the function.

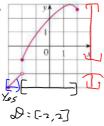
7.



8.



9.

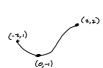


10.

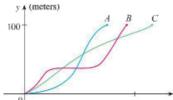


All are relations.

Not all are y=f(x)



14. Three runners compete in a 100-meter race. The graph depicts the distance run as a function of time for each runner. Describe in words what the graph tells you about this race. Who won the race? Did each runner finish the race?



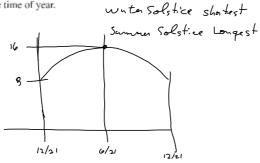
A: 41m the sace

B: Was wirning, Fell down,

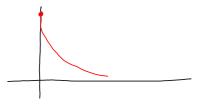
C: Slow, but steady. Camp is 3rd

0 20 t (seconds)

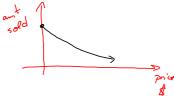
16. Sketch a rough graph of the number of hours of daylight as a function of the time of year.



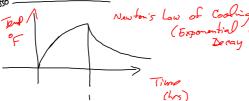
18. Sketch a rough graph of the market value of a new car as a function of time for a period of 20 years. Assume the car is well maintained.



19. Sketch the graph of the amount of a particular brand of coffee sold by a store as a function of the price of the coffee.



20. You place a frozen pie in an oven and bake it for an hour. Then you take it out and let it cool before eating it. Describe how the temperature of the pie changes as time passes. Then sketch a rough graph of the temperature of the pie as a function of time.



25. If $f(x) = 3x^2 - x + 2$, find f(2), f(-2), f(a), f(-a), f(a+1), 2f(a), f(2a), $f(a^2)$, $[f(a)]^2$, and f(a+h).

$$f(x) = 3(x)^{2} - 2 + 2 = 12 = f(x)$$

$$f(x) = 3(x)^{2} - 2 + 2 = 12 = f(x)$$

$$f(x) = 3(x)^{2} - (x) + 1 = 16 = f(x)$$

$$f(x) = 3(x)^{2} - (x) + 1 = 16 = f(x)$$

$$f(x) = 3(x)^{2} - 2 + 2$$

$$f(x) = 3(x)^{2} - 2 + 2$$

$$f(x) = 3(x)^{2} - 2 + 1 = 3(x^{2} + 2x + 1) - 3 + 1$$

$$= 3(x)^{2} - 2 + 1 = 3(x^{2} + 2x + 1) - 3 + 1$$

$$= 3(x)^{2} - 2 + 1 = 3(x^{2} + 2x + 1) - 3 + 1$$

$$= 3x^{2} + 6x + 3 - 3 + 1$$

$$= 3x^{2} + 6x + 3 - 3 + 1$$

$$= 3x^{2} - 2x + 1 + 2 = 16x$$

$$f(x) = 3(x)^{2} - 2x + 2$$

$$= (3x^{2} - 2x + 2) = 16x$$

$$f(x) = 3(x)^{2} - 2x + 2$$

$$= (3x^{2} - 2x + 2) = 16x$$

$$f(x) = 3(x)^{2} - 2x + 2$$

$$= (3x^{2} - 2x + 2) = 16x$$

$$= 9x^{2} - 3x^{2} + 6x^{2}$$

$$-3x^{3} + 6x^{2} - 2x + 2$$

$$= 3x^{3} + 6x^{3} - 2x + 2$$

$$= 3x^{3} + 6x + 3 + 2$$

$$= 3x^{3}$$

 $= 3(3+1)^{2} - (3+1) + 2$ $= 3(3+1)^{2} - (3+1) + 2$

= 322+62+3h2-3-4+2 = f(a+h). one, here

26. A spherical balloon with radius r inches has volume $V(r) = \frac{4}{3}\pi r^3$. Find a function that represents the amount of air required to inflate the balloon from a radius of r inches to a radius of r + 1 inches.

Now air added = Now Volume - Old Volume
=
$$\frac{4}{3}\pi \left[r+i\right]^3 - \frac{4}{3}\pi r^3$$

= $\frac{4}{3}\pi \left[r^3+3r^2+3r+1-r^3\right]$
= $\frac{4}{3}\pi \left[3r^2+3r+1\right]$
= $\frac{4}{3}\pi \left[3r^2+3r+1\right]$

27-30 Evaluate the difference quotient for the given function

Simplify your answer.

To see it, complete

To see it, complete

the square on find intercepts

$$h = m_{SC}$$

etc.

$$\frac{f(3+h)-f(3)}{h} = \frac{4+3(3+h)-(3+h)^2-[4+3(3)-3^2]}{h}$$

$$= \frac{4+9+3h-[3^2+6h+h^2]-(4)}{h} = \frac{13+3h-9-6h-42-4}{h}$$

29.
$$f(x) = \frac{1}{x}$$
, $\frac{f(x) - f(a)}{x - a} = Msec$

$$= \frac{3h - 6h - h^2}{h} = \frac{-3h - 6h^2}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \left[-3 - h\right] = \frac{f(3 + h) - f(3)}{h}$$

$$= \left[-3 - h\right] = \frac{f(3 + h) - f(3)}{h}$$

29.
$$f(x) = \frac{1}{x}$$
, $\frac{f(x) - f(a)}{x - a} = m_{SeC}$

$$= \frac{3h - (h - h^{2})}{h} = \frac{3h - (h^{2} - h)}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^{2})}{h} = \frac{h \left[-3 - h\right]}{h}$$

$$= \frac{3h - (h - h^$$

30.
$$f(x) = \frac{x+3}{x+1} = \frac{f(x) - f(1)}{x-1} = \frac{f(x) - f(a)}{x-2} = \frac{f(x+b) - f(x)}{b}$$

$$= \frac{\frac{x+3}{x+1} - \frac{1+3}{1+1}}{x-1} = \frac{\frac{y+3}{x+1} - \frac{y}{2}}{x-1} = \frac{\frac{y+3}{x+1} - 2(\frac{x+1}{x+1})}{x-1}$$

$$= \frac{\frac{x+3}{x+1} - (\frac{2x+2}{x+1})}{x-1} = \frac{\frac{y+3-2x-2}{x+1}}{x-1} = \frac{\frac{-x+1}{x+1}}{x-1} = \frac{1-x}{(x+1)(x-1)}$$

$$= \frac{-(x-1)}{(y+1)(y-1)} - \frac{-1}{x+1} = \frac{x+1}{x+1}$$

31-37 Find the domain of the function.

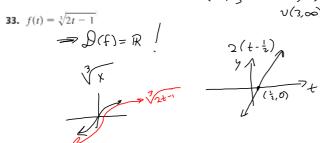
31.
$$f(x) = \frac{x+4}{x^2-9}$$

$$(x-3)(x+3) \neq 0$$

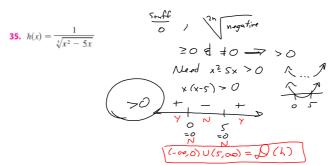
$$= \mathbb{R} \setminus \{-3,3\} = (-\infty,-3) \cup (-3,3) \cup (-3,3) \cup (-3,\infty)$$

33.
$$f(t) = \sqrt[3]{2t-1}$$

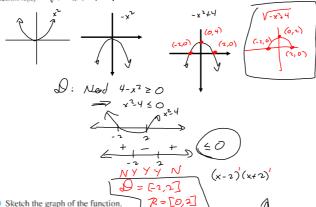




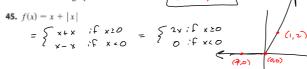
1-1-notes.notebook August 22, 2017



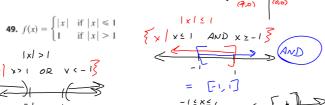
38. Find the domain and range and sketch the graph of the function $h(x) = \sqrt{4 - x^2}$. is tophall of random $x = \sqrt{4 - x^2}$.



45-50 Sketch the graph of the function.



49.
$$f(x) = \begin{cases} |x| & \text{if } |x| \le 1\\ 1 & \text{if } |x| > 1 \end{cases}$$



(-00,-1) U(1,00)



51-56 Find an expression for the function whose graph is the given curve.

51. The line segment joining the points (1, -3) and (5, 7)

$$w = \frac{7x - 7_1}{x_2 - x_1} = \frac{7 + 3}{5 - 1} = \frac{10}{4} = \frac{5}{5} = u_1$$

$$y = u_1(x - x_1) + y_1$$

$$y = \frac{5}{2}(x - 1) - 3 \quad \text{for} \quad 1 \le x \le 5$$

53. The bottom half of the parabola $x + (y - 1)^2 = 0$ Solve for y.

$$(y-1)^{2} = -x$$

$$(y-1)^{2} = -x$$

$$y-1 = \sqrt{-x}$$

$$y = \sqrt{-x} + 1$$

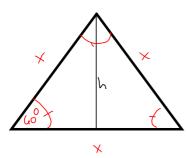
54. The top half of the circle $x^2 + (y - 2)^2 = 4$

57-61 Find a formula for the described function and state its domain.

57. A rectangle has perimeter 20 m. Express the area of the rectangle as a function of the length of one of its sides.

58. A rectangle has area 16 m². Express the perimeter of the rectangle as a function of the length of one of its sides.

59. Express the area of an equilateral triangle as a function of the length of a side.

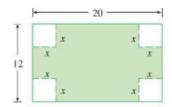


Ang = $\frac{1}{2}bh = \frac{1}{2}xh =$ $\frac{h}{x} = sico^{0} = \frac{\sqrt{3}}{2}$ $\Rightarrow h = \frac{\sqrt{3}}{2}x \Rightarrow$ $A = (\frac{1}{2}x)(\frac{\sqrt{3}}{2}x) = \frac{\sqrt{3}}{4}x^{2} = A(x)$



61. An open rectangular box with volume 2 m3 has a square base. Express the surface area of the box as a function of the length of a side of the base.

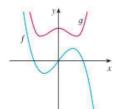
63. A box with an open top is to be constructed from a rectangular piece of cardboard with dimensions 12 in. by 20 in. by cutting out equal squares of side x at each corner and then folding up the sides as in the figure. Express the volume V of the box as a function of x.



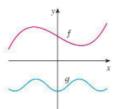


69–70 Graphs of f and g are shown. Decide whether each function is even, odd, or neither. Explain your reasoning.

69.



70.



- 71. (a) If the point (5, 3) is on the graph of an even function, what other point must also be on the graph?
 - (b) If the point (5, 3) is on the graph of an odd function, what other point must also be on the graph?

73–78 Determine whether f is even, odd, or neither. If you have a graphing calculator, use it to check your answer visually.

73.
$$f(x) = \frac{x}{x^2 + 1}$$

76.
$$f(x) = x |x|$$

74.
$$f(x) = \frac{x^2}{x^4 + 1}$$

77.
$$f(x) = 1 + 3x^2 - x^4$$

75.
$$f(x) = \frac{x}{x+1}$$

78.
$$f(x) = 1 + 3x^3 - x^5$$

1-1-notes.notebook

August 22, 2017