

201. §2.5 #5 1-31, 55, 70, 73

#51-6 write as $f(g(x))$

(1) $y = \sqrt[3]{1+4x}$ Let $f(u) = \sqrt[3]{u}$
 $y' = \frac{1}{3}(4x+1)^{-2/3}(4)$ $g(x) = 4x+1$

(3) $y = \tan(\pi x)$ $f(u) = \tan u$
 $y' = (\sec^2(\pi x))(\pi)$ $g(x) = \pi x$

(5) $y = \sqrt{\sin x} = (\sin x)^{1/2}$ $f(u) = \sqrt{u} = u^{1/2}$
 $y' = \left(\frac{1}{2}(\sin x)^{-1/2}\right)(\cos x)$ $g(x) = \sin x$

#5 746 Find the derivative

(7) $F(x) = (x^4 + 3x^2 - 2)^5 \rightarrow$

$$F'(x) = (5(x^4 + 3x^2 - 2)^4)(4x^3 + 6x)$$

(9) $F(x) = \sqrt{-2x+1} = (-2x+1)^{1/2} \rightarrow$

$$F'(x) = \frac{1}{2}(-2x+1)^{-1/2}(-2)$$

(11) $f(z) = \frac{1}{z^2+1} = (z^2+1)^{-1/2} \rightarrow$

$$f'(z) = -\frac{1}{2}(z^2+1)^{-3/2}(2z)$$

(13) $y = \cos(x^3 + a^3) \rightarrow$

$$y' = (-\sin(x^3 + a^3))(3x^2)$$

K

↓

(15) $y = x \sec(kx) \rightarrow y' = 1 \sec(kx) + x(\sec(kx)\tan(kx))(k)$

201 5' 2.5 #5 17-31, 58, 70, 73

$$(17) f(x) = (2x-3)^4 (x^2+x+1)^5 \Rightarrow$$

$$f'(x) = (4(2x-3)^3(2))(x^2+x+1)^5 + (2x-3)^4(5(x^2+x+1)^4(2x+1))$$

$$(19) h(x) = (t+1)^{\frac{2}{3}} (2t^2-1)^3 \Rightarrow$$

$$h'(x) = \frac{2}{3}(t+1)^{-\frac{1}{3}}(2t^2-1)^3 + (t+1)^{\frac{2}{3}}(3(2t^2-1)^2(4t))$$

$$(21) y = \left(\frac{x^2+1}{x^2-1} \right)^3 \Rightarrow$$

$$y' = 3 \left(\frac{x^2+1}{x^2-1} \right)^2 \left(\frac{2x(x^2-1) - (x^2+1)(2x)}{(x^2-1)^2} \right)$$

$$(23) y = \sin(x \cos x) \Rightarrow$$

$$y' = (\cos(x \cos x)) (\cos x - x \sin x)$$

$$(25) F(z) = \sqrt{\frac{z-1}{z+1}} = \left(\frac{z-1}{z+1} \right)^{\frac{1}{2}} \Rightarrow$$

$$F'(z) = \frac{1}{2} \left(\frac{z-1}{z+1} \right)^{-\frac{1}{2}} \left(\frac{1(z+1) - (z-1)(1)}{(z+1)^2} \right)$$

201 5' 2.5 #5 27-31, 55, 70, 73

$$(27) y = \frac{r}{\sqrt{r^2+1}} = r(r^2+1)^{-\frac{1}{2}} \rightarrow$$

$$y' = \left[(r^2+1)^{-\frac{1}{2}} + r \left(-\frac{1}{2} (r^2+1)^{-\frac{3}{2}} \right) \right] (2r)$$

$$(29) y = \sin \sqrt{x^2+1} \rightarrow$$

$$y' = \left(\cos \sqrt{x^2+1} \right) \left(\frac{1}{2} (x^2+1)^{-\frac{1}{2}} (2x) \right)$$

$$(31) y = \sin(\tan(2x)) \rightarrow$$

$$y' = \cos(\tan(2x)) (\sec^2(2x)) (2)$$

(55) (a) Find eq'n of tan line to the curve $y = \tan\left(\frac{\pi x^2}{4}\right)$ @ $(1, 1)$



$$y' = \left(\sec^2\left(\frac{\pi x^2}{4}\right) \right) \left(\frac{2\pi x}{4} \right) = \left(\sec^2\left(\frac{\pi x^2}{4}\right) \right) \left(\frac{\pi}{2} x \right)$$

$$y'(1) = \left(\sec^2\left(\frac{\pi}{4}\right) \right) \left(\frac{\pi}{2} \right) = (\sqrt{2})^2 \cdot \frac{\pi}{2} = \pi = m_{\tan}$$

$$y = \pi(x-1) + 1$$

201 $\int 2.5 \#s 70, 73$

(55) (b) Illustrate w/ graph
(See Notes)

(70) If g is twice-diff^l and $f(x) = xg(x^2)$,
find f'' in terms of g, g', g'' &

$$f'(x) = g(x^2) + xg'(x^2)(2x) = g(x^2) + 2x^2g'(x^2)$$

$$f''(x) = g'(x^2) \cdot 2x + 4xg'(x^2) + 2x^2g''(x^2)(2x)$$

$$= \boxed{2xg'(x^2) + 4xg'(x^2) + 4x^3g''(x^2)}$$

(73) Find $D^{103} \cos(2x)$ by seeing the pattern.

$$D^1 \cos(2x) = -2 \sin(2x)$$

$$D^2 \cos(2x) = -4 \cos(2x) = -2^2 \cos(2x)$$

$$D^3 \cos(2x) = +8 \sin(2x) =$$

$$D^4 \cos(2x) = +16 \cos(2x)$$

$$D^5 (\cos(2x)) = -32 \cos(2x)$$

$$103 = \frac{100}{\downarrow} + 3$$

+ (mult. of 4)

My guess is

$$\boxed{+ 2^{103} \sin(2x)}$$