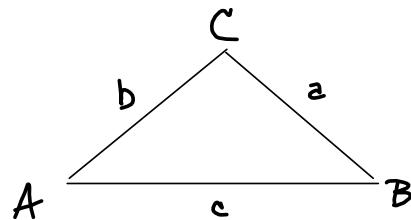


## Section 3.1 - Law of Sines



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

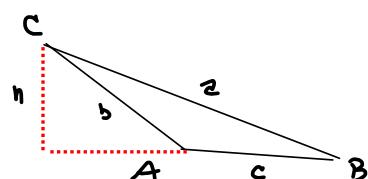
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\sin A = \frac{h}{b} \quad \& \quad \sin B = \frac{h}{a}$$

$$\Rightarrow b \sin A = h = a \sin B \Rightarrow$$

$$\frac{\sin A}{a} = \frac{\sin B}{b}, \text{ etc.}$$

$A$  is obtuse.



$$\sin A = \sin(\pi - A) = \frac{h}{b}$$

$$\sin B = \frac{h}{a}, \text{ etc.}$$

$$\begin{aligned} \sin(\pi - A) &= \sin \pi \cos(-A) + \sin(-A) \cos \pi \\ &= 0 \cdot \sim - \sin(A) \sim (-1) \\ &= \sin(A) \end{aligned}$$

## 3.1 #3

Use the Law of Sines to solve the triangle. Round your answers to two decimal places.

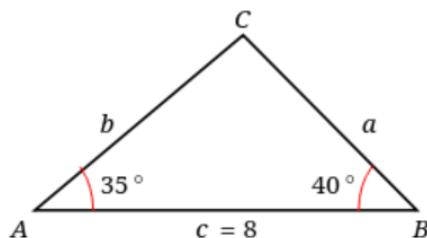
$$C = \boxed{105^\circ} \quad \boxed{105}^\circ$$

$$C = 180^\circ - B - A = 180^\circ - 35^\circ - 40^\circ = 180^\circ - 75^\circ = 105^\circ$$

$$a = \boxed{4.75} \quad \boxed{4.75}$$

$$b = \boxed{5.32} \quad \boxed{5.32}$$

$$\boxed{105^\circ = C}$$



$$\frac{a}{\sin A} = \frac{c}{\sin C} \quad \rightarrow$$

$$a = \frac{c \sin A}{\sin C}$$

$$\frac{a}{\sin 35^\circ} = \frac{8}{\sin 105^\circ} \quad \rightarrow$$

$$a = \frac{8 \sin 35^\circ}{\sin(105^\circ)} \approx \frac{4.75048017759}{\sin(105^\circ)} \approx \boxed{4.75 \approx a}$$

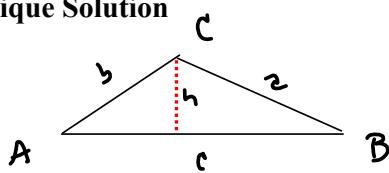
Use this in  
calculations  
(Don't Round!)

$$\frac{b}{\sin B} = \frac{c}{\sin C}$$

$$b = \frac{c \sin B}{\sin C} = \frac{8 \sin(40^\circ)}{\sin(105^\circ)} \approx 5.32370161097 \approx \boxed{5.32 \approx b}$$

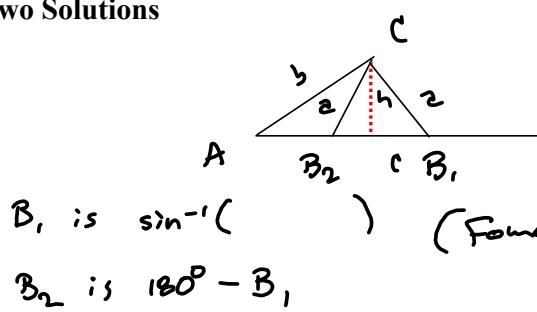
There are 3 possibilities

Unique Solution



Need  $a > h$  to have any sol'n.  
 $a > b \Rightarrow$  one solution!  
 $h < b < a$

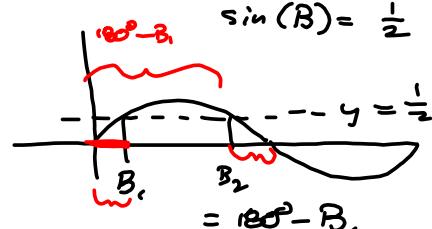
Two Solutions



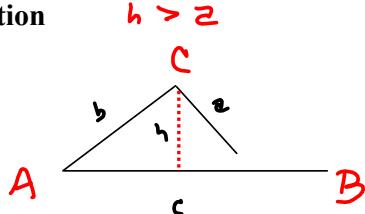
$B_1$  is  $\sin^{-1}(\frac{h}{a})$  (Found with calculator).  
 $B_2$  is  $180^\circ - B_1$

Need  $a > h$  for a solution  
 $a < b$  for 2 sol'n's

$$h < a < b$$



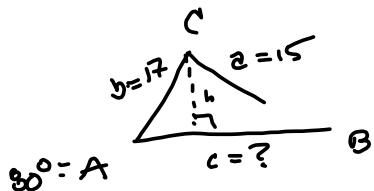
No Solution



$$h > a$$

3.1 #6

$$A = 80^\circ, a = 15, b = 17$$

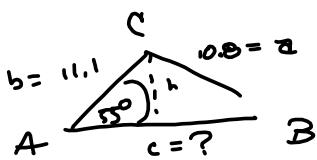


$$\begin{aligned} \frac{h}{17} &= \sin A \rightarrow h = 17 \sin A \\ &= 17 \sin(80^\circ) \approx 16.7417318012 > 15 = c \\ \rightarrow &\boxed{\text{No Sol'n !}} \end{aligned}$$

## 2 Solutions

Use the Law of Sines to solve (if possible) the triangle. If two solutions exist, find both. Round your answers to two decimal places. (If a triangle is not possible, enter IMPOSSIBLE in each corresponding answer blank.)

$$A = 55^\circ, a = 10.8, b = 11.1$$



$a < b \Rightarrow$  potential 2-sol'n switch.

$$\frac{h}{a} = \sin(55^\circ) = \frac{b}{a}$$

$$\Rightarrow h = (\sin 55^\circ)(11.1) \approx 9.09258769161 < 10.8$$

$h < a < b \Rightarrow 2 \text{ sol'n s}$

$$\frac{\sin B}{b} = \frac{\sin A}{a} \rightarrow$$

$$\sin B = \frac{b \sin A}{a} = \frac{11.1 \sin 55^\circ}{10.8} \approx 0.841906267741$$

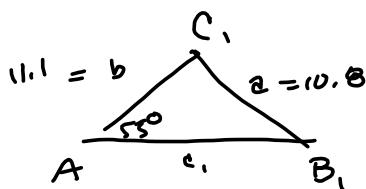
$$\Rightarrow B_1 = \arcsin(\sin B) \approx 57.3419676248^\circ \approx [57.34^\circ \text{ or } B_2]$$

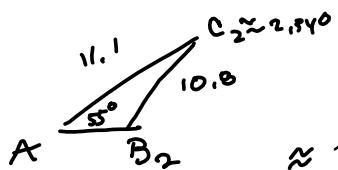
$$C_1 = 180^\circ - A - B \approx 180^\circ - 55^\circ - 57.3419676248^\circ$$

$$\approx 67.6580323752 \approx [67.66^\circ \approx C_1]$$

$$c_1 = \frac{a \sin C_1}{\sin A} = \frac{10.8 \sin(67.6580323752^\circ)}{\sin(55^\circ)} \approx 12.1946353915$$

$$\approx 12.19 \approx c_1$$



2<sup>nd</sup> Sol'n: $B$  is obtuse:

$$B_2 = 180^\circ - B, \approx 180^\circ - 57.3419676248$$

$$\approx 122.658032375^\circ \approx 122.66^\circ \approx B_2$$

$$\begin{aligned} \angle C_2 &= 180^\circ - A - B_2 \approx 180^\circ - 55^\circ - 122.658032375^\circ \\ &\approx 2.341967625^\circ \approx 2.34^\circ \approx C_2 \end{aligned}$$

$$\frac{c_2}{\sin C_2} = \frac{a}{\sin A} \Rightarrow c_2 = \frac{a \sin C_2}{\sin A} = \frac{10.8 \sin(2.341967625^\circ)}{\sin(55^\circ)}$$

$$c_2 \approx 0.538761495486$$

$$\approx 0.54 \approx c_2$$

So small, it looks like a sine!

Case 1:

$$B = \boxed{\quad} \times$$

$$\boxed{\text{key}} 57.34^\circ$$

$$C = \boxed{\quad} \times$$

$$\boxed{\text{key}} 67.66^\circ$$

$$c = \boxed{\quad} \times$$

$$\boxed{\text{key}} 12.19$$

(smaller  $B$ -value)

Case 2:

$$B = \boxed{\quad} \times$$

$$\boxed{\text{key}} 122.66^\circ$$

(large value)

$$C = \boxed{\quad} \times$$

$$\boxed{\text{key}} 2.34$$

°

$$c = \boxed{\quad} \times$$

$$\boxed{\text{key}} 0.54$$