

(1) Spts Let  $f(x) = x^2 + 3x - 7$ . We apply the rules of differentiation.

(a) Differentiate  $f(x)$  w.r.t.  $x$ :

$$\frac{df}{dx} = 2x + 3$$

(b) Differentiate  $f(x)$  w.r.t.  $z$

$$\frac{df}{dz} = 0$$

$$\frac{dy}{dx} = \frac{df}{dx} = 2x + 3$$

(2) Spts we find the eq'n of the tangent line

$L_{-2}(x)$  to  $f(x)$  @  $x = -2$

$$L(x) = f'(x_1)(x - x_1) + f(x_1)$$

$$f'(x) = 2x + 3 \Rightarrow f'(x_1) = f'(-2) = 2(-2) + 3 = -1$$

$$f(x_1) = f(-2) = (-2)^2 + 3(-2) - 7 = 4 - 6 - 7 = 4 - 13 = -9$$

$$\Rightarrow L(x) = -1(x - (-2)) - 9 = -x - 2 - 9 = -x - 11$$

**STOP!**

(3) Spts we sketch  $f(x)$  &  $L(x) = L_{-2}(x)$  on same set of coordinate axes, with labels A, B, C, ... from left to right

$$f(x) = x^2 + 3x - 7 = x^2 + 3x + \left(\frac{3}{2}\right)^2 - \frac{9}{4} - \frac{28}{4}$$

$$= \left(x + \frac{3}{2}\right)^2 - \frac{37}{4} \rightarrow (h, k) = \left(-\frac{3}{2}, -\frac{37}{4}\right) = \text{vertex}$$

$$(-2, -9) = (x_1, f(x_1))$$

x-int:

$$\left(x + \frac{3}{2}\right)^2 = \frac{37}{4}$$

$$x = \frac{-3 \pm \sqrt{37}}{2}$$

$$\boxed{\text{y-int: } (0, -7)}$$

$$A = \left(\frac{-3 - \sqrt{37}}{2}, 0\right) \approx (-4.541381265, 0)$$

$$B = (0, -7)$$

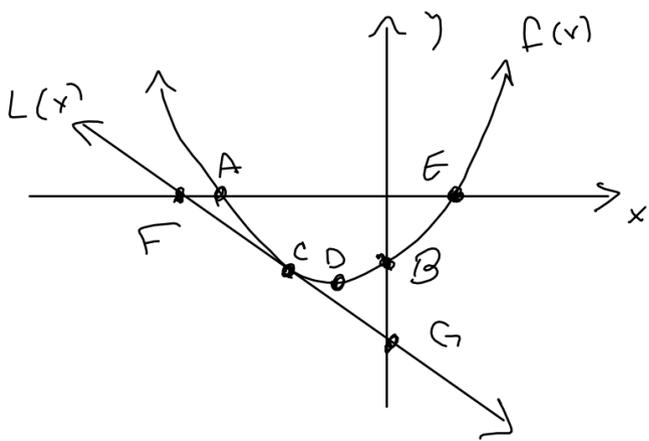
$$C = \left(-\frac{3}{2}, -9\right)$$

$$D = \left(-\frac{3}{2}, -\frac{37}{4}\right)$$

$$E = \left(\frac{-3 + \sqrt{37}}{2}, 0\right) \approx (1.541381265, 0)$$

$$F = (-11, 0)$$

$$G = (0, -11)$$



I guess I left off the x- & y-ints of  $L(x)$ :

$$y = -(x + 2) - 9$$

$$= -x - 2 - 9$$

$$= -x - 11$$

$$\begin{array}{r|l} x & y \\ 0 & -11 \\ -11 & 0 \end{array}$$

$$-x - 11 = 0$$

$$x = -11$$

2410

w#5

MILLS

4) We differentiate the following. We do not simplify. 1

a) 5pts  $F(y) = \left(\frac{1}{y^2} + \frac{2}{y^5}\right)(y^3 - y^7)$

$$= (y^{-2} + 2y^{-5})(y^3 - y^7) \rightarrow$$

$$F'(y) = (-2y^{-3} - 10y^{-6})(y^3 - y^7) + (y^{-2} + 2y^{-5})(3y^2 - 7y^6)$$

b) 5pts  $g(\theta) = \theta^2 \cos \theta \rightarrow g'(\theta) = 2\theta \cos \theta - \theta^2 \sin \theta$

c) 5pts  $h(x) = \frac{x^2 + 3x - 7}{x^3 + 1} \rightarrow$

$$h'(x) = \frac{(2x+3)(x^3+1) - (x^2+3x-7)(3x^2)}{(x^3+1)^2}$$

d) 5pts  $Q(\omega) = \frac{\omega^2 + \tan(\omega)}{\cos(\omega) + \omega} \rightarrow$

$$Q'(\omega) = \frac{(2\omega \tan(\omega) + \omega^2 \sec^2(\omega))(\cos(\omega) + \omega) - (\omega^2 + \tan(\omega))(-\sin(\omega) + 1)}{(\cos(\omega) + \omega)^2}$$

⑤ (5pts) Find eq'n of tangent line to  $y = \frac{5x}{x^2-4} = f(x)$  (a)  $x_1 = 3$

$$f'(x) = \frac{5(x^2-4) - 5x(2x)}{(x^2-4)^2} \Rightarrow$$

$$f'(3) = \frac{5(9-4) - 5(3)(2(3))}{(9-4)^2} = \frac{5(5) - 15(6)}{5^2}$$

$$= \frac{5(5-3(6))}{5^2} = \frac{5-18}{5} = -\frac{13}{5} = m_{\text{tan}}$$

$$f(3) = \frac{5(3)}{3^2-4} = \frac{15}{9-4} = \frac{15}{5} = 3 \Rightarrow (x_1, y_1) = (x_1, f(x_1)) = (3, 3)$$

$$L(x) = y = m_{\text{tan}}(x - x_1) + y_1$$

$$= f'(3)(x-3) + f(3)$$

$$= \left[ -\frac{13}{5}(x-3) + 3 = L(x) = y \right]$$

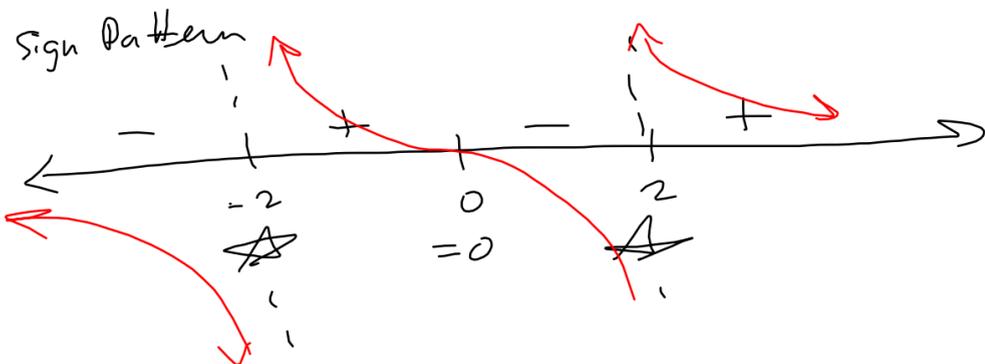
⑥ (5pts Bonus)  $f(x) = \frac{5x}{x^2-4}$

$$D = \mathbb{R} \setminus \{ \pm 2 \}$$

$x=2, x=-2$  are V.A.

H.A:  $f$  is proper  $\Rightarrow y=0$  is H.A.

$$f(x) = \frac{5x}{x^2-4} \stackrel{\text{SET } 0}{=} 0 \Rightarrow 5x=0 \Rightarrow x=0 \Rightarrow (0,0)$$



$$f(x) = \frac{5x}{x^2-4}$$

