

- (a) For the limit $\lim_{x \rightarrow 1} (x^3 + x + 3) = 5$, use a graph to find a value of δ that corresponds to $\epsilon = 0.4$. (Round your answer down to three decimal places.)

$\delta =$ ✓

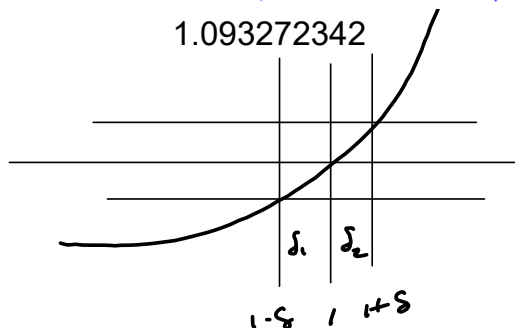
Gives the smaller value of δ .

- (b) By solving the cubic equation $x^3 + x + 3 = 5 + \epsilon$, find the largest possible value of δ that works for any given $\epsilon > 0$.

$\delta(\epsilon) =$ ✗ $\frac{(216 + 108\epsilon + 12\sqrt{336 + 324\epsilon + 81\epsilon^2})^{2/3} - 12}{6(216 + 108\epsilon + 12\sqrt{336 + 324\epsilon + 81\epsilon^2})^{1/3}} - 1$

- (c) Put $\epsilon = 0.4$ in your answer to $\frac{(216 + 108\epsilon + 12\sqrt{81\epsilon^2 + 324\epsilon + 336})^{2/3} - 12}{6(216 + 108\epsilon + 12\sqrt{81\epsilon^2 + 324\epsilon + 336})^{1/3}}$

$\delta(0.4) =$ ✗ $\frac{(216 + 108\epsilon + 12\sqrt{81\epsilon^2 + 324\epsilon + 336})^{2/3} - 12}{6(216 + 108\epsilon + 12\sqrt{81\epsilon^2 + 324\epsilon + 336})^{1/3}}$



$\delta_1 > \delta_2$ because it's concave up. (getting more steep)