



$$y = y(t) = 300t$$

want $\frac{dx}{dt}$ | $t = 1 \text{ min} = \frac{1}{60} \text{ hr}$

~~$$\frac{z+1}{x} = \sin \theta \qquad \frac{z}{y} = \sin \frac{\pi}{6} = \frac{1}{2}$$~~

~~$$z+1 = x \sin \theta$$~~

$$z = \frac{1}{2}y$$

~~$$x = (z+1) \csc \theta$$~~

~~$$x = \left(\frac{1}{2}y + 1\right) \csc \theta = \left(\frac{1}{2}y + 1\right) \frac{x}{w}$$~~

~~$$\frac{z}{w} = \tan \theta$$~~

~~$$z = w \tan \theta$$~~

~~$$\frac{1}{2}y = w \tan \theta = \left(y \cdot \frac{\pi}{6}\right)$$~~

$$\frac{w}{y} = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

$$w = \frac{\sqrt{3}}{2} y$$

$$\frac{z+1}{w} = \tan \theta$$

$$w^2 + (z+1)^2 = x^2 \quad \text{Aha!}$$

$$2ww' + 2(z+1)z' = 2xx'$$

Want x'

$$\frac{w}{y} = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2} \implies$$

$$w = \frac{\sqrt{3}}{2} y$$

$$w' = \frac{\sqrt{3}}{2} y' = \frac{\sqrt{3}}{2} \cdot 300$$

$$w' = 150\sqrt{3} \frac{\text{km}}{\text{hr}}$$

$$z = \frac{1}{2} y$$

$$z' = \frac{1}{2} y'$$

$$z' = \frac{1}{2} (300) = 150 \frac{\text{km}}{\text{hr}} = z'$$

$t = 1 \text{ min}$

~~$$x^2 = \left(\frac{\sqrt{3}}{2} y\right)^2 + \left(\frac{1}{2} y + 1\right)^2$$~~

$$y |_{t=0} = 5$$

$$y=5 \implies w = \frac{5\sqrt{3}}{2}, \quad z = \frac{5}{2}$$

$$x^2 = \left(\frac{5\sqrt{3}}{2}\right)^2 + \left(\frac{5}{2} + 1\right)^2 = \frac{25 \cdot 3}{4} + \left(\frac{7}{2}\right)^2$$

$t = 1 \text{ min}$

$$= \frac{75}{4} + \frac{49}{4} = \frac{124}{4} = \frac{62}{2} = 31 = x^2$$

$$\Rightarrow x = \sqrt{31} \text{ when } t = 1 \text{ min}$$

$$x x' = w w' + (z+1) z'$$

$$\sqrt{31} x' = \frac{5\sqrt{3}}{2} \cdot 150\sqrt{3} + \left(\frac{5}{2} + 1\right)(150)$$

$$\cancel{z = \frac{1}{2} \cdot \frac{5}{2}} = 5 \cdot 3 \cdot 75 + \left(\frac{7}{2}\right)(150)$$

$$= 1125 + 525$$

$$= 1650 = \sqrt{31} x'$$

$$x' = \frac{1650}{\sqrt{31}} \approx 296.3487483$$
$$\approx 296 \text{ km/hr}$$

Woo-Hoo!

Text uses Law of Cosines.

Big Deal. Who remembers that?!