

St.5 Avg Value

$$y_{AVG} = \frac{1}{b-a} \int_a^b f(x) dx$$

f is cont^l for this to work.

if it is then you might be asked to find y_{AVG} AND find x , where $f(x) = y_{AVG}$.

(a) Net Displacement $t^2 - 5t + 6$

$$\int_0^4 (t^2 - 5t + 6)$$

(b) Total Displacement

$$\int_0^4 |t^2 - 5t + 6| dt$$

we analyze sign pattern for $t^2 - 5t + 6$:

$$t^2 - 5t + 6 = 0$$

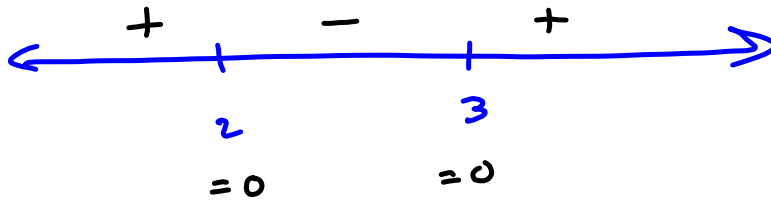
$$(t-3)(t-2) = 0$$

$$t = 2, 3$$

$$t^2 + \begin{matrix} \nearrow - \\ \searrow + \end{matrix}$$

$$t=0 \quad y=6$$

$$t=2.5 \quad y=?$$



$$\int_0^2 (t^2 - 5t + 6) dt - \int_2^3 (t^2 - 5t + 6) dt$$

$$+ \int_3^4 (t^2 - 5t + 6) dt$$

$$|t^2 - 5t + 6| = \begin{cases} t^2 - 5t + 6 & \text{if } t \leq 2 \text{ OR } t \geq 3 \\ -(t^2 - 5t + 6) & \text{if } 2 < t < 3 \end{cases}$$

§ 5.4 # 13

$\frac{1}{2} \text{ lb/ft}$

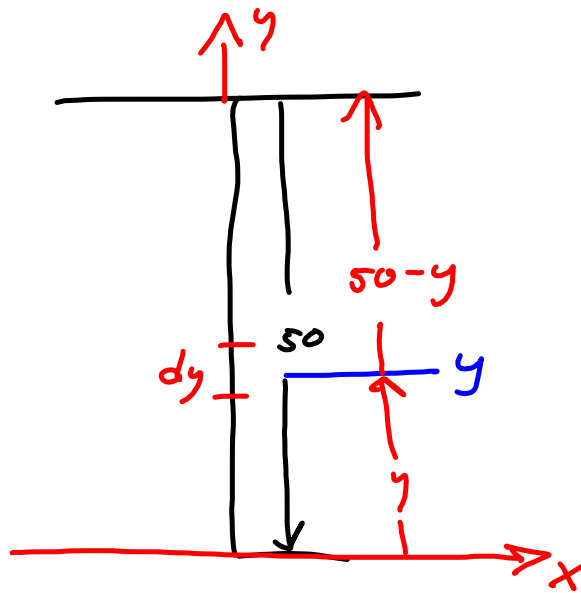
$$\int_0^{50} dy$$

$$\begin{aligned} \text{Force} &= \left(\frac{1}{2} \text{ lb/ft} \right) (dy \text{ ft}) \\ &= .5 dy \text{ lbs} \end{aligned}$$

Distance moved:

$50 - y \text{ ft}$

$$\text{Work} = \int_0^{50} (.5)(50 - y) dy$$



Work =
Force times
distance