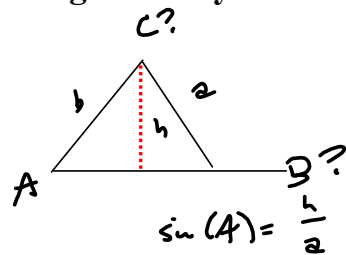


$$\frac{\sin A}{a} = \frac{\sin B}{b} \quad ; \quad \sin A = \frac{h}{b} \quad \text{and} \quad \sin B = \frac{h}{a} .$$

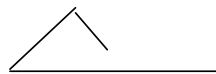
$$\rightarrow \quad b \sin A = h = a \sin B \quad \rightarrow$$

$$\frac{\sin A}{a} = \frac{\sin B}{b}$$

The only thing to worry about is being an ASS.



zero solutions

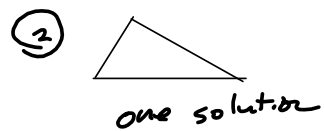


a is too short to form a triangle.

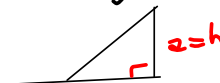
Ambiguous Case

$a < b$ & $a > h$
 Not too long Long enough

IF $a > h$: ① $a < b$ ② $a > b$

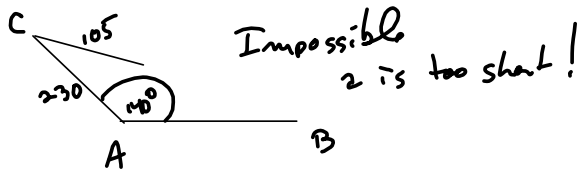


$a = h$ (rare)
 You have a right triangle!



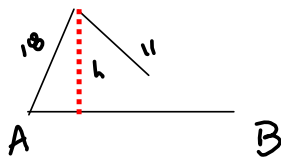
Use the Law of Sines to solve (if possible) the triangle. If two solutions exist, find both. Round your answers to two decimal places. (If a triangle is not possible, enter IMPOSSIBLE in each corresponding answer blank.)

$$A = 140^\circ, a = 105, b = 230$$



Use the Law of Sines to solve (if possible) the triangle. If two solutions exist, find both. Round your answers to two decimal places. (If a triangle is not possible, enter IMPOSSIBLE in each corresponding answer blank.)

$$A = 75^\circ, a = 11, b = 18$$



$$18 \sin(75)$$

$$17.38666487$$

$$\frac{h}{18} = \sin A$$

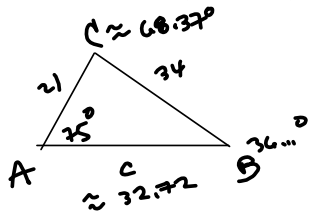
$$h = 18 \sin A = 18 \sin 75^\circ \approx 17.38666487 > 11 = a \text{ ?!}$$

2's too short to
form a triangle!
No Solution!

Use the Law of Sines to solve (if possible) the triangle. If two solutions exist, find both. Round your answers to two decimal places. (If not possible, enter IMPOSSIBLE.)

$A = 75^\circ, a = 34, b = 21$

a is long enough, but too long for there to be 2 solutions.



Exactly one solution.
B is acute

```
18sin(75
17.38666487
21sin(75)/34
.5966012456
sin^-1(Ans
36.62686564
```

$$\frac{\sin B}{b} = \frac{\sin A}{a} =$$

$$\sin B = \frac{b \sin A}{a} = \frac{21 \sin 75^\circ}{34} \approx .5966012456$$

$$\rightarrow B = \sin^{-1}(.5966...) \approx 36.62686564^\circ$$

$B \approx 36.63^\circ$

We get C by subtraction: $180^\circ - 75^\circ - 36.6...^\circ \approx 68.37 \approx C$

```
Ans+75-180
-68.37313436
-Ans
68.37313436
34sin(Ans)/sin(7
5)
32.72148585
```

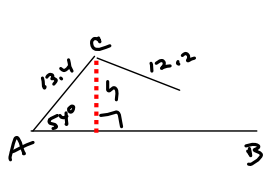
$$\frac{c}{\sin C} = \frac{a}{\sin A}$$

$$c = \frac{a \sin C}{\sin A} \approx \frac{34 \sin(68.37^\circ)}{\sin(75^\circ)} \approx 32.72 \approx c$$

$32.72 \approx c$

Use the Law of Sines to solve (if possible) the triangle. If two solutions exist, find both. Round your answers to two decimal places. (If a triangle is not possible, enter IMPOSSIBLE in each corresponding answer blank.)

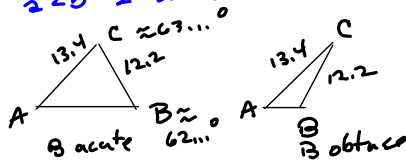
$A = 54^\circ, a = 12.2, b = 13.4$



$\frac{h}{13.4} = \sin 54^\circ$

$13.4 \sin(54)$
 10.84082772

$h = 13.4 \sin 54^\circ \approx 10.8$
 $a > h$ ✓ has sol'n
 $a < b$ 2 sol'ns



$\frac{\sin B}{b} = \frac{\sin A}{a}$

$\sin B = \frac{b \sin A}{a} = \frac{13.4 \sin(54^\circ)}{12.2} \approx .88 \dots$

$B \approx \arcsin(.88 \dots) \approx 62.69620255^\circ \approx B$

$C = 180^\circ - A - B \approx 63.30309745^\circ$

$C \approx 63.30^\circ$

$13.4 \sin(54) / 12.2$
 $.8885924364$
 $\sin^{-1}(\text{Ans})$
 62.69690255
 $\text{Ans} + 54 - 180$
 -63.30309745
 $\text{Ans} + 54 - 180$

$\text{Ans} + 54 - 180$
 -63.30309745
 $-\text{Ans}$
 63.30309745
 $12.2 \sin(\text{Ans}) / \sin(54)$
 13.47243302

$\frac{c}{\sin C} = \frac{a}{\sin A}$

$c = \frac{a \sin C}{\sin A} \approx 13.47243302$

$c \approx 13.47$

Now find other triangle, where B is obtuse.

$\sin B \approx .8885924364$



we want this one



$B_2 = \text{Obtuse solution} = 180^\circ - B$

$\approx 117.30^\circ \approx B_2 \text{ (obtuse)}$

B Acute sol'n.

still have $C = 180^\circ - A - B$
do $c = \frac{a \sin C}{\sin A}$ to do.

$13.4 \sin(54) / 12.2$
 $.8885924364$
 $180 - 62.69690255$
 117.30309745

Area of an Oblique Triangle

The area of any triangle is one-half the product of the lengths of two sides times the sine of their included angle. That is,

$$\text{Area} = \frac{1}{2}bc \sin A = \frac{1}{2}ab \sin C = \frac{1}{2}ac \sin B.$$

