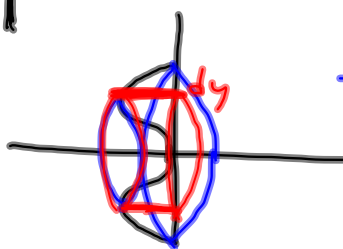
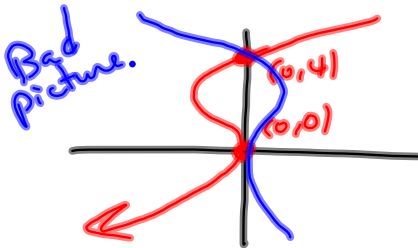


§ 5.3 #12

$x = 4y^2 - y^3$ ,  $x=0$  about  $x$ -axis  
 $= y^2(4-y)$

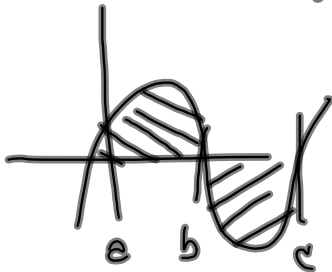
$-x^3$



thickness =  $dy$   
 height =  $0 - (4y^2 - y^3)$   
 $= y^3 - 4y^2$   
 radius =  $y$

$$\text{Volume} = 2\pi \int_a^b y f(y) dy$$

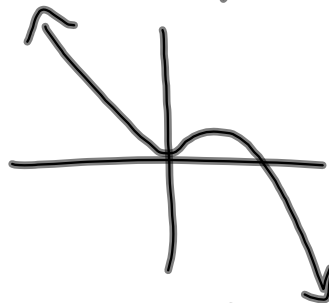
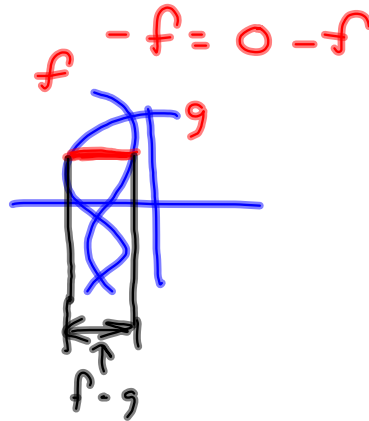
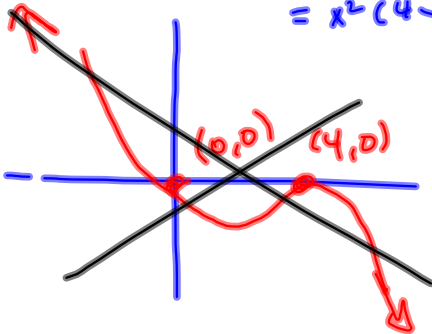
$$= 2\pi \int_0^4 y (y^3 - 4y^2) dy$$



Area from  $a$  to  $c$   
 is  $\int |f| = \int_a^b f - \int_b^c f$

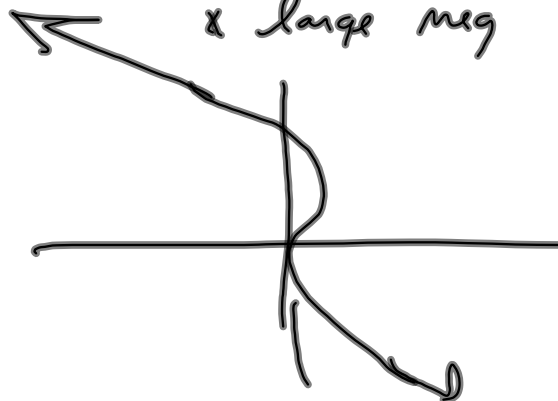
might be easier to swap vars.

$y=0$  &  $y=4x^2-x^3$   
 $=x^2(4-x)$



$x$  large pos  
 $\Rightarrow y$  large neg  
 Swap.

$y$  large pos  
 $x$  large neg



### §5.5 Mean Value Thm for Integrals

If  $f$  is cont<sup>s</sup> on  $[a, b]$ , then it achieves its average value.

Its average value is

$$f_{\text{avg}} = \frac{1}{b-a} \int_a^b f(x) dx$$

Nothing on how to FIND  $c \ni f(c) = f_{\text{avg}}$ .  
we just know that  $c$  exists!

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### §5.4 Work      WORK = FORCE $\times$ Distance

Until now, you could only do a constant force. Now the force is variable.

$$\text{work} = \int_a^b F(x) dx$$


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How much work is done when a hoist lifts a 200 kg rock 3m?

$$W = F \cdot x$$

Not force!  
Need to  
work in gravity

$$\int_0^3 200 \, dx = 200x \Big|_0^3 = 200 \cdot 3$$

$$F = (200 \text{ kg}) \left( 9.8 \frac{\text{m}}{\text{s}^2} \right) = 1960 \frac{\text{kg} \cdot \text{m}}{\text{s}^2} = 1960 \text{ N}$$

$$\int_0^3 1960 \, dx = 1960 \cdot 3$$

A leaky sandbag would be one way to make the force be variable.

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#s 11, 13, 14, 16, 17, 21, 23