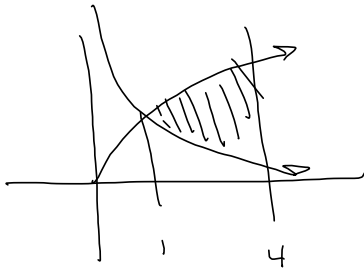
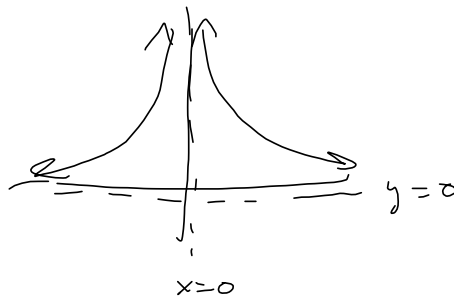
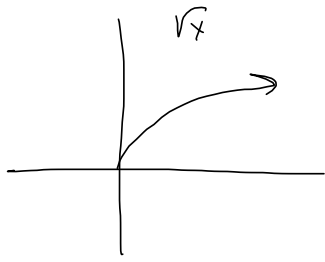


Find area bdd by  $y = \sqrt{x}$  &  $y = \frac{1}{x^2}$ , &  $x=1$  &  $x=4$



$$\sqrt{x} = \frac{1}{x^2}$$

$$x = \frac{1}{x^4}$$

$$x^4 x = 1$$

$$\boxed{x^5 - 1 = 0}$$

$$(x-1)(x^4 + x^3 + x^2 + x + 1)$$

$$x^n - 1 = (x-1)(x^{n-1} + x^{n-2} + \dots + x^1 + 1)$$

$$x^{n-(n-1)} = x^1$$

$$\frac{5}{x=1}$$

$$\sqrt[5]{x^5} = \sqrt[5]{1}$$

$$x=1$$

$$\begin{array}{r} 1 \mid 1 \quad 0 \quad 0 \quad 0 \quad 0 \quad -1 \\ \quad \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \\ \hline \quad \frac{1}{x^4} \quad \frac{1}{x^3} \quad \frac{1}{x^2} \quad \frac{1}{x} \quad \frac{1}{x} \quad 0 \\ \quad (x-1)(x^4 + x^3 + x^2 + x + 1) \end{array}$$

$$\int_{\frac{1}{4}}^4 (\text{upper} - \text{lower}) dx$$

$$= \int_1^4 \left( \sqrt{x} - \frac{1}{x^2} \right) dx = \int_1^4 \left( x^{\frac{1}{2}} - x^{-2} \right) dx$$

$$= \left[ \frac{2}{3} x^{\frac{3}{2}} + x^{-1} \right]_1^4 = \frac{2}{3} (4)^{\frac{3}{2}} + \frac{1}{4} - \left( \frac{2}{3} (1)^{\frac{3}{2}} + \frac{1}{1} \right)$$

$$\frac{2}{3}(2)^3 + \frac{1}{4} - \frac{2}{3} - 1 = \frac{16}{3} + \frac{1}{4} - \frac{2}{3} - 1 = \frac{14}{3} - \frac{3}{4} = \frac{56-9}{12} = \boxed{\frac{47}{12}}$$

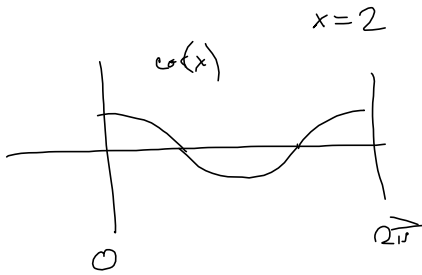
$$x^{-2} \rightarrow \frac{x^{-1}}{-1}$$

Wolfram Alpha - integrate, differentiate, graph and solve equations.

wolframalpha.com

Period of  $\cos(\pi x)$  :

want  $\pi x = 2\pi$

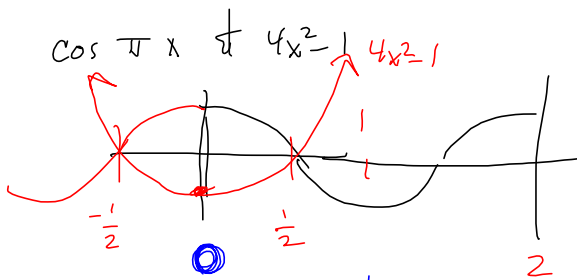
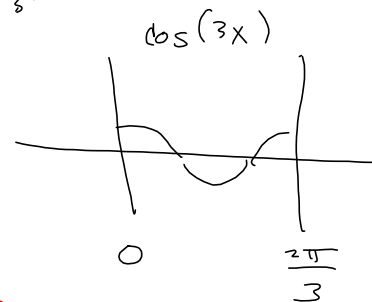
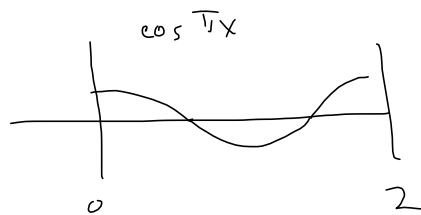


$\cos(\pi x)$

$x \mapsto \frac{1}{\pi} x$

$\cos(3x)$

$x \mapsto \frac{1}{3} x$



$4x^2 - 1 = 0$   
 $x^2 = \frac{1}{4}$   
 $x = \pm \frac{1}{2}$

$\int_{-\frac{1}{2}}^{\frac{1}{2}} (\cos(\pi x) - 4x^2 + 1) dx = 2 \int_0^{\frac{1}{2}} (\cos(\pi x) - 4x^2 + 1) dx$

FORGOT THE "2"

$= \frac{1}{\pi} \int_0^{\frac{1}{2}} \cos(\pi x) \pi dx - \int_0^{\frac{1}{2}} 4x^2 dx + \int_0^{\frac{1}{2}} 1 dx$

Symmetry.

$u = \pi x$   
 $du = \pi dx$

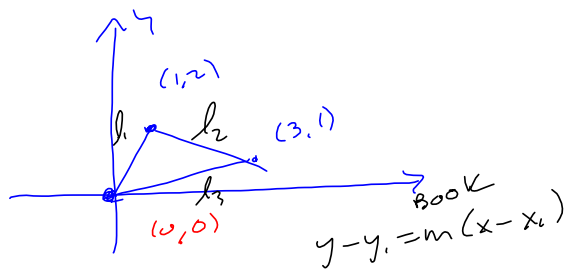
$= \frac{1}{\pi} \left[ \sin(\pi x) - \frac{4}{3} x^3 + x \right]_0^{\frac{1}{2}}$

$= \frac{1}{\pi} \left[ 1 - 0 \right] - \left[ \frac{4}{3} \left( \frac{1}{8} \right) - \frac{4}{3} (0) \right] + \left[ \frac{1}{2} - 0 \right]$

$\frac{1}{\pi} - \frac{1}{6} + \frac{1}{2} = \frac{6 - \pi + 3\pi}{6} = \frac{1}{\pi} - \frac{1}{6} + \frac{3}{6} = \frac{1}{\pi} + \frac{1}{3}$

TIMES 2:  $\boxed{\frac{2}{\pi} + \frac{2}{3}}$

$(0,0), (3,1), (1,2)$

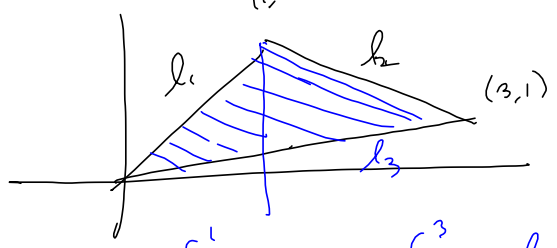


ME:  
 $y = m(x - x_1) + y_1$

$l_1: m = \frac{2-0}{1-0} = 2 \quad y = 2(x-0) + 0 = 2x = l_1(x)$

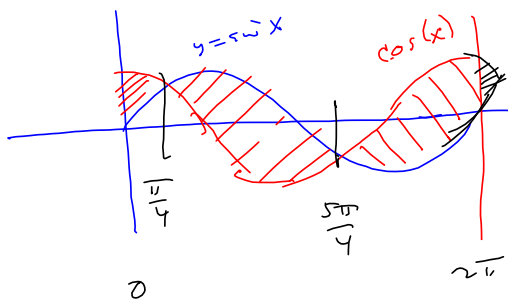
$l_2: m = \frac{1-2}{3-1} = -\frac{1}{2} = m \quad y = -\frac{1}{2}(x-1) + 2 = l_2(x)$   
 $= -\frac{1}{2}x + \frac{1}{2} + 2 = -\frac{1}{2}x + \frac{5}{2} = l_2(x)$

$l_3: m = \frac{1-0}{3-0} = \frac{1}{3} \quad y = \frac{1}{3}(x-0) + 0 = \frac{1}{3}x = l_3(x)$



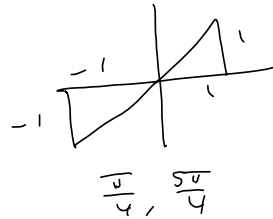
$\int_0^1 l_1 - l_3 + \int_1^3 l_2 - l_3 = \int_0^1 (2x - \frac{1}{3}x) dx + \int_1^3 (-\frac{1}{2}x - \frac{1}{3}x) dx$

Area bdd by sine & cosine from  $x=0$  to  $x=2\pi$



$$\sin x = \cos x$$

$$\frac{\sin x}{\cos x} = \tan x = 1$$



$$\int_0^{\pi/4} (\cos x - \sin x) dx + \int_{\pi/4}^{\pi/2} (\sin x - \cos x) dx$$

$$+ \int_{\pi/2}^{\pi} (\cos x - \sin x) dx$$

$$+ \int_{\pi}^{5\pi/4} (\sin x - \cos x) dx$$

$$+ \int_{5\pi/4}^{2\pi} (\cos x - \sin x) dx$$

$$\rightarrow 2\pi + \frac{\pi}{4} = \frac{8\pi + \pi}{4} = \frac{9\pi}{4}$$

$$\int_{\frac{5\pi}{4}}^{\frac{9\pi}{4}} (\cos x - \sin x) dx$$

$$y = \sqrt{2x+6}$$

$$y^2 = 2x+6$$

$$y^2 - 6 = 2x$$

$$(x-1)^2 = -\left(\sqrt{2x+6}\right)^2$$

$$\frac{1}{2}y^2 - 3 = \frac{y^2 - 6}{2} = x = g_1(y)$$

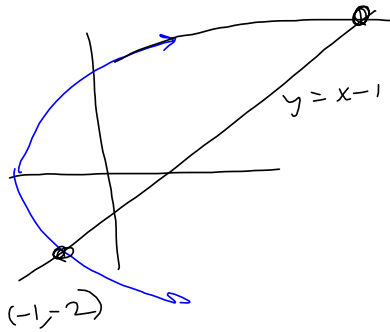
$$x = \frac{1}{2}y^2 - 3$$

$$x^2 - 2x + 1 = 2x + 6$$

$$x^2 - 4x - 5 = (x-5)(x+1)$$

$$x-1 = \sqrt{2x+6}$$

$$x=5, -1$$



$$y = x - 1 \implies x = y + 1$$

$$\int_{-2}^4 (\text{RIGHT} - \text{LEFT})$$

$$= \int_{-2}^4 \left( (y+1) - \left( \frac{1}{2}(y^2-6) \right) \right) dx$$

$$\int_{-3}^{-1} \left( \sqrt{2x+6} - (-\sqrt{2x+6}) \right) dx$$

$$+ \int_{-1}^5 \left( \sqrt{2x+6} - (x-1) \right) dx$$