

S'6.3 II #4 Find the inverse

$$f(x) = y = (\ln(x))^4$$

$$x = (\ln(y))^4 = x \quad \text{Solve for } y$$

$$\sqrt[4]{(\ln(y))^4} = \sqrt[4]{x} \quad \text{so } \sqrt[4]{x} \text{ is real.}$$

$$e^{\ln(y)} = e^{\sqrt[4]{x}} \quad \text{means } y = e^{\sqrt[4]{x}}$$

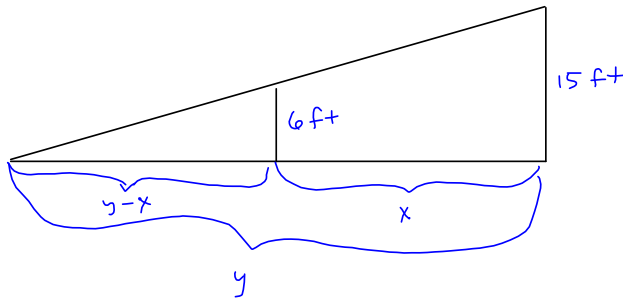
I prefer

$$y = e^{\sqrt[4]{x}}$$

Give a shout! I'm lurking, nearby! I'll probably do a related rates example, from Chapter 2, to help with the comprehensive (Chapters 1 - 4) part of the Final.

This is one like #15 in the Related-Rates section. I think it's 2.7, 2.8 or 2.9. Checking... Yeah. 2.8 #15 from the 8th Edition.

15. A street light is mounted at the top of a 15-ft-tall pole. A man 6 ft tall walks away from the pole with a speed of 5 ft/s along a straight path. How fast is the tip of his shadow moving when he is 40 ft from the pole?



GIVEN

$$\frac{dx}{dt} = x' = 5 \frac{\text{ft}}{\text{s}}$$

WANT

$$\frac{dy}{dt} \Big|_{x=40 \text{ ft}}$$

"Similar triangles thing going on, here..."

$$\frac{15}{y} = \frac{6}{y-x} \Rightarrow$$

$$\Rightarrow 15(y-x) = 6y$$

$$15y - 15x = 6y$$

$$9y = 15x$$

$$\frac{d}{dt} \left[ y = \frac{15}{9}x = \frac{5}{3}x \right]$$

$$\frac{dy}{dt} = \frac{5}{3} \frac{dx}{dt} = \frac{5}{3} \cdot 5 = \frac{25}{3} \text{ ft/s} = \frac{dy}{dt}$$

Note  $\frac{dy}{dt}$  is a constant!

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