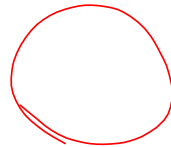


Cauchy-Schwarz.

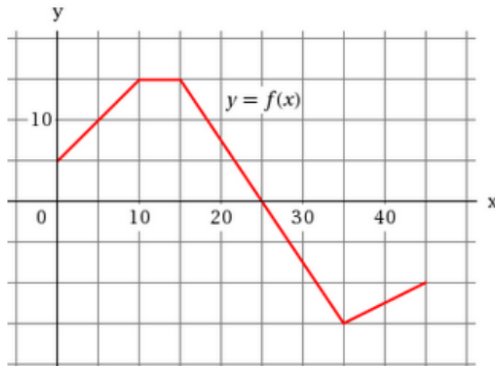
$$3 \cdot 2 + 4 \cdot 5 \leq \sqrt{3^2 + 4^2} \sqrt{2^2 + 5^2}$$

$$\sum f g \leq \sqrt{\sum f^2} \sqrt{\sum g^2}$$

$$\int f g \leq \sqrt{\int f^2} \sqrt{\int g^2}$$



The graph of f is shown. Evaluate each integral by interpreting it in terms of areas.



(a) $\int_0^{10} f(x) dx$

(b) $\int_0^{25} f(x) dx$

(c) $\int_{25}^{35} f(x) dx$

(d) $\int_0^{45} f(x) dx$

$$\int_0^{45} f(x) dx = \int_0^{10} f(x) dx + \int_{10}^{15} f(x) dx + \int_{15}^{25} f(x) dx + \int_{25}^{35} f(x) dx + \int_{35}^{45} f(x) dx$$

1 + 2 + 3 + 4 + 5

① $b_1=5, b_2=15, h=10$

Trapezoid Area =

$$\frac{1}{2}(b_1+b_2)h = \frac{1}{2}(5+15)10$$

$$= \frac{1}{2}(20)(10) = 100 = A_1$$

② Rect.

$$15 \cdot 5 = 75 = A_2$$

③ $A_3 = \frac{1}{2}bh = 10 \cdot 15 = 150 = A_3$

④ $10(-15) = -150 = A_4$

⑤ $\frac{1}{2}(-15-10)(10) = \frac{1}{2}(25)(10) = -5 \cdot 25 = -125$

$$\int_0^{45} f(x) dx = \sum_{k=1}^5 A_k = 100 + 75 + 150 - 150 - 125$$

$$= 175 - 125 = 50 = A_{net}$$

is net area.

what about $\int_0^{45} |f(x)| dx = \sum |A_k|$

$$= 100 + 75 + 150 + 150 + 125$$

$$= 175 + 300 + 125 = 475 + 125 = 600 = \int |f|$$

$$\int_0^1 (5-3x^2) dx, \text{ given } \int_0^1 x^2 dx = \frac{1}{3}$$

$$\int_0^1 (5-3x^2) dx = \int_0^1 5 dx + \int_0^1 (-3x^2) dx$$

$$= 5 \int_0^1 1 dx - 3 \int_0^1 x^2 dx$$

$$= 5 [1-0] - 3 \left[\frac{1}{3} \right] = 5 - 1 = 4 = \int_0^1 (5-3x^2) dx$$

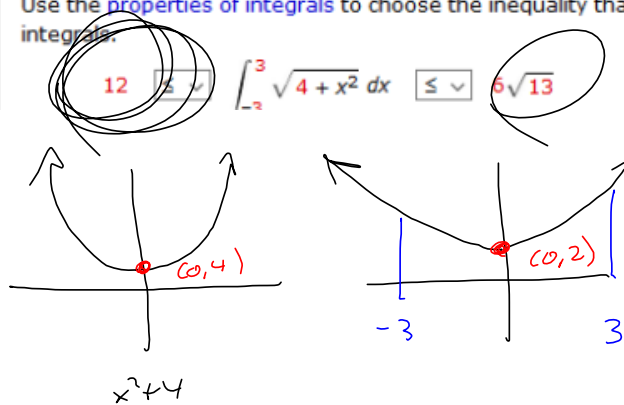
$$\sum_{k=1}^n \left(\frac{k^2}{n^2} + \frac{5k}{n} - 4 \right)$$

$$= \frac{1}{n^2} \sum k^2 + \frac{5}{n} \sum k - 4 \sum 1$$

16. Question Details

SCalc8 4.2.057. [3353944]

Use the properties of integrals to choose the inequality that would make the statement true without evaluating the integral.



$$n = 2$$

$$M = \sqrt{4+3^2} = \sqrt{13}$$

$$b-a = 3 - (-3) = 6$$

$$2 \cdot 6 \leq \int \leq 6\sqrt{13}$$

$$1 \leq \sqrt{1+x^3} \leq 1+x^3$$

\sqrt{x} is an increasing function of x

$x \geq 0$, then

$$x^3 \geq 0$$

$$1 = \sqrt{1} \leq \sqrt{1+x^3}$$

$$\forall x \geq 1, \sqrt{x} \geq \sqrt{1}$$

$$1+x^3$$

$$\sqrt{\odot} \leq \odot : f$$

$\odot \geq 1$ if this is the case,

since $1+x^3 \geq 1$

If $f \geq g$ on $[a, b]$

$$\text{Then } \int_a^b f dx \geq \int_a^b g dx$$

So

$$1 \leq \sqrt{1+x^3} \leq 1+x^3 \Rightarrow$$

$$\int_0^1 dx = \int_0^1 x^0 dx \leq \int_0^1 \sqrt{1+x^3} dx \leq \int_0^1 (1+x^3) dx$$

$$= \left[\frac{x^1}{1} \right]_0^1 \leq \int_0^1 \sqrt{1+x^3} dx \leq \left[x + \frac{x^4}{4} \right]_0^1$$

$$1 - 0 \leq \int_0^1 \sqrt{1+x^3} dx \leq 1 + \frac{1}{4} - \left(0 + \frac{0}{4} \right)$$

$$1 \leq \int_0^1 \sqrt{x^3+1} dx \leq \frac{5}{4} = 1.25 < 1.41$$

Note This estimate is better than

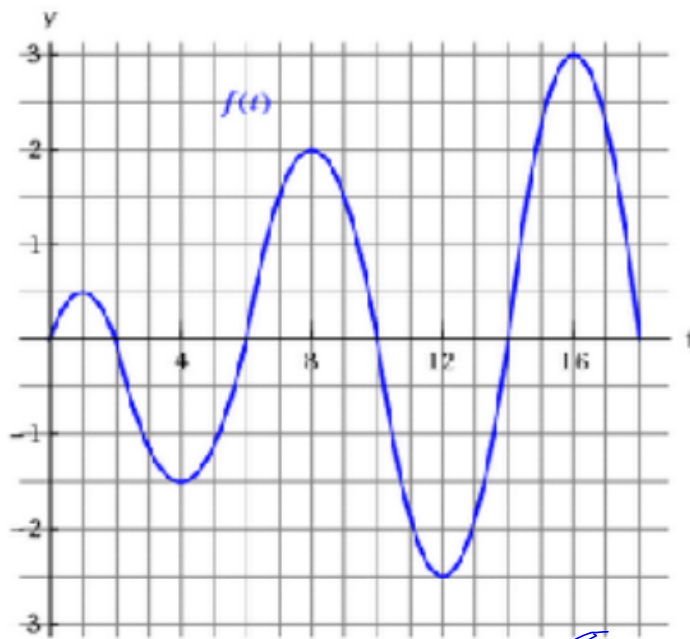
$$(\min)(b-a) \leq \int_a^b f \leq (\max)(b-a) =$$

$$\sqrt{1+1^3} = \sqrt{2} \approx 1.41 > 1.25$$

$\int e^{-x^2} dx$ has no closed-form

ant. derivative

Note 4 future



local max of $\int_0^y f(t) dt$

$x = 2, 10, 18$

mins \textcircled{a} $x = 6, 14$

