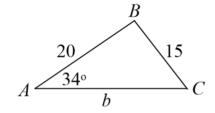
I think you know the drill on margins and legibility. I can't give points for what I can't read. Take a minute, at the end, to make sure your work is organized and submitted in proper order.

- 1. Let  $f(x) = 3x^3 8x^2 + 19x 10$ 
  - a. (10 pts) Use synthetic division to find f(3).
  - b. (10 pts) Use synthetic division to show that x=1+2i is a solution of the equation f(x)=0.
  - c. (10 pts) Split f into linear factors, that is, factor f all the way.
- **2.** Let  $z = 3\sqrt{6} 3\sqrt{6}i$ 
  - a. (10 pts) Find  $z + \overline{z}$  and  $z\overline{z}$ , where  $\overline{z}$  is the complex conjugate of z.
  - b. (10 pts) Express z in trigonometric form.
- 3. Let  $z = 16 \left( \cos \left( \frac{5\pi}{4} \right) + i \sin \left( \frac{5\pi}{4} \right) \right)$ 
  - a. (10 pts) Express z in standard form.
  - b. (10 pts) Find the principal 4<sup>th</sup> root of z, i.e., find  $\sqrt[4]{z}$ . Leave z in trigonometric form for this.
  - c. (10 pts) Now, find the *other*  $4^{th}$  roots of z, in trigonometric form.
  - d. (10 pts) Find the trigonometric form of  $z^4$ .
- **4.** (10 pts) Find all solutions  $\theta \in [0, 2\pi)$  of the trig equation  $4\sin^3(2\theta) + 12\sin^2(2\theta) 3\sin(2\theta) 9 = 0$ . (Hint: If  $f(x) = 4x^3 + 12x^2 3x 9$ , then f(-3) = 0.)

Work up to 15 points' worth of bonus.

**Bonus 1.** Consider the triangle on the right.

- a. (5 pts) Prove that there are two possible solutions to this triangle.
- b. (5 pts) Use the Law of Sines to find the measure of angle *C* for the case where *B* is *acute*. (The case where *B* is obtuse is shown.) Give final answer accurate to 6 decimal places.



- c. (5 pts) Use the Law of Cosines and your answer from part b to find the length of side b. Give final answer accurate to 6 decimal places.
- **Bonus 2.** The vector  $\overline{u}$  has a magnitude of  $\|\overline{u}\| = 60$  Newtons (N) and a direction angle  $\theta = 45^{\circ}$ . The vector  $\overline{v}$  has a magnitude of  $\|\overline{v}\| = 50$  and a direction angle of  $\phi = 120^{\circ}$ .

- a. (5 pts) Draw a diagram that describes this situation.
- b. (5 pts) Express  $\overline{u}$  and  $\overline{v}$  in component form, in two ways: Give an exact answer, and an answer rounded to 3 decimal places.
- c. (5 pts) Find the resultant force.
- **Bonus 3.** (5 pts) Sketch the graph of  $10\sin\left(\frac{\pi}{50}x \frac{7\pi}{50}\right) 11$
- **Bonus 4.** (5 pts) Find  $\sin\left(\frac{u}{2}\right)$  and  $\cos\left(\frac{u}{2}\right)$ , given that  $\cos(u) = \frac{3}{4}$  and  $\sin(u) < 0$ . Give exact answers in simplified radical form for full credit.
- **Bonus 5.** (5 pts) What quadrant does 2u lie in if  $\cos(u) = \frac{3}{4}$  and  $\sin(u) < 0$ ?
- **Bonus 6.** (5 pts) Find the cosine function that in one of its periods achieves a maximum at (7,100) and a minumum at (43,-200)