

#s 1 – 3: Graph the function, by hand, by transforming a basic function.

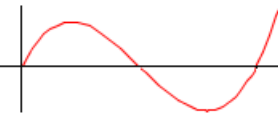
1. $y = \frac{1}{2}(1 - \cos(x))$

2. $y = 1 - 2x - x^2$

3. $y = |\sqrt{x} - 1|$

4. The graph of $f(x)$ is given, for $x \geq 0$.

Graph of $f(x)$, for $x \geq 0$



a. Explain how the graph of $f(|x|)$ is obtained from the graph of $f(x)$.

Supply the graph of $f(|x|)$. Is $f(|x|)$ even, odd, or neither?

b. If $f(x) = \sin(x)$, what is $f(|x|)$? Give me a sketch of $f(|x|)$.

c. If $f(x) = \sqrt{x}$, what is $f(|x|)$? Give me a sketch of $f(|x|)$.

5. Given $f(x) = x^3 + 2x^2$ and $g(x) = 3x^2 - 1$, find – and simplify – the following functions, and state the domain of each.

a. $(f + g)(x)$

b. $(f - g)(x)$

c. $(fg)(x)$

d. $\left(\frac{f}{g}\right)(x)$

In the following exercises, find (a) $(f \circ g)(x)$, (b) $(g \circ f)(x)$, (c) $(f \circ f)(x)$, and (d) $(g \circ g)(x)$. State the domain of each function.

6. $f(x) = x^2 - 1$, $g(x) = 2x + 1$

7. $f(x) = x + \frac{1}{x}$, $g(x) = \frac{x+1}{x+2}$

8. Express $F(x) = \frac{\sqrt[3]{x}}{\sqrt[3]{x+1}}$ as a composition $(f \circ g)(x)$.

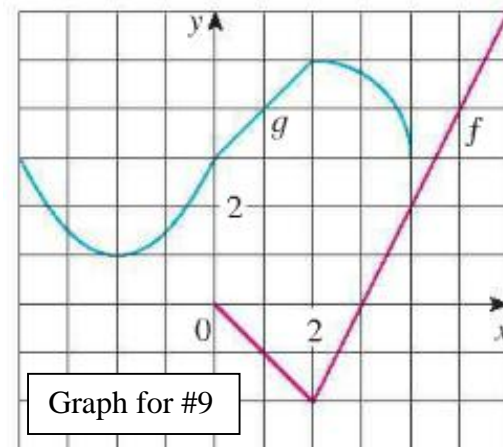
9. Use the given graph of f and g to evaluate the following, if possible. If not possible, state why.

- (a) $f(g(2))$
- (b) $g(f(0))$
- (c) $(f \circ g)(0)$
- (d) $(g \circ f)(6)$
- (e) $(g \circ g)(-2)$
- (f) $(f \circ f)(4)$

10. A spherical balloon is being inflated. Its radius is increasing at a rate of 2 cm/s.

a. Express the radius, r , as a function of time, t , where t is measured in seconds.

b. Find volume, V , as a function of time, t . This is a little different wording than the book's wording, which is why my solution looks weird.



Graph for #9