

7.49 §4.3

$$\frac{d}{dx} \left[\int_0^{3x} f(u) du \right] = f(3x) \cdot 3$$

$$\frac{d}{dx} \left[\int_{2x}^0 f(u) du \right] = - \frac{d}{dx} \left[\int_0^{2x} f(u) du \right] \text{ etc.}$$

§4.5

#5 1, 2, 7, 11, 15, 21, 25, 35, 37, 41, 42, 46, (51?)

$$\begin{aligned} \textcircled{10} \int (3t+2)^{2.4} dt &= \int u^{2.4} \frac{du}{3} = \frac{1}{3} \int u^{2.4} du \\ u &= 3t+2 \\ du &= 3 dt \\ \frac{du}{3} &= dt \\ &= \frac{1}{3} \cdot \frac{u^{3.4}}{3.4} + C \\ &= \frac{u^{3.4}}{10.2} + C \end{aligned}$$

$$\textcircled{20} \int \sqrt{x} \sin(x^{3/2} + 1) dx =$$

$$\left(\begin{array}{l} u = x^{3/2} + 1 \\ du = \frac{3}{2} x^{1/2} dx = \frac{3\sqrt{x}}{2} dx \end{array} \right)$$

$$\Rightarrow dx = \frac{2}{3\sqrt{x}} du$$

$$= \int \sqrt{x} \sin(u) \frac{2 du}{3\sqrt{x}}$$

$$= \frac{2}{3} \int \sin u du$$

=

$$= \frac{2}{3} \int \frac{3\sqrt{x}}{2} \sin(x^{3/2} + 1) dx$$

$$= \frac{2}{3} \int \sin(x^{3/2} + 1) \cdot \frac{3}{2} \sqrt{x} dx$$

$$= \frac{2}{3} \int \sin u du$$

$$= \frac{2}{3} (-\cos u) + C$$

$$= -\frac{2}{3} \cos(x^{3/2} + 1) + C$$

$$24 \int \frac{dt}{\cos^2 t \sqrt{\tan t + 1}}$$

$$\left(\begin{array}{l} u = \cos^2 t \sqrt{\tan t + 1} \\ \Rightarrow du = \text{OMG} \end{array} \quad \begin{array}{l} u = \tan t + 1 \\ du = \sec^2 t dt \\ dt = \frac{du}{\sec^2 t} \end{array} \right)$$

$$= \int \frac{\frac{du}{\sec^2 t}}{\left(\frac{\cos^2 t \sqrt{u}}{1} \right)} = \int \frac{du}{\sec^2 t} \cdot \frac{1}{\cos^2 t \sqrt{u}}$$

$$= \int \frac{du}{\sqrt{u}} = \int u^{-\frac{1}{2}} du = \frac{u^{\frac{1}{2}}}{\frac{1}{2}} + C = 2\sqrt{\tan t + 1} + C$$

$$\int \frac{dt}{\cos^2 t \sqrt{\tan t + 1}} = \int (\tan t + 1)^{-\frac{1}{2}} (\sec^2 t dt)$$

$$= \int u^{-\frac{1}{2}} du, \text{ where } u = \tan t + 1, \text{ etc.}$$

$$(30) \int x^3 \sqrt{x^2+1} dx$$

$$u = x^2 + 1 \Rightarrow du = 2x dx$$

$$dx = \frac{du}{2x}$$

$\frac{d}{dx} [2y^2] = 4yy'$
 if we assume
 y is some sort
 of f(x). If we don't,
 then $\frac{d}{dx} [2y^2] = 0$

$$= \int x^3 u^{\frac{1}{2}} \cdot \frac{du}{2x}$$

$$\frac{1}{2} \int x^2 u^{\frac{1}{2}} du = \frac{1}{2} \int (u-1) u^{\frac{1}{2}} du$$

\int ~~u~~ $u^{\frac{1}{2}}$
 $u = x^2 + 1 \Rightarrow$
 $u - 1 = x^2$

$$= \frac{1}{2} \int (u^{\frac{3}{2}} - u^{\frac{1}{2}}) du$$

$$= \frac{1}{2} \left[\frac{u^{\frac{5}{2}}}{\frac{5}{2}} - \frac{u^{\frac{3}{2}}}{\frac{3}{2}} \right] + C = \frac{1}{2} \left[\frac{2}{5} u^{\frac{5}{2}} - \frac{2}{3} u^{\frac{3}{2}} \right] + C$$

$$= \frac{1}{5} (x^2+1)^{\frac{5}{2}} - \frac{1}{3} (x^2+1)^{\frac{3}{2}} + C$$

Compare & Contrast

$$\int_{60}^{100} v(t) dt \quad \text{-vs-} \quad \int_{60}^{100} |v(t)| dt$$

Displacement
(Net Change)

Total
Distance

Assuming $v(t)$ represents Velocity.

True/FALSE $\frac{d}{dx} \int_a^b f(x) dx = f(x)$ FALSE

$$\int_0^1 x dx = \left[\frac{x^2}{2} \right]_0^1 = \frac{1^2}{2} - \frac{0^2}{2} = \frac{1}{2}$$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$

$$\frac{d}{dx} \left[\int_0^1 x dx \right] = \frac{d}{dx} \left[\frac{1}{2} \right] = 0$$

§ 4.5 # 51

$$\int_0^1 \frac{dx}{(1+\sqrt{x})^4} = \int_1^2 \frac{2x^{\frac{1}{2}} dy}{u^4}$$

$$u = x^{\frac{1}{2}} + 1 \quad \rightarrow \quad (u-1) = x^{\frac{1}{2}}$$

$$du = \frac{1}{2} x^{-\frac{1}{2}} dx = dy$$

$$dx = 2x^{\frac{1}{2}} du$$

u	x=0	x=1
	u=1	u=2