

S 1.1 # 21 (WebAssign)

$$f(x) = \frac{x+7}{x+2}$$

$$\frac{f(x) - f(3)}{x - 3} =$$

$$= \frac{\frac{x+7}{x+2} - \frac{3+7}{3+2}}{x-3}$$

$$= \frac{\frac{x+7}{x+2} - \frac{10}{5}}{x-3} = \frac{1}{x-3} \left( \frac{x+7}{x+2} - \frac{2}{1} \cdot \left( \frac{x+2}{x+2} \right) \right)$$

$$= \frac{1}{x-3} \left( \frac{x+7 - 2(x+2)}{x+2} \right) = \left( \frac{x+7 - 2x - 4}{x+2} \right) \left( \frac{1}{x-3} \right)$$

$$= \left( \frac{-x+3}{x+2} \right) \left( \frac{1}{x-3} \right) = \left( \frac{-(x-3)}{x+2} \right) \left( \frac{1}{x-3} \right) = \boxed{\frac{-1}{x+2}}$$

$$\frac{f(x+h) - f(x)}{h}$$

OR

$$\frac{f(x) - f(c)}{x - c}$$

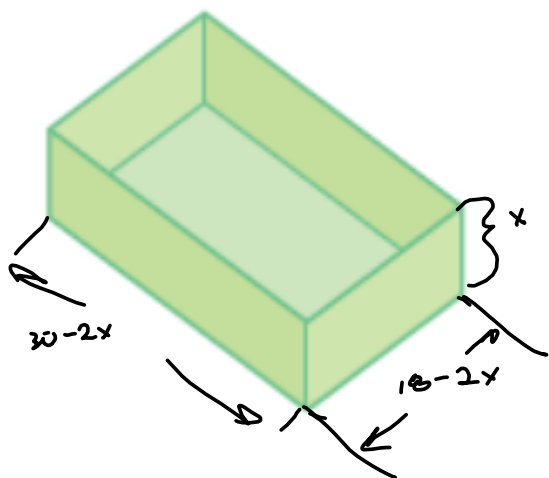
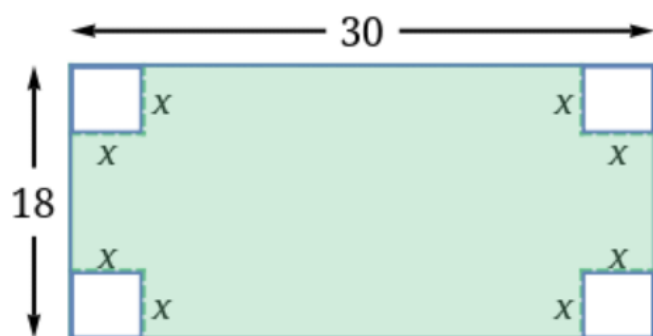
where

$$x+h \text{ is } x$$

$$c \text{ is } x$$

Grade Reports will be sent to you, later today.

Writing Project #0? We'll talk about that, tomorrow.



$$\Rightarrow \text{Volume is}$$

$$x(30-2x)(18-2x)$$

$$= H(L)(W)$$

$$4x^3 - 96x^2 + 540x$$

(Copy-Paste from Maple Computer Algebra System, because I'm lazy and insecure.

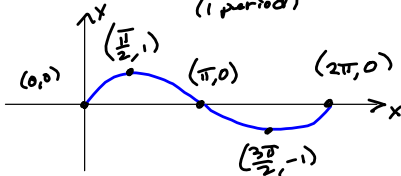
Section 1.3 - Transformations of Functions

$$\begin{aligned}
 & f(x) \\
 & 2f(x) \\
 & f(bx) \\
 & f(x+c) \\
 & f(x) + d
 \end{aligned}
 \left. \vphantom{\begin{aligned} f(x) \\ 2f(x) \\ f(bx) \\ f(x+c) \\ f(x) + d \end{aligned}} \right\} 2f(bx+c) + d$$

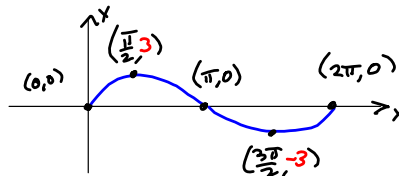
$$f(x) = \sin(x) \rightarrow 3f\left(\frac{\pi}{6}x + \frac{7\pi}{6}\right) + 11 = 3\sin\left(\frac{\pi}{6}x + \frac{7\pi}{6}\right) + 11$$

STEPS:

$$f(x) = \sin(x) \quad (1 \text{ period})$$

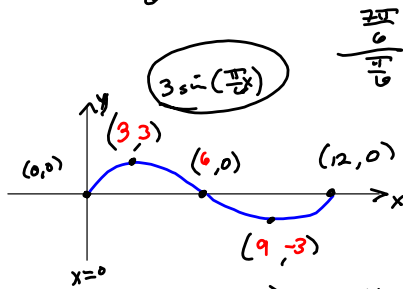


$$3f(x) = 3\sin(x) \quad : y \mapsto 3y$$



$$3\sin\left(\frac{\pi}{6}(x+7)\right) + 11$$

$$\frac{\pi}{6}x + \frac{7\pi}{6} = \frac{\pi}{6}(x+7)$$



$$\frac{2\pi}{\frac{\pi}{6}} = \frac{2\pi \cdot 6}{\pi} = 12$$

$$\frac{\frac{\pi}{6}}{\frac{\pi}{12}} = \frac{\frac{\pi}{6} \cdot 12}{\pi} = 2$$

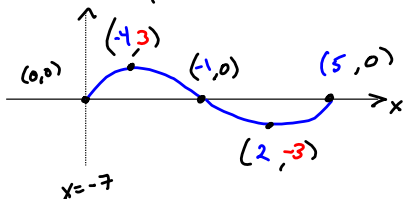
$$\frac{3\pi}{2} \cdot \frac{6}{\pi} = 9$$

$$f\left(\frac{\pi}{6}x\right) : x \mapsto \frac{1}{\frac{\pi}{6}}x$$

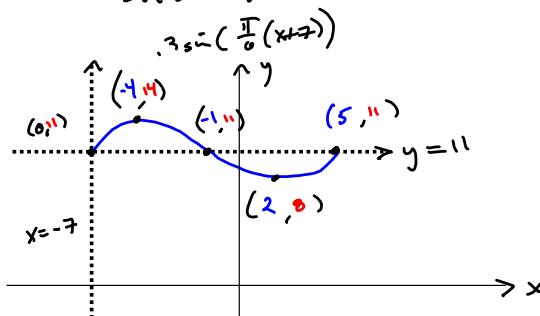
$$f(bx) : x \mapsto \frac{1}{b}x$$

$$3\sin\left(\frac{\pi}{6}(x+7)\right)$$

$$f(x+7) : x \mapsto x-7$$



$$3f\left(\frac{\pi}{6}(x+7)\right) + 11 = 3\sin\left(\frac{\pi}{6}(x+7)\right) + 11 \quad : y \mapsto y+11$$



If graphing by transforming is foreign to you, I have some stuff on the College Algebra website that talks about this:

It's on [harryzaims.com](http://harryzaims.com), right above our class!

Writing Project #2 for College Algebra is where this skill is covered.

College Trig Approach to trig functions, in particular....

$$3 \sin\left(\frac{\pi}{6}x + \frac{7\pi}{6}\right) + 11$$

$$= 3 \sin\left(\frac{\pi}{6}(x+7)\right) + 11$$

Amplitude  $\uparrow$   
 Wavelength  $\uparrow$   
 $\frac{\pi}{6}x = 2\pi$   
 $x = 2\pi \cdot \frac{6}{\pi} = 12$   
 Phase Sh.  $\uparrow$   
 $x \mapsto x-7$   
 Midline:  $y = 11$