

Questions for today?

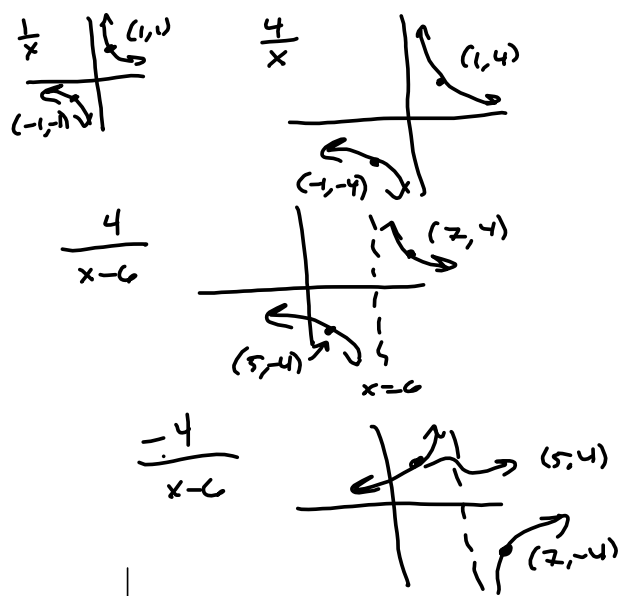
I'll have Week 2 Written Posted later today.

Grade Reports Coming Soon (today or tomorrow)

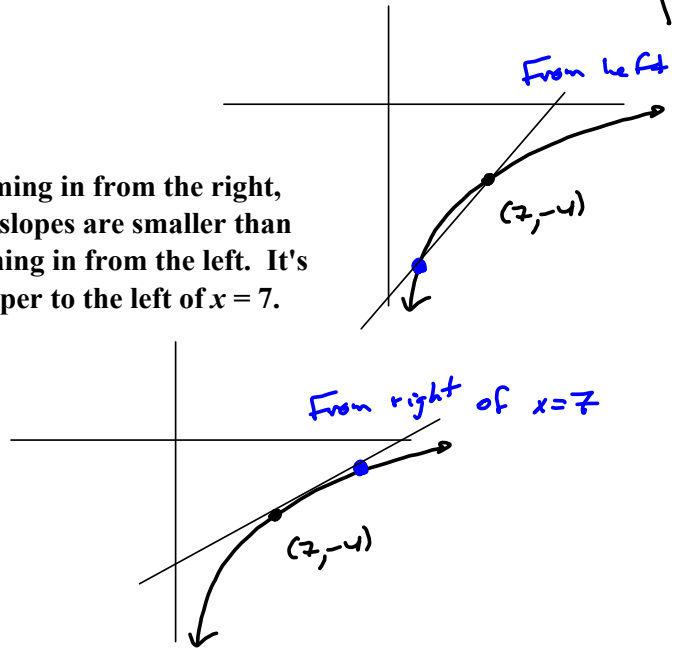
$(7, -4)$  lies on  $f(x) = y = \frac{4}{6-x} = -\frac{4}{x-6}$

(a) Find the slope of the secant line PQ correct to 6 decimal places for the following values of x:

- (i) 6.9
- (ii) 6.99
- (iii) 6.9999
- (iv) 6.99999
- (v) 7.1
- (vi) 7.01
- (vii) 7.001
- (viii) 7.0001



Coming in from the right, the slopes are smaller than coming in from the left. It's steeper to the left of  $x = 7$ .



Conclude  
 $m_{\text{tan}} @ x=7 \text{ is}$   
 $m_{\text{tan}} = 4$

Using Desmos to compute a bunch of slopes. The idea is to come closer and closer to  $x = 7$  to come closer and closer to the actual slope of the curve.

$f(x) = \frac{4}{6-x}$	×
$\frac{(f(6.9) - f(7))}{6.9 - 7}$	×
$= 4.444444444444$	
$\frac{(f(6.99) - f(7))}{6.99 - 7}$	×
$= 4.0404040404$	
$\frac{(f(6.9999) - f(7))}{6.9999 - 7}$	×
$= 4.00040004$	

Aiming for  $f'(7)$  for this function.

$\frac{4}{6-x} = f(x)$ . Aiming  $\textcircled{a}$

$$\frac{f(7+h) - f(7)}{h} \quad \frac{1}{x}$$

$$= \frac{\frac{4}{6-(7+h)} - \frac{4}{6-7}}{h}$$

$$= \frac{\frac{4}{-1-h} - \frac{4}{-1}}{h}$$

$$= \frac{-\frac{4}{1+h} + \frac{4}{1}}{h} = \frac{-4 + 4(1+h)}{1+h} \cdot \frac{1}{h}$$

$$= \frac{-4 + 4 + 4h}{1+h} = \frac{4h}{1+h} \cdot \frac{1}{h}$$

$$= \frac{1}{h} \left[ \frac{4h}{1+h} \right] = \frac{4}{1+h} \xrightarrow{h \rightarrow 0} \frac{4}{1} = m_{tan}$$

By hand (ugh!)

$$\frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(6.9) - f(7)}{6.9 - 7} = \frac{\frac{4}{6-6.9} - \frac{4}{6-7}}{6-7} = \frac{\frac{4}{-.9} - \frac{4}{-1}}{-1}$$

$$= \frac{\frac{4}{.9} - \frac{4}{1}}{-1} = \frac{4 - 4(.9)}{-.9} = \frac{4(1-.9)}{-.9} = \frac{4(.1)}{-.9} = \frac{.4}{-.9} = \frac{4}{9}$$

$$\begin{array}{r} .44\dots \\ 9 \overline{) 4.0000} \\ \underline{3.6} \phantom{00} \\ .4000 \end{array}$$

$$\approx \boxed{.444444}$$