

$$z := 32 \cdot \left(\cos\left(\frac{\text{Pi}}{3}\right) + I \cdot \sin\left(\frac{\text{Pi}}{3}\right) \right)$$

$$z := 16 + 16 I \sqrt{3} \quad (1)$$

$$z1 := 2 \cdot \left(\cos\left(\frac{\text{Pi}}{15}\right) + I \cdot \sin\left(\frac{\text{Pi}}{15}\right) \right)$$

$$z1 := 2 \cos\left(\frac{\pi}{15}\right) + 2 I \sin\left(\frac{\pi}{15}\right) \quad (2)$$

$$z1^5$$

$$\left(2 \cos\left(\frac{\pi}{15}\right) + 2 I \sin\left(\frac{\pi}{15}\right) \right)^5 \quad (3)$$

$$\text{simplify}(\%)$$

$$16 + 16 I \sqrt{3} \quad (4)$$

$$z2 := 2 \cdot \left(\cos\left(\frac{7 \cdot \text{Pi}}{15}\right) + I \cdot \sin\left(\frac{7 \cdot \text{Pi}}{15}\right) \right)$$

$$z2 := 2 \cos\left(\frac{7 \pi}{15}\right) + 2 I \sin\left(\frac{7 \pi}{15}\right) \quad (5)$$

$$z2^5$$

$$\left(2 \cos\left(\frac{7 \pi}{15}\right) + 2 I \sin\left(\frac{7 \pi}{15}\right) \right)^5 \quad (6)$$

$$\text{simplify}(\%)$$

$$16 + 16 I \sqrt{3} \quad (7)$$

$$z3 := 2 \cdot \left(\cos\left(\frac{13 \cdot \text{Pi}}{15}\right) + I \cdot \sin\left(\frac{13 \cdot \text{Pi}}{15}\right) \right)$$

$$z3 := -2 \cos\left(\frac{2 \pi}{15}\right) + 2 I \sin\left(\frac{2 \pi}{15}\right) \quad (8)$$

$$z3^5$$

$$\left(-2 \cos\left(\frac{2 \pi}{15}\right) + 2 I \sin\left(\frac{2 \pi}{15}\right) \right)^5 \quad (9)$$

$$\text{simplify}(\%)$$

$$16 + 16 I \sqrt{3} \quad (10)$$

$$z4 := 2 \cdot \left(\cos\left(\frac{19 \cdot \text{Pi}}{15}\right) + I \cdot \sin\left(\frac{19 \cdot \text{Pi}}{15}\right) \right)$$

$$z4 := -2 \cos\left(\frac{4 \pi}{15}\right) - 2 I \sin\left(\frac{4 \pi}{15}\right) \quad (11)$$

$$z4^5$$

$$\left(-2 \cos\left(\frac{4 \pi}{15}\right) - 2 I \sin\left(\frac{4 \pi}{15}\right) \right)^5 \quad (12)$$

simplify(%)

$$16 + 16 \text{I} \sqrt{3} \quad (13)$$

$$z5 := 2 \cdot \left(\cos\left(\frac{25 \cdot \text{Pi}}{15}\right) + \text{I} \cdot \sin\left(\frac{25 \cdot \text{Pi}}{15}\right) \right)$$

$$z5 := 1 - \text{I} \sqrt{3} \quad (14)$$

$$z5^5$$

$$(1 - \text{I} \sqrt{3})^5 \quad (15)$$

simplify(%)

$$-(\text{I} \sqrt{3} - 1)^5 \quad (16)$$

Notice if we go beyond the 5th one, we're back to the first one. $\frac{31 \pi}{15}$ is coterminal with $\frac{\pi}{15}$:

$$\frac{31 \text{ Pi}}{15}$$

$$\frac{31 \pi}{15} \quad (17)$$

$$z6 := 2 \cdot \left(\cos\left(\frac{31 \cdot \text{Pi}}{15}\right) + \text{I} \cdot \sin\left(\frac{31 \cdot \text{Pi}}{15}\right) \right)$$

$$z6 := 2 \cos\left(\frac{\pi}{15}\right) + 2 \text{I} \sin\left(\frac{\pi}{15}\right) \quad (18)$$

$$z6^5$$

$$\left(2 \cos\left(\frac{\pi}{15}\right) + 2 \text{I} \sin\left(\frac{\pi}{15}\right) \right)^5 \quad (19)$$

simplify(%)

$$16 + 16 \text{I} \sqrt{3} \quad (20)$$