

201

~~§ 5.1 #s 35, 37~~

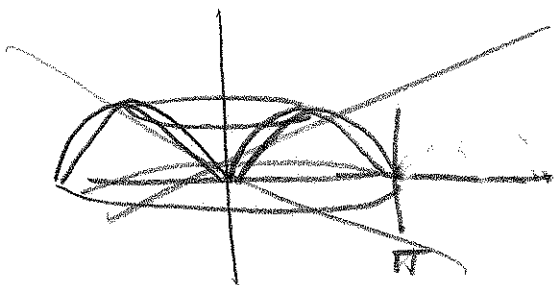
This is § 5.3 #35!

Find Exact

#s 35, 36 use CAS to ~~estimate~~ x-coords of intersections

Find exact volume of the solid obtained by rotating the region bounded by the given curves about the specified line

(35) $y = \sin^2 x$, $y = \sin^4 x$, $0 \leq x \leq \pi$ about $x = \frac{\pi}{2}$



$\sin^4 x$ is underneath.

$\sin^4 x = \sin^2 x$ @ $x = \frac{\pi}{2}, 0, \pi$

Outer - inner

Washer Method, right-left (upper-lower) on the radius

Right : $y = \sin^2 x$ } outer washer
 Left : $y = \sin^4 x$

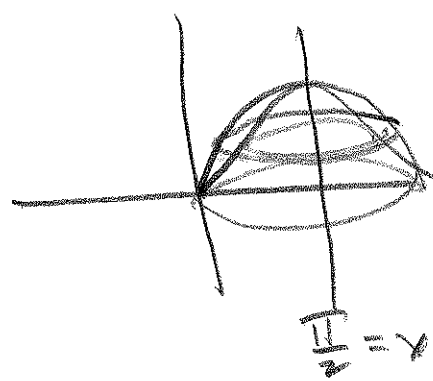
Then again

~~Right : $\sin^4 x$ } inner washer.
 Left : $\sin^2 x$~~

wait : rotating about $x = \frac{\pi}{2}$, we have some

symmetry

Better pic.



outer : $y = \sin^2 x$

$\sqrt{y} = \sin x$

$x = \arcsin(\sqrt{y})$

Inner :

$x = \arcsin(\sqrt[4]{y})$

$y = [0, 1]$

201 §5.1 #535, 37

35 cont'd

$$\pi \int_0^1 \left((\arcsin(y^{\frac{1}{2}}))^2 - (\arcsin(y^{\frac{1}{4}}))^2 \right) dy = \boxed{-\frac{1}{32} \pi^3}$$

is the setup, I think.

See attached
Maple transcript.

oops! Worked the wrong one!