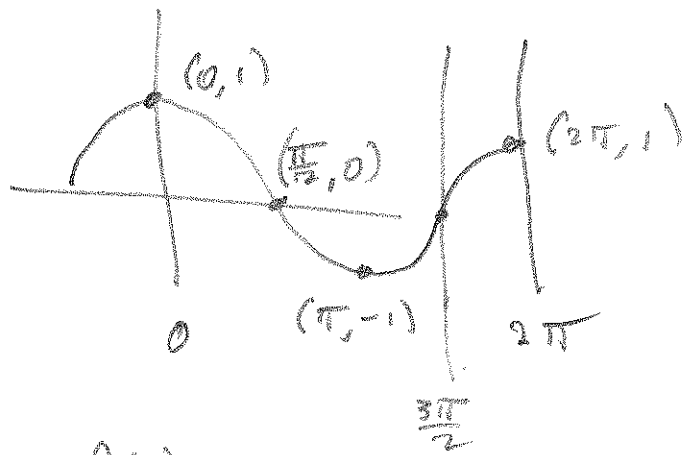


201 § 1.3 #s 17-23, 27-31, 35, 43, 51, 54

#s 9-24 Graph the func. by hand by transforming a standard func.

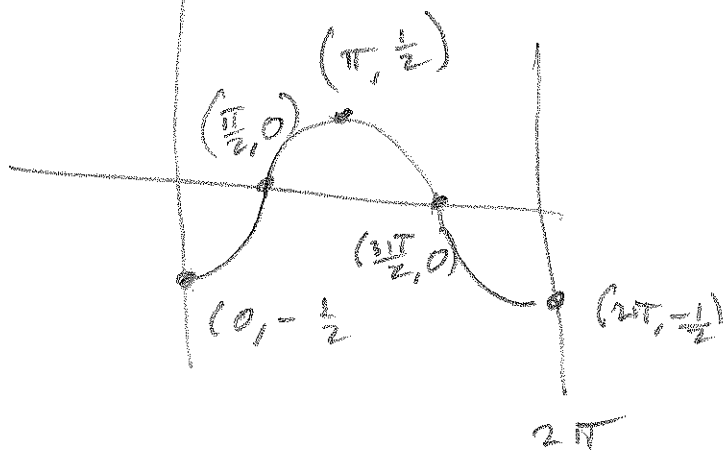
(17) $y = \frac{1}{2}(1 - \cos x) = \frac{1}{2} - \frac{1}{2} \cos x = -\frac{1}{2} \cos x + \frac{1}{2}$



$f(x) = \cos x$

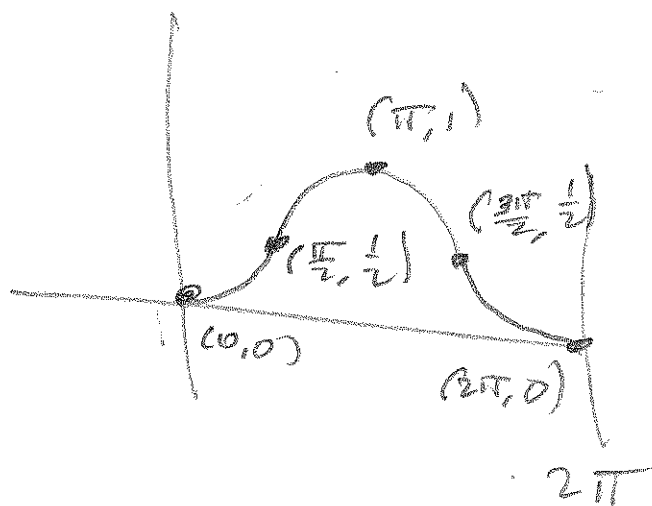
$-\frac{1}{2} f(x) = -\frac{1}{2} \cos x$

$(x, y) \mapsto (x, -\frac{1}{2}y)$



$y = -\frac{1}{2} \cos x + \frac{1}{2} = -\frac{1}{2} f(x) + \frac{1}{2}$

$(x, y) \mapsto (x, y + \frac{1}{2})$



201 $\int 1, 3 \#s$ 19-23, 27-31, 35, 43, 51, 54

19 $y = 1 - 2x - x^2$

$f(x) = -x^2 - 2x + 1$

$-f(x) = x^2 + 2x - 1$

$-f(x) + 1 = x^2 + 2x$

$-f(x) + 1 + 1^2 = x^2 + 2x + 1^2$

$-f(x) + 2 = (x+1)^2$

$-f(x) = (x+1)^2 - 2$

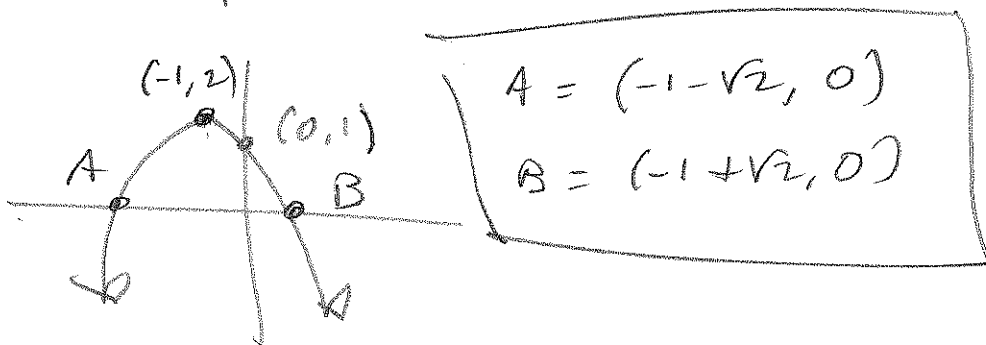
$f(x) = -(x+1)^2 + 2$

$x^2 \rightarrow -x^2 \rightarrow -(x+1)^2 \rightarrow -(x+1)^2 + 2$

flip vertically
h + 1
up 2

$(h, k) = (-1, 2)$

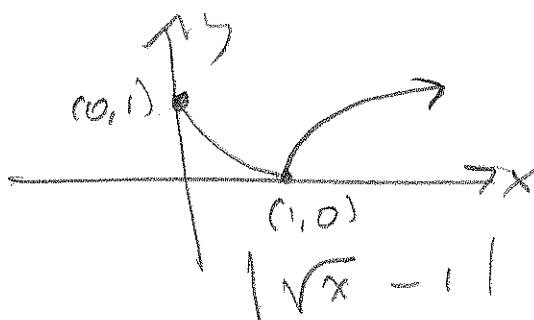
opens down



28 $y = |\sqrt{x} - 1|$

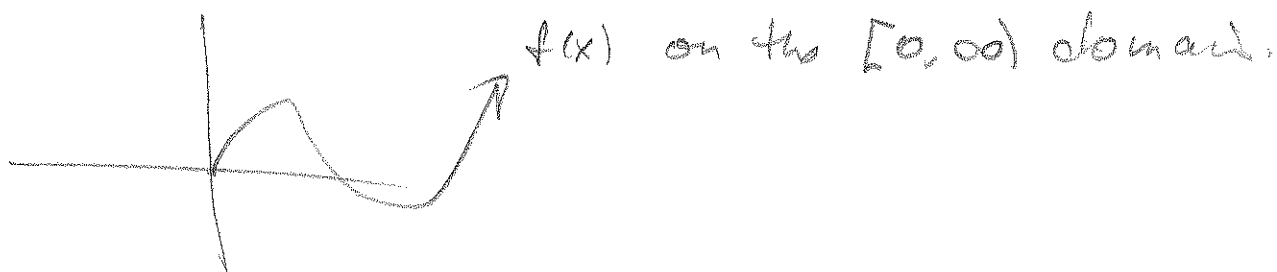
I'd attack it by doing

$\sqrt{x} \rightarrow \sqrt{x} - 1 \rightarrow |\sqrt{x} - 1|$

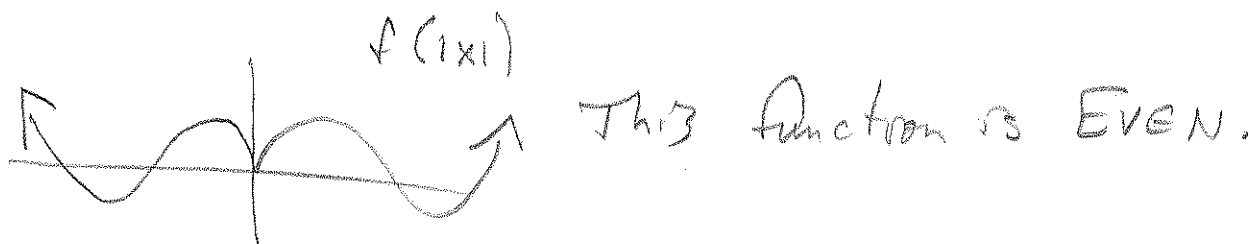


201 Q 1/3 #s 27-31

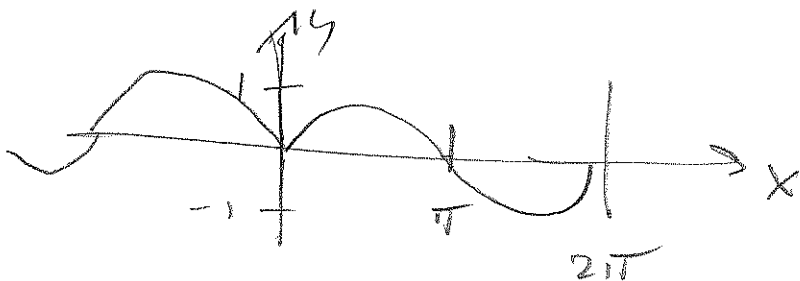
(27) The graph of $f(|x|)$ is obtained by reflecting the graph of $f(x)$ for $x \geq 0$ thru the y -axis.



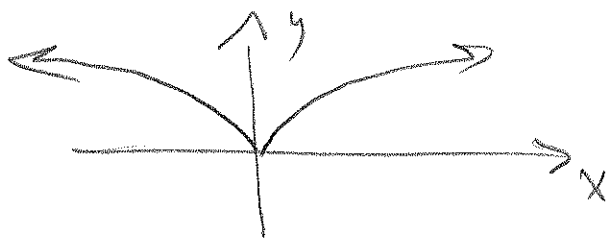
New function =



(b) $f(x) = \sin x \rightarrow f(|x|) = \sin(|x|)$



(c) $f(x) = \sqrt{|x|} \rightarrow f(|x|) = \sqrt{|x|}$



201 § 1.3 #5 29, 31, 35, 43, 51, 54

(29) $f(x) = x^3 + 2x^2$, $g(x) = 3x^2 - 1 \implies$

(a) $(f+g)(x) = x^3 + 2x^2 + 3x^2 - 1$
or $x^3 + 5x^2 - 1$ $\mathcal{D} = \mathbb{R}$

(b) $(f-g)(x) = x^3 + 2x^2 - 3x^2 + 1$
 $= x^3 - x^2 + 1$ $\mathcal{D} = \mathbb{R}$

(c) $(fg)(x) = (x^3 + 2x^2)(3x^2 - 1)$
 $= 3x^5 - x^3 + 6x^4 - 2x^2$
 $= 3x^5 + 6x^4 - x^3 - 2x^2$ $\mathcal{D} = \mathbb{R}$

(d) $\left(\frac{f}{g}\right)(x) = \frac{x^3 + 2x^2}{3x^2 - 1}$

$\mathcal{D} = \{x \mid 3x^2 - 1 \neq 0\} = \{x \mid x \neq \pm \sqrt{\frac{1}{3}}\}$

$= \{x \mid x \neq \pm \frac{\sqrt{3}}{3}\} = (-\infty, -\frac{\sqrt{3}}{3}) \cup (-\frac{\sqrt{3}}{3}, \frac{\sqrt{3}}{3}) \cup (\frac{\sqrt{3}}{3}, \infty)$
Domain

201 § 1.3 #5 31, 35, 43, 51, 54

#531-36 Find (a) $f \circ g$ (b) $g \circ f$ (c) $F \circ F$ of

(a) $g \circ g$

(31) $f(x) = x^2 - 1$, $g(x) = 2x + 1$ $\mathcal{D}(f) = \mathbb{R} = \mathcal{D}(g)$

(a) $(f \circ g)(x) = f(g(x)) = (g(x))^2 - 1 = \underline{(2x+1)^2 - 1 = (f \circ g)(x)}$
 $\mathcal{D} = \mathbb{R}$

(b) $(g \circ f)(x) = 2(x^2 - 1) + 1$ $\mathcal{D} = \mathbb{R}$

(c) $(f \circ f)(x) = (x^2 - 1)^2 - 1$ $\mathcal{D} = \mathbb{R}$

(d) $(g \circ g)(x) = 2(2x+1) + 1$ $\mathcal{D} = \mathbb{R}$

(35) $f(x) = x + \frac{1}{x}$, $g(x) = \frac{x+1}{x+2}$ $\mathcal{D}(f) = \mathbb{R} \setminus \{0\}$
 $\mathcal{D}(g) = \mathbb{R} \setminus \{-2\}$

(a) $(f \circ g)(x) = \frac{x+1}{x+2} + \frac{1}{\frac{x+1}{x+2}} = \frac{x+1}{x+2} + \frac{x+2}{x+1}$

$\mathcal{D}(f \circ g) = \{x \mid x \in \mathcal{D}(g) \text{ and } g(x) \in \mathcal{D}(f)\}$

$= \{x \mid x \neq -2 \text{ AND } \frac{x+1}{x+2} \neq 0\}$ $\rightarrow g(x) \in \mathcal{D}(f)!$

$= \{x \mid x \neq -2 \text{ AND } x \neq -1\}$
 $= (-\infty, -2) \cup (-2, -1) \cup (-1, \infty)$

$\frac{x+1}{x+2} = 0$

$x+1 = 0$

$x = -1$

201 § 1.3 #5 35, 43, 51, 54

35 cont'd

$$(b) (g \circ f)(x) = \frac{x + \frac{1}{x} + 1}{x + \frac{1}{x} + 2}$$

$$\mathcal{D}(g \circ f) = \left\{ x \mid x \in \mathcal{D}(f) \text{ AND } f(x) \in \mathcal{D}(g) \right\}$$

$$= \left\{ x \mid x \neq 0 \text{ and } x + \frac{1}{x} \neq -2 \right\}$$

$$= \left\{ x \mid x \neq 0 \text{ and } x \neq 1 \right\} = (-\infty, 0) \cup (0, 1) \cup (1, \infty)$$

$$x + \frac{1}{x} = -2$$

$$\frac{x^2 + 1}{x} = \frac{-2x}{x}$$

$$x^2 + 1 = -2x$$

$$x^2 + 2x + 1 = 0$$

$$(x+1)^2 = 0$$

$$x+1 = 0$$

$$x = -1$$

$$= \frac{x^2+1}{x} + \frac{x}{x^2+1}$$
$$= \frac{(x^2+1)^2 + x^2}{x(x^2+1)} \text{ so who cares?}$$

$$(c) (f \circ f)(x) = x + \frac{1}{x} + \frac{1}{x + \frac{1}{x}} = \frac{x^2+1}{x} + \frac{1}{\frac{x^2+1}{x}}$$

$$\mathcal{D}(f \circ f) = \left\{ x \mid x \in \mathcal{D}(f) \text{ and } f(x) \in \mathcal{D}(f) \right\} !$$

$$= \left\{ x \mid x \neq 0 \text{ and } x + \frac{1}{x} \neq 0 \right\}$$

$$= \left\{ x \mid x \neq 0 \right\}$$

201 § 1.3 #5 35, 43, 51, 54

(35c) ent'd

Scratch: $x + \frac{1}{x} = 0$

$$\frac{x^2 + 1}{x} = 0$$

$x^2 + 1 = 0$ No real solim, so

$x + \frac{1}{x} \in \mathcal{D}(f)$ is no restriction

$$(c) \quad (g \circ g)(x) = \frac{\frac{x+1}{x+2} + 1}{\frac{x+1}{x+2} + 2}$$

$$\mathcal{D}(g \circ g) = \left\{ x \mid x \in \mathcal{D}(g) \text{ AND } g(x) \in \mathcal{D}(g) \right\}$$

$$= \left\{ x \mid x \neq -2 \text{ AND } g(x) \neq -2 \right\}$$

$$= \left\{ x \mid x \neq -2 \text{ AND } x \neq -\frac{5}{3} \right\}$$

$$\text{Scratch: } \frac{x+1}{x+2} = -2 \quad = (-\infty, -2) \cup (-2, -\frac{5}{3}) \cup (-\frac{5}{3}, \infty)$$

$$x+1 = -2x-4$$

$$3x = -5$$

$$x = -\frac{5}{3}$$

201 8'1,3 #543,51,54

#541-46 Express as a composition $f \circ g$

$$(43) \quad F(x) = \frac{\sqrt[3]{x}}{\sqrt[3]{x} + 1}$$

Let $g(x) = \sqrt[3]{x}$ and $f(x) = \frac{x}{x+1}$. Then

$$F(x) = (f \circ g)(x)$$

(51) Pair in the next picture goes here:
use graph to evaluate or explain why it
can't.

$$(a) \quad f(g(2)) = f(5) = 4$$

$$(b) \quad g(f(0)) = g(0) = 3$$

$$(c) \quad (f \circ g)(0) = f(g(0)) = f(3) = 0$$

$$(d) \quad (g \circ f)(6) = g(f(6)) = g(6) \quad \text{No, b/c} \\ 6 \notin \mathcal{D}(g).$$

$$(e) \quad (g \circ g)(-2) = g(g(-2)) = g(1) = 4$$

$$(f) \quad (f \circ f)(4) = f(f(4)) = f(2) = -2$$

201 § 1.3 #54

(54) A spherical balloon is being inflated. Its radius is increasing at a (constant) rate of 2 cm/s .

(a) Express the radius r as a function of time t , in seconds: $r = 2t$

(b) Find $V = \text{Volume}$ as function of r :

I'm not quite sure what they mean.

I know $V(r) = \frac{4}{3}\pi r^3$ and I know

$r(t) = 2t$, so that volume as function of time is $V(r(t)) = \frac{4}{3}\pi (2t)^3 = \frac{32}{3}\pi t^3$.

This is unusual model. Usually volume changes at a constant rate and radius grows more slowly as volume increases.