

with(*plots*) :

▼ Trigonometric Polynomial

$$g := x \mapsto \sin(x) + \cos(x) \qquad g := x \mapsto \sin(x) + \cos(x) \qquad (1.1)$$

$$gp := D(g) \qquad gp := x \mapsto \cos(x) - \sin(x) \qquad (1.2)$$

$$gpp := D(gp) \qquad gpp := x \mapsto -\sin(x) - \cos(x) \qquad (1.3)$$

$$\text{solve}(g(x) = 0) \qquad -\frac{\pi}{4} \qquad (1.4)$$

$$\text{solve}(gp(x) = 0) \qquad \frac{\pi}{4} \qquad (1.5)$$

$$\text{solve}(gpp(x) = 0) \qquad -\frac{\pi}{4} \qquad (1.6)$$

$$\text{evalf}(\text{sqrt}(2)) \qquad 1.414213562 \qquad (1.7)$$

$$\text{evalf}\left(\frac{\text{Pi}}{4}\right) \qquad 0.7853981635 \qquad (1.8)$$

$$\% \cdot 3 \qquad 2.356194490 \qquad (1.9)$$

$$\text{evalf}\left(\frac{7 \cdot \text{Pi}}{4}\right) \qquad 5.497787144 \qquad (1.10)$$

$$\text{evalf}(2 \cdot \text{Pi}) \qquad 6.283185308 \qquad (1.11)$$

$$\text{expand}\left(\left(x - \frac{(3 - \text{sqrt}(3))}{2}\right) \cdot \left(x - \frac{(3 + \text{sqrt}(3))}{2}\right)\right) \qquad x^2 - 3x + \frac{3}{2} \qquad (1.12)$$

$$\% \cdot 2 \qquad 2x^2 - 6x + 3 \qquad (1.13)$$

$$f := x \mapsto 2x^2 - 6x + 3 \qquad f := x \mapsto 2 \cdot x^2 - 6 \cdot x + 3 \qquad (1.14)$$

$$f(\sin(x))$$

$$2 \sin(x)^2 - 6 \sin(x) + 3 \quad (1.15)$$

Rational Function

$$R := x \mapsto \frac{(2 \cdot x^2 - x - 15)}{x^2 - 4 \cdot x - 21}$$

$$R := x \mapsto \frac{2 \cdot x^2 - x - 15}{x^2 - 4 \cdot x - 21} \quad (2.1)$$

$$Rp := D(R)$$

$$Rp := x \mapsto \frac{4 \cdot x - 1}{x^2 - 4 \cdot x - 21} - \frac{(2 \cdot x^2 - x - 15) \cdot (2 \cdot x - 4)}{(x^2 - 4 \cdot x - 21)^2} \quad (2.2)$$

$$\frac{4 \cdot x - 1}{x^2 - 4 \cdot x - 21} - \frac{(2 \cdot x^2 - x - 15) \cdot (2 \cdot x - 4)}{(x^2 - 4 \cdot x - 21)^2}$$

$$\frac{4 x - 1}{x^2 - 4 x - 21} - \frac{(2 x^2 - x - 15) (2 x - 4)}{(x^2 - 4 x - 21)^2} \quad (2.3)$$

$$\text{simplify}(\%)$$

$$\frac{-7 x^2 - 54 x - 39}{(x^2 - 4 x - 21)^2} \quad (2.4)$$

$$\text{factor}(\%)$$

$$- \frac{7 x^2 + 54 x + 39}{(x + 3)^2 (x - 7)^2} \quad (2.5)$$

$$\text{solve}(Rp(x) = 0)$$

$$- \frac{27}{7} - \frac{2 \sqrt{114}}{7}, - \frac{27}{7} + \frac{2 \sqrt{114}}{7} \quad (2.6)$$

$$\text{evalf}(\%)$$

$$-6.907736643, -0.806549071 \quad (2.7)$$

$$\text{evalf}\left(-\frac{27}{7}\right)$$

$$-3.857142857 \quad (2.8)$$

$$R(-6.907736643)$$

$$1.607083130 \quad (2.9)$$

$$Rpp := D(Rp)$$

$$Rpp := x \mapsto \frac{4}{x^2 - 4 \cdot x - 21} - \frac{2 \cdot (4 \cdot x - 1) \cdot (2 \cdot x - 4)}{(x^2 - 4 \cdot x - 21)^2} + \frac{2 \cdot (2 \cdot x^2 - x - 15) \cdot (2 \cdot x - 4)^2}{(x^2 - 4 \cdot x - 21)^3} \quad (2.10)$$

$$\begin{aligned}
& - \frac{2 \cdot (2 \cdot x^2 - x - 15)}{(x^2 - 4 \cdot x - 21)^2} \\
& \frac{4}{x^2 - 4 \cdot x - 21} - \frac{2 \cdot (4 \cdot x - 1) \cdot (2 \cdot x - 4)}{(x^2 - 4 \cdot x - 21)^2} + \frac{2 \cdot (2 \cdot x^2 - x - 15) \cdot (2 \cdot x - 4)^2}{(x^2 - 4 \cdot x - 21)^3} \\
& - \frac{2 \cdot (2 \cdot x^2 - x - 15)}{(x^2 - 4 \cdot x - 21)^2} \\
& \frac{4}{x^2 - 4 \cdot x - 21} - \frac{2 \cdot (4 \cdot x - 1) \cdot (2 \cdot x - 4)}{(x^2 - 4 \cdot x - 21)^2} + \frac{2 \cdot (2 \cdot x^2 - x - 15) \cdot (2 \cdot x - 4)^2}{(x^2 - 4 \cdot x - 21)^3} \\
& - \frac{2 \cdot (2 \cdot x^2 - x - 15)}{(x^2 - 4 \cdot x - 21)^2}
\end{aligned} \tag{2.11}$$

simplify(%)

$$\frac{14 \cdot x^3 + 162 \cdot x^2 + 234 \cdot x + 822}{(x^2 - 4 \cdot x - 21)^3} \tag{2.12}$$

The above is R''(x).