

Power Rule, Product Rule, Quotient Rule

If $n \neq 0$, then $\frac{d}{dx}[x^n] = nx^{n-1}$

$$\begin{aligned}\frac{d}{dx}[3x^2 - 5x^{17}] &= \frac{d}{dx}[3x^2] - \frac{d}{dx}[5x^{17}] = 3\frac{d}{dx}[x^2] - 5\frac{d}{dx}[x^{17}] \\ &= 3 \cdot 2x - 5 \cdot 17x^{16} \\ &= 6x - 85x^{16}\end{aligned}$$

$$\begin{aligned}\frac{d}{dx}[x\sqrt{x}] &= \frac{d}{dx}[x^1 \cdot x^{\frac{1}{2}}] \\ &= \frac{d}{dx}[x^{1+\frac{1}{2}}] = \frac{d}{dx}[x^{\frac{3}{2}}] = \frac{3}{2}x^{\frac{3}{2}-1} = \frac{3}{2}x^{\frac{1}{2}}\end{aligned}$$

$$\frac{d}{dx}[x^{-20}] = -20x^{-21}$$

Product Rule

$$(fg)' = f'g + fg'$$

$$(fgh)' = f'gh + fg'h + fgh'$$

$$\begin{aligned}(fgh)' &= ((fg)h)' = (fg)'h + (fg)h' \\ &= (f'g + fg')h + fgh' \\ &= f'gh + fg'h + fgh'\end{aligned}$$

Quotient Rule

$$\left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$$

$$h(x) = \frac{3x+2}{7x-5} = \frac{f(x)}{g(x)} = \frac{f}{g} \rightarrow$$

$$\frac{g f' - f g'}{g^2} \text{ BOOK}$$

$$f(x) = 3x+2 \Rightarrow f'(x) = 3$$

$$g(x) = 7x-5 \Rightarrow g'(x) = 7$$

$$h'(x) = \frac{f'g - fg'}{g^2} = \frac{3(7x-5) - (3x+2)(7)}{(7x-5)^2} = \frac{21x-15-21x-14}{()^2}$$

STOP!

$$= \frac{-29}{(7x-5)^2}$$

$$\begin{aligned}\frac{d}{dx} \left[\frac{5x^3 + 7x^2 - 11}{\sqrt[3]{x}} \right] &= \frac{d}{dx} \left[\frac{5x^3}{x^{1/3}} + \frac{7x^2}{x^{1/3}} - \frac{11}{x^{1/3}} \right] \\&= \frac{d}{dx} \left[5x^{3-\frac{1}{3}} + 7x^{2-\frac{1}{3}} - 11x^{-\frac{1}{3}} \right] \\&= \frac{d}{dx} \left[5x^{\frac{8}{3}} + 7x^{\frac{5}{3}} - 11x^{-\frac{1}{3}} \right] = \frac{40}{3} x^{\frac{5}{3}} + \frac{35}{3} x^{\frac{2}{3}} + \frac{11}{3} x^{-\frac{4}{3}}\end{aligned}$$

2.3
#8 $g(x) = \frac{2x^2 + 6x + 2}{\sqrt{x}} = 2x^{2-\frac{1}{2}} + 6x^{1-\frac{1}{2}} + 2x^{-\frac{1}{2}}$

$$= 2x^{\frac{3}{2}} + 6x^{\frac{1}{2}} + 2x^{-\frac{1}{2}} \rightarrow$$

$$g'(x) = \underbrace{3x^{\frac{1}{2}} + 3x^{-\frac{1}{2}} - 1x^{-\frac{3}{2}}}_{\text{Acceptable to me \& WebAssign}} =$$

WebAssign says this, but accepts the other.

$$3\sqrt{x} + \frac{3}{\sqrt{x}} - \frac{1}{x\sqrt{x}}$$