

201 S'2.3 #s 51, 52, 55, 57, 59, 63, 67, 69, 73, 77, 79, 81, 89

(51) Find eq'n of tan line to the curve (a) the given point.

$$y = \frac{2x}{x+1} \quad (a) \quad (1, 1) : y' = \frac{2(x+1) - (2x)(1)}{(x+1)^2} \rightarrow$$

$$y'(1) = \frac{2(2) - 2}{2^2} = \frac{4-2}{4} = \frac{1}{2} = m$$

$$\boxed{y = \frac{1}{2}(x-1) + 1} \quad y = m(x-x_1) + y_1$$

(52) $y = x^4 + 2x^2 - x$ (a) (1, 2) \rightarrow

$$y' = 4x^3 + 4x - 1 \rightarrow$$

$$y'(1) = 4 + 4 - 1 = 7 \rightarrow$$

$$\boxed{y = 7(x-1) + 2}$$

~~(53)~~ #s 55-58 Find tan line and NORMAL LINE

(55) $y = x + \sqrt{x} = x + x^{\frac{1}{2}}$ (a) (1, 2)

$$y' = 1 + \frac{1}{2}x^{-\frac{1}{2}} \rightarrow y'(1) = 1 + \frac{1}{2} = \frac{3}{2} = m_{\text{tan}}$$

$$\rightarrow m_{\perp} = -\frac{2}{3}$$

$$\boxed{\begin{array}{l} \text{TAN LINE : } y = \frac{3}{2}(x-1) + 2 \\ \text{NORMAL LINE : } y = -\frac{2}{3}(x-1) + 2 \end{array}}$$

201 § 2.3 II #s 57, 59, 63, 67, 69, 73, 77, 79, 81, 89

(57) $y = \frac{3x+1}{x^2+1}$ (9) (1, 2) :

$$y' = \frac{3(x^2+1) - (3x+1)(2x)}{(x^2+1)^2} \Rightarrow$$

$$y'(1) = \frac{3(2) - (4)(2)}{2^2} = \frac{6-8}{4} = -\frac{2}{4} = -\frac{1}{2} = m_{\text{tan}}$$

$$\Rightarrow m_{\perp} = 2 \Rightarrow$$

TAN LINE :	$y = -\frac{1}{2}(x-1) + 2$
NORMAL LINE :	$y = 2(x-1) + 2$

559-62 Find 1st & 2nd Derivatives

(59) $P(x) = x^4 - 3x^3 + 16x \Rightarrow$

$P'(x) = 4x^3 - 9x^2 + 16$	\Rightarrow
$P''(x) = 12x^2 - 18x$	

(63) Eq'n of motion $\Rightarrow s = t^3 - 3t$, where s is in m and t is in s.

(a) Find velocity & acceleration func's

$v(t) = 3t^2 - 3$, $a(t) = 6t$

(b) $a(1) = 6$

(c) Graph.

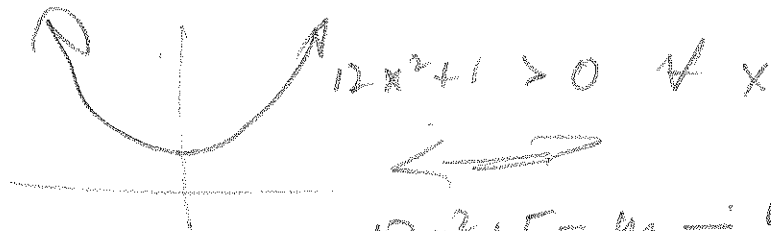
201 § 2.3 #s 72, 77, 81, 89

(72) UGH

(77) Show that $6x^3 + 5x - 3$ has no tangent line with $m = 4$.

$$f'(x) = 12x^2 + 5 \stackrel{\text{SET}}{=} 4 \Rightarrow$$

$$12x^2 + 1 = 0 \Rightarrow \text{Never!}$$



$$12x^2 + 5 = m = 4$$

has no solution.

(81) Find eqn of normal line to parabola $y = x^2 - 5x + 4$ that's \perp to $x - 3y = 5$

$$x - 3y = 5 \Rightarrow -3y = -x + 5$$

$$\Rightarrow y = \frac{1}{3}x + \frac{5}{3} \Rightarrow m = \frac{1}{3} \Rightarrow m_{\perp} = -3$$

$$y' = 2x - 5 \stackrel{\text{SET}}{=} -3$$

$$2x = 2$$

$$\boxed{x = 1}$$

$$\Rightarrow y = 1 - 5 + 4 = 0$$

$$\Rightarrow \boxed{y = -3(x - 1) + 0}$$

$$\text{OR } y = -3x + 3$$

201 § 2.3 II #s 67, 69, 73, 77, 79, 81, 89

(67) $f(5) = 1, f'(5) = 6, g(5) = -3, g'(5) = 2$
~~f(5)~~ \rightarrow

(a) $(fg)'(5) = f'(5)g(5) + f(5)g'(5)$
 $= (6)(-3) + (1)(2) = -18 + 2 = -16$

(b) $\left(\frac{f}{g}\right)'(5) = \frac{f'(5)g(5) - f(5)g'(5)}{(g(5))^2}$
 $= \frac{(6)(-3) - (1)(2)}{(-3)^2} = \frac{-18 - 2}{9} = -\frac{20}{9}$

(c) $\left(\frac{g}{f}\right)'(5) = \frac{g'(5)f(5) - g(5)f'(5)}{(f(5))^2}$

$= \frac{(2)(1) - (-3)(6)}{1^2} = 2 + 18 = 20$

(69) If $f(x) = \sqrt{x} g(x), g(4) = 8$ & $g'(4) = 7$,
find $f'(4)$

$f'(x) = \frac{1}{2}x^{-\frac{1}{2}}g(x) + x^{\frac{1}{2}}g'(x) \Rightarrow$

$f'(4) = \frac{1}{2}(4)^{-\frac{1}{2}}g(4) + 4^{\frac{1}{2}}g'(4)$

$= \frac{1}{2 \cdot 2} \cdot 8 + 2 \cdot 7 = 2 + 14 = 16$

201 #89

(89) Find a cubic func. $y = ax^3 + bx^2 + cx + d$

∴ it has horizontal tangents @ $(-2, 6)$ & $(2, 0)$

$y' = 3ax^2 + 2bx + c$ SET \ominus ~~Minimum~~

$f(2) = 0 \rightarrow f(x) = a(x-2)(x^2 + bx + c)$

$f(-2) = 6 \rightarrow f(-2) = -4a(4 - 2b + c) = 6$

~~Minimum~~ $-16a + 8ab - 4ac = 6$

Let's go horizontal tangents route.

$y' = 3a(x-2)(x+2)$ ($y' = 0$ @ $x = \pm 2$)

$= 3a(x^2 - 4)$

$= 3ax^2 - 12a = 3ax^2 + 2bx + c$

$\Rightarrow b = 0$ & $c = -12a$

$\Rightarrow y = ax^3 - 12ax + d$

$y(2) = 0 \Rightarrow 8a - 24a + d = 0$

$-16a + d = 0$

$-16a = -d$

$a = \frac{1}{16}d$

$y(-2) = 6 \Rightarrow \frac{1}{16}d(-2)^3 - 12(\frac{1}{16}d) + d = 6$

$-\frac{1}{2}d - \frac{3}{4}d + d = 6$

$-2d - 3d + 4d = 24$

$-d = 24$

$d = -24$

$a = \frac{1}{16} \cdot 24 = \frac{3}{2}$

$y = \frac{3}{2}x^3 - 6x - 24$