Two curves are orthogonal if their tangent lines are perpendicular at each point of intersection. Are the given families of curves orthogonal trajectories of each other? That is, is every curve in one family orthogonal to every curve in the other

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 $y = cx^2$, $x^2 + 2y^2 = k$ es, the given families of curves are orthogonal trajectories.



Sketch both families of curves on the same axes.

I'm not getting negative reciprocals for the slopes.

$$x^{2}+2y^{2}=K$$
 $2x+4yy'=0$

$$y'=-\frac{2y}{4y}=-\frac{x}{2y}=\pm \sqrt{\frac{K-x^{2}}{2}}$$
 No

The WebAssign "Watch It" is much better than my treatment.

I left out looking for the slope when the curves intersect. They occur when $y = cx^2$ Substitute cx^2 for y in the equation $y' = -x/(2y) = -x/(2(cx^2)) = -x/(2cx) = -x/($

2.8 Related Rates

- **2.** (a) If A is the area of a circle with radius r and the circle expands as time passes, find dA/dt in terms of dr/dt.
 - (b) Suppose oil spills from a ruptured tanker and spreads in a circular pattern. If the radius of the oil spill increases at a constant rate of 1 m/s, how fast is the area of the spill increasing when the radius is 30 m?

(b)
$$\frac{dA}{dt} = 2\pi r \cdot \frac{dr}{dt} = \frac{dA}{dt} \cdot \frac{m^2}{s^2}$$

Given:

$$\frac{A = A(r) = \sigma r^2}{A = A(r)}$$

Assume $r = r(t)$ is a function of time. $\Rightarrow A = A(r(t))$

We find $\frac{dr}{dt}$.

$$= \frac{dA}{dr} \cdot \frac{dr}{dt} = \frac{dA}{dr} \cdot \frac{dr}{dt} = \frac{dA}{dr} \cdot \frac{m^2}{dt}$$

$$= \frac{dA}{dr} \cdot \frac{dr}{dt} = \frac{dA}{dr} \cdot \frac{dr}{dt} = \frac{dA}{dt} \cdot \frac{m^2}{s^2} = \frac{dA}{dt}$$

(b) $\frac{dA}{dt} = 2\pi r \cdot \frac{dr}{dt} = \frac{dA}{dt} \cdot \frac{m^2}{s^2} = \frac{dA}{dt}$

$$= 2\pi r \cdot \frac{dr}{dt} = \frac{dA}{dt} \cdot \frac{dr}{dt} = \frac{dA}{dt} \cdot \frac{m^2}{s^2} = \frac{dA}{dt}$$

Given:

Falling Body, by Newton

Letter, a counds. Then

$$h(H) = height of a body in free full, where

 $h(H) = -\frac{1}{2}gt^{2} + v_{0}t + h_{0}$, where

 $v_{0} = u_{0}thal velocity and$
 $h_{0} = initial height$

There are both

 $g = \sqrt{\frac{92}{52}} = \sqrt{\frac{9}{10}} \frac{m}{52}$ (on Earth) the wrong sign, given

 $f(H) = h'(t) = velocity = \frac{dh}{dt} = speed$

The contribution of

 $f(H) = huight of a body in free full, where

 $f(H) = u_{0} = u_{0} = u_{0} = u_{0}$

The model!

The are both

 $f(H) = u_{0} = u_{0} = u_{0} = u_{0} = u_{0}$

The contribution of

 $f(H) = u_{0} = u_{0$$$$

