


Trigonometry.

<https://harryzaims.com/>

 Click Me!

Notes and videos for ALL your homework.

Tests are *also* on WebAssign, and the questions come from the same bank as the homework questions.

Be honest. Common sense and common courtesy.

We're going to do 1.1 and 1.2 in sequence. I hate 1.2.

Don't memorize the dad-gum 12-point unit circle if you haven't, already.

Learn 5 triangles:

30-60-90

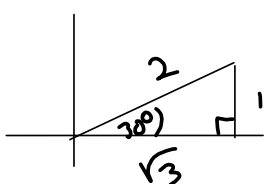
60-30-90

45-45-90

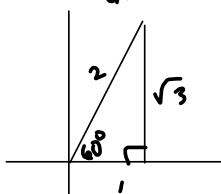
0-90-90 } Degenerate

90-0-90

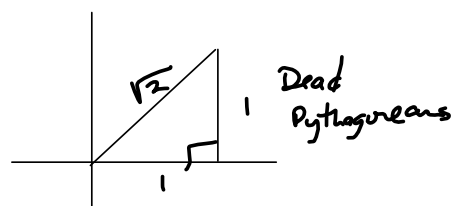
30-60



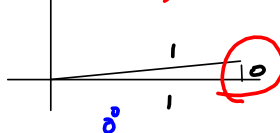
60-30



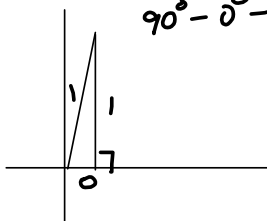
45-45



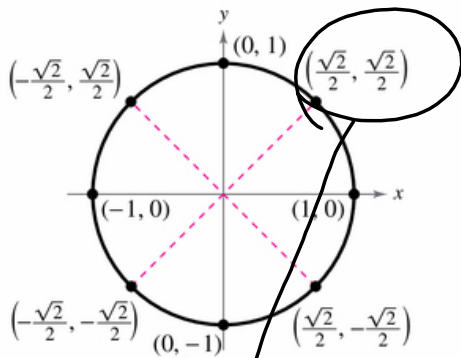
0°-90°-90°
 Degenerate cases



90°-0°-90°

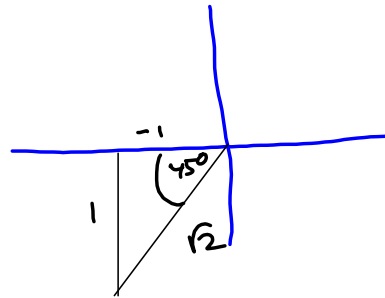


Learn these & apply to sine, cosine, & tangent in the sequel (S 1.2)

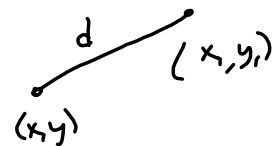


Huh?

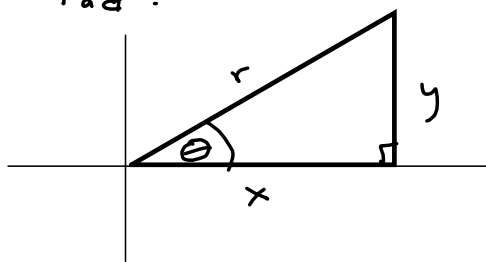
Draw me the triangle for 225°



Distance: $d = \sqrt{(x-x_1)^2 + (y-y_1)^2}$

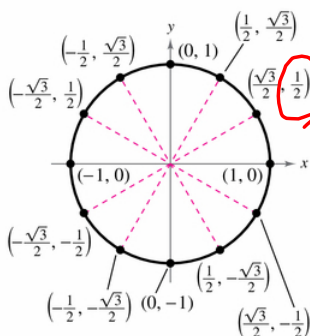


Fact:



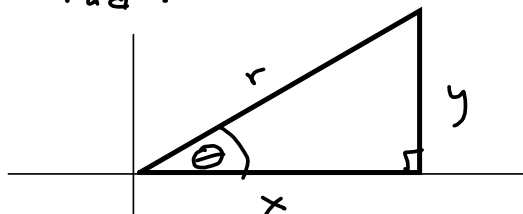
$r^2 = x^2 + y^2$

sine of theta = $\sin(\theta) = \frac{y}{r} = \frac{\text{opposite}}{\text{Hypotenuse}}$



Note:
 $\sin(30^\circ) = y$ -coordinate of the point on the unit circle corresponding to 30° .

Fact:



$$r^2 = x^2 + y^2$$

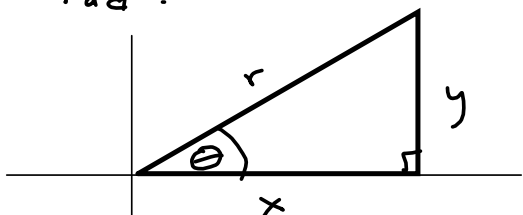
Always include the argument

$$\text{cosine of theta} = \cos(\theta)$$

$$= \frac{x}{r} = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\cos(30^\circ) = \frac{\sqrt{3}}{2}$$

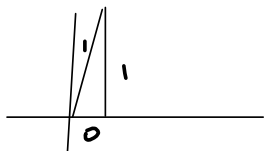
Fact:



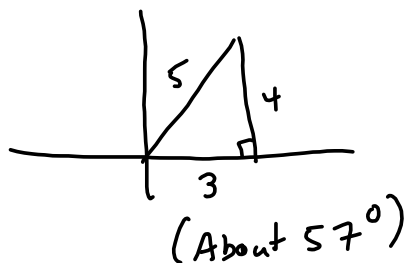
tangent of θ is $\tan(\theta)$

$$= \frac{y}{x} = \frac{\text{opposite}}{\text{adjacent}}$$

$$\tan(90^\circ) = \frac{y}{x} = \frac{1}{0} \text{ DNE, undefined, } \exists$$



Special 3-4-5



1.1

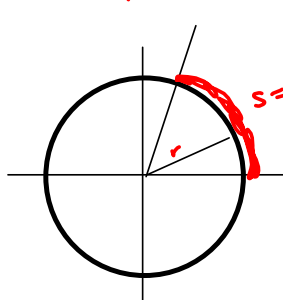
 360° is 2π RadiansCircumference is $2\pi r$

All the way around the circle

Arc length of $\frac{1}{2}$ -circle?

$$\frac{1}{2}(2\pi r) = \pi r = \theta r$$

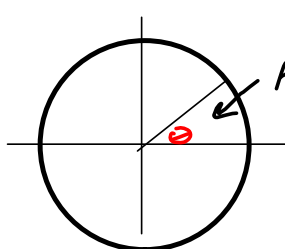
$$\frac{1}{4}\text{-circle? } \frac{1}{2}\pi r = \frac{1}{2}\theta r$$



360°	2π	Full
180°	π	HALF
90°	$\frac{\pi}{2}$	Quarter

$$s = r\theta$$

Do same for area of sector



Area of sector =

$$\begin{aligned} \pi r^2 &= \text{Area of whole thing} \\ &= \frac{1}{2}(2\pi)r^2 \\ &= \frac{1}{2}\theta r^2 \\ &= \frac{1}{2}r^2\theta \end{aligned}$$