

1. **Question Details** LarTrig9 1.8.0

Fill in the blank.

A(n)  measures the acute angle a path or line of sight makes with a fixed north-south line.

Bearing.



2. **Question Details** LarTrig9 1.8.002. [2596932]

Fill in the blank.

A point that moves on a coordinate line is said to be in simple  when its distance  $d$  from the origin at time  $t$  is given by either  $d = a \sin \omega t$  or  $d = a \cos \omega t$ .

harmonic motion

3. **Question Details**

Fill in the blank.

The time for one complete cycle of a point in simple harmonic motion is its .

$\frac{\text{time}}{1 \text{ cycle}}$

$T$

Period

4. **Question Details**

Fill in the blank.

The number of cycles per second of a point in simple harmonic motion is its .

$\frac{\text{cycles}}{1 \text{ sec}}$

$f$

frequency

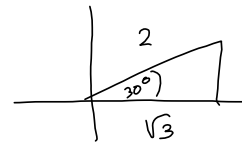
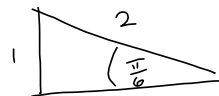
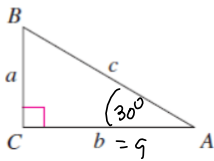
$$f = \frac{1}{T}$$

5. Question Details

LarTrig9 1.8.005 [24632]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places.

$A = 30^\circ, b = 9$



$B = 60^\circ = \frac{\pi}{3} \text{ rad}$   
 $C = 90^\circ = \frac{\pi}{2} \text{ rad}$   
 $c = \frac{18}{\sqrt{3}}$   
 $a = \frac{9}{\sqrt{3}}$

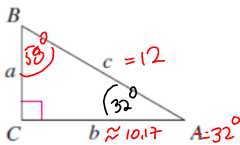
$\cos(30^\circ) = \frac{9}{c}$   
 $\Rightarrow c \cos(30^\circ) = 9$   
 $\Rightarrow c = \frac{9}{\cos(30^\circ)} = \frac{9}{(\frac{\sqrt{3}}{2})} = \frac{18}{\sqrt{3}}$

$\frac{a}{9} = \tan(30^\circ) \Rightarrow$   
 $a = 9 \tan(30^\circ) = 9 \left(\frac{1}{\sqrt{3}}\right) = \frac{9\sqrt{3}}{3} = 3\sqrt{3}$

6. Question Details

Solve the right triangle shown in the figure. Round your answers to two decimal places.

$B = 58^\circ, c = 12$



$C = 90^\circ$

$A = 90^\circ - 58^\circ = 32^\circ = A$

$\cos(A) = \cos(32^\circ) = \frac{b}{12}$   
 $12 \cos(32^\circ) = b \approx 10.17$

$\sin(A) = \frac{a}{12}$   
 $12 \sin(A) = a \approx$   
 $12 \sin(32^\circ) = a \approx 6.36$

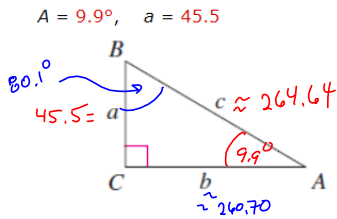
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10.17657715
12cos(32)
10.17657715
12sin(32)
6.359031171
12cos(58)
6.359031171
    
```

7. Question Details

LarTrig9 1.8.008. [32208]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places.



$A = 9.9^\circ, a = 45.5$

M1  
 $\sin(9.9^\circ) = \frac{45.5}{c}$   
 $c \sin(9.9^\circ) = 45.5$

M2:  
 $\frac{c}{45.5} = \csc(9.9^\circ)$   
 $c = 45.5 \csc(9.9^\circ)$

$c = \frac{45.5}{\sin(9.9^\circ)} = 45.5 \csc(9.9^\circ) \approx 264.64 \approx c$

calculator has no csc(x) button!

$\frac{45.5}{b} = \tan(9.9^\circ)$   
 $45.5 = b \tan(9.9^\circ)$

$45.5 \cot(9.9^\circ) = \frac{45.5}{\tan(9.9^\circ)} = b \approx 260.70$

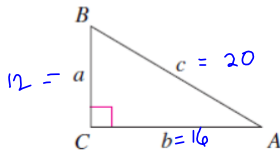
$B = 90^\circ - 9.9^\circ = 80.1^\circ = B$

8. Question Details

LarTrig9 1.8.009. [24632]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places.

$a = 12, b = 16$



$12^2 + 16^2 = 144 + 256 = 400 = 20^2$

Use inverse trig to get two angles.

$\frac{a}{c} = \sin A = \frac{12}{20} = \frac{3}{5} \Rightarrow$

$\arcsin(\sin(A)) = A = \arcsin(\frac{3}{5}) \approx 36.87^\circ \approx A$

True if  $-\frac{\pi}{2} \leq A \leq \frac{\pi}{2}$   
 A is acute so, yeah.

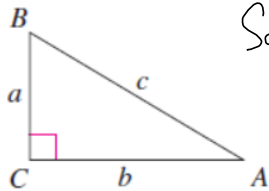
$B = 90^\circ - A \approx 90^\circ - 36.87^\circ = 53.13^\circ \approx B$

9. [Question Details](#)

LarTrig9 1.8.010. [2550]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places.

$$a = 40, \quad c = 46$$



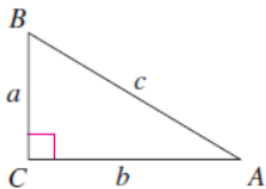
Same as #9 method

10. [Question Details](#)

LarTrig9 1.8.011. [2463]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places.

$$b = 16, \quad c = 69$$



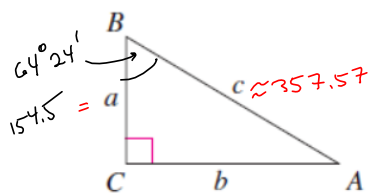
Same, only different sides given

11. Question Details

LarTrig9 1.8.014. [255]

Solve the right triangle shown in the figure for all unknown sides and angles. Round your answers to two decimal places

$B = 64^\circ 24'$ ,  $a = 154.5$



$$64^\circ 24' = 64^\circ + 24'$$

$$= 64^\circ + (24') \left( \frac{1^\circ}{60'} \right)$$

$$\frac{154.5}{c} = \cos(64^\circ 24')$$

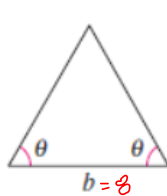
$$\frac{154.5}{\cos(64^\circ 24')} = c \approx 357.57$$

12. Question Details

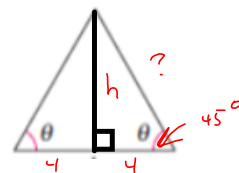
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Find the altitude of the isosceles triangle shown in the figure. Round your answer to two decimal places.

$\theta = 45^\circ$ ,  $b = 8$




Drop a perpendicular



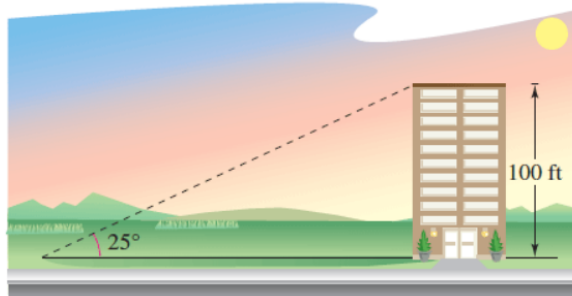
$$\frac{h}{4} = \tan \theta$$

$$h = 4 \tan 45^\circ = 4 = h$$

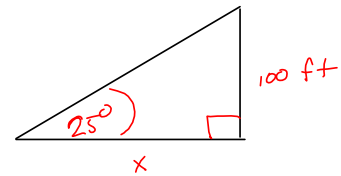
13.  Question Details

LarTrig9 1.8.019. [2596908]

The sun is  $25^\circ$  above the horizon. Find the length of a shadow cast by a building that is 100 feet tall (see figure). (Round your answer to two decimal places.)

 ft


Let  $x$  = the length of the shadow (ft).



$$\tan 25^\circ = \frac{100}{x} \Rightarrow$$

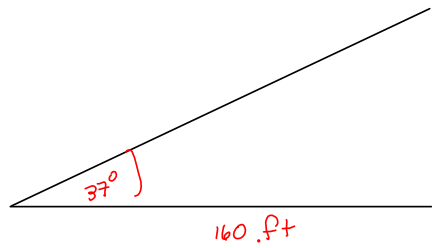
$$x = \frac{100}{\tan(25^\circ)} \approx$$

Draw Your Own Picture!

14.  Question Details

LarTrig9 1.8.022. [2456857]

The length of a shadow of a tree is 160 feet when the angle of elevation of the sun is  $37^\circ$ . Approximate the height of the tree.  
(Round your answer to one decimal place.)

 ft

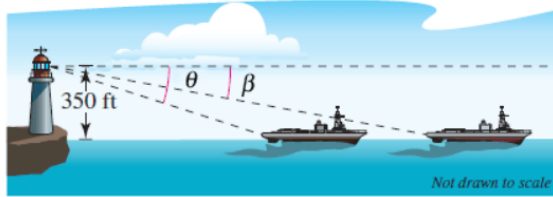
Let  $x$  = height of tree (ft)

15. Question Details

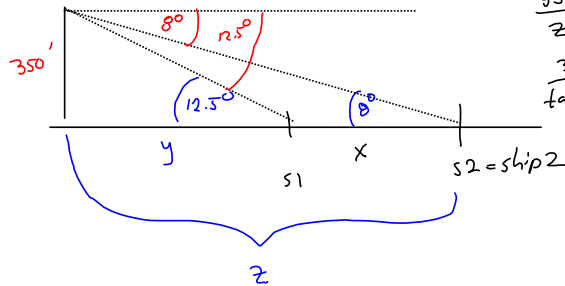
LarTrig9 1.8.024. [245666]

An observer in a lighthouse 350 feet above sea level observes two ships directly offshore. The angles of depression to the ships are  $\beta = 8^\circ$  and  $\theta = 12.5^\circ$  (see figure). How far apart are the ships? (Round your answer to one decimal place.)

ft



$x$  = distance between ships (ft)  
 $z$  = dist. to ship 2 (ft)  
 $y$  = " " ship 1 (ft)



$$\frac{350}{z} = \tan 8^\circ$$

$$\frac{350}{\tan 8^\circ} = z \approx 2490.4$$

$$\frac{350}{y} = \tan(12.5^\circ)$$

$$\frac{350}{\tan(12.5^\circ)} = y \approx 1578.7$$

$$x = z - y \approx 2490.4 - 1578.7, \text{ etc.}$$

ion Details

LarTrig9 1.8.026. [2456209]

serve a plane approaching overhead and assume that its speed is 650 miles per hour. The angle of elevation of the s  $15^\circ$  at one time and  $58^\circ$  one minute later. Approximate the altitude of the plane. (Round your answer to two decimal

)  mi



17.  Question Details LarTrig9 1.8.034. [245604]

During takeoff, an airplane's angle of ascent is  $17^\circ$  and its speed is 300 feet per second.

(a) Find the plane's altitude after 1 minute. (Round your answer to the nearest whole number.)

ft

(b) How long will it take the plane to climb to an altitude of 10,000 feet? (Round your answer to one decimal place)

sec

18.  Question Details LarTrig9 1.8.036. [2456170]

A jet leaves Reno, Nevada and is headed toward Miami, Florida at a bearing of  $100^\circ$ . The distance between the two cities is approximately 2472 miles.

(a) How far north and how far west is Reno relative to Miami? (Round your answers to two decimal places.)

miles north

miles west

(b) If the jet is to return directly to Reno from Miami, at what bearing should it travel?

$^\circ$

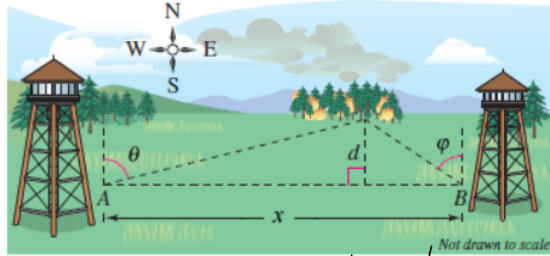
19. Question Details

LarTrig9 1.8.042.MI. [2463203]

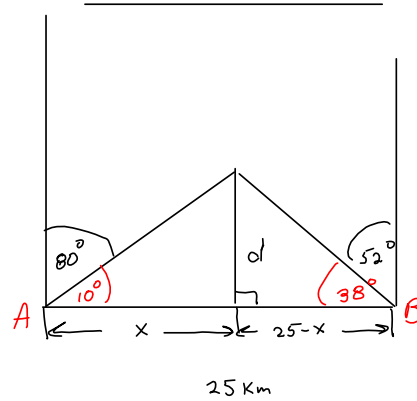
Fire tower A is  $x = 25$  kilometers due west of fire tower B. A fire is spotted from the towers, and the bearings from A and B are  $\theta = N 80^\circ E$  and  $\phi = N 52^\circ W$ , respectively (see figure). Find the distance  $d$  of the fire from the line segment AB. (Round your answer to two decimal places.)

$d = \text{[ ] km}$

$d = \text{distance to fire from } \overline{AB} \text{ (km)}$



Hey!  $d = d!$



$$\frac{d}{25-x} = \tan 38^\circ \Rightarrow d = (25-x) \tan 38^\circ$$

$$\frac{d}{x} = \tan 10^\circ \Rightarrow d = x \tan 10^\circ$$

$$(25-x) \tan(38^\circ) = x \tan(10^\circ)$$

Linear, in  $x$ .

$$(25-x)a = x \cdot b$$

$$25a - 2x = bx$$

$$-2x - bx = -25a$$

$$x(-2-b) = -25a$$

$$x = \frac{-25a}{-2-b} = \frac{25a}{2+b}$$

$$\frac{25 \tan(38^\circ)}{\tan(38^\circ) + \tan(10^\circ)} \approx 20.39670376$$

Use un-rounded to find  $d$ :

$$d = x \tan(10^\circ) \approx 20.39670376 \tan(10^\circ) \approx 3.59648919$$

```
350/tan(12.5)
1578.747976
25tan(38)/(tan(38)+tan(10))
20.39670376
Ans*tan(10)
3.59648919
```

$\approx 3.6 \text{ km} \approx d$

20. Question Details

Find a model for simple harmonic motion satisfying the specified conditions.

Displacement  
( $t = 0$ )  
**0**

Amplitude

**1.9 meters**      **4 seconds**

$$T = 4$$

$$bx = 2\pi \text{ when } x = 4 \Rightarrow$$

$$b = \frac{2\pi}{4} = \frac{\pi}{2} \text{ will have period } T = 4$$

$$f(x) = 1.9 \sin\left(\frac{\pi}{2}x\right)$$

$$\frac{\pi}{2}x = 2\pi \text{ when}$$

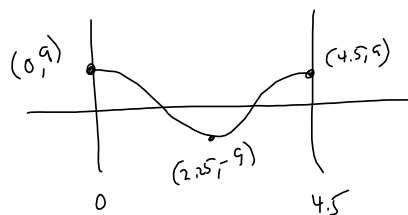
$$x = \frac{2\pi}{(\frac{\pi}{2})} = (2\pi)\left(\frac{2}{\pi}\right) = 4 \checkmark$$

$\sin(x)$  starts @  $y=0$ . Use sine.

21. + Question Details

Find a model for simple harmonic motion satisfying the specified conditions.

Displacement, $d$ ( $t = 0$ )	Amplitude, $a$	Period
9 inches	9 inches	4.5 seconds



$$T = 4.5$$

$$bx = 2\pi \text{ when } x = 4.5$$

$$4.5b = 2\pi$$

$$b = \frac{2\pi}{4.5} = \frac{4\pi}{9}$$

$$\frac{4\pi}{9}x = 2\pi$$

$$x = \frac{18\pi}{4\pi} = 4.5 \checkmark$$

$$9 \cos\left(\frac{4\pi}{9}x\right)$$

22. + Question Details

LarTrig9 1.8.051. [2550721]

A point on the end of a tuning fork moves in simple harmonic motion described by  $d = a \sin \omega t$ . Find  $\omega$  given that the tuning fork for a certain note has a frequency of 272 vibrations per second.

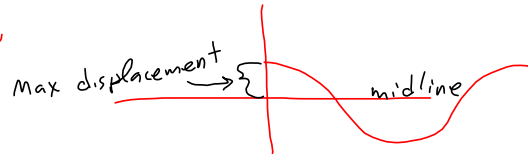
$$\omega = \boxed{\phantom{000000}}$$

23. Question Details LarTrig9 1.8.054. [2456678]

For the simple harmonic motion described by the trigonometric function, find the maximum displacement, the frequency, the value of  $d$  when  $t = 6$  and the least positive value of  $t$  for which  $d = 0$ . Use a graphing utility to verify your results.

$$d = \frac{1}{4} \cos(16\pi t)$$

(a) Find the maximum displacement, *from the midline*  
  $a = \text{amplitude} = \frac{1}{4}$ .

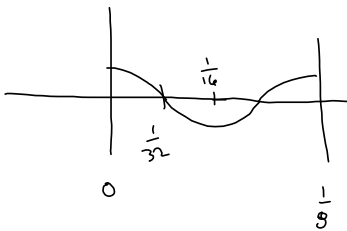


(b) Find the frequency.  
 cycles per unit of time

$T = ?$   
 $16\pi t = 2\pi$  when?  
 $t = \frac{2\pi}{16\pi} = \frac{1}{8} = T = \text{time for one cycle} = \frac{\text{time}}{\text{cycle}}$   
 $\Rightarrow f = \frac{1}{T} = 8 \text{ cycles/unit time} = \frac{\text{cycles}}{\text{Time}}$

(c) Find the value of  $d$  when  $t = 6$ .  
 $d = \frac{1}{4}$

(d) Find the least positive value of  $t$  for which  $d = 0$ .  
 $t = \frac{1}{32}$



(c)  $d(6) = \frac{1}{4} \cos(16\pi(6))$   
 $= \frac{1}{4} \cos(96\pi) = \frac{1}{4}$

