

$(1, 13.8)$
 $(7, 78.6)$
 $f(x) = a \cos(b(x-c)) + d$

amp: $\frac{78.6 - 13.8}{2}$

$= \frac{64.8}{2} = 32.4 = a$

Period = 24 hrs:

$b \cdot 24 = 2\pi$

$24b = 2\pi \Rightarrow$

$b = \frac{2\pi}{24} = \frac{\pi}{12} = b$

START @ HIGH POINT:

$x = -5$ OR $x = 7 = c$

$f(x) \dots$ Nah. Use $t = \text{Months, starting w/ January corresponding to } t=1$

$f(t) = 32.2 \cos\left(\frac{\pi}{12}(x-7)\right) + 46.2$

$\approx 32.2 \cos(.3(x-7)) + 46.2$

WebAssign might want

$32.2 \cos(.3x - 2.1) + 46.2$

32.4

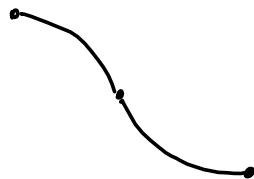
DOH! 12 months in a year, Steve!

So, $32.2 \cos\left(\frac{\pi}{6}(t-7)\right) + 46.2$

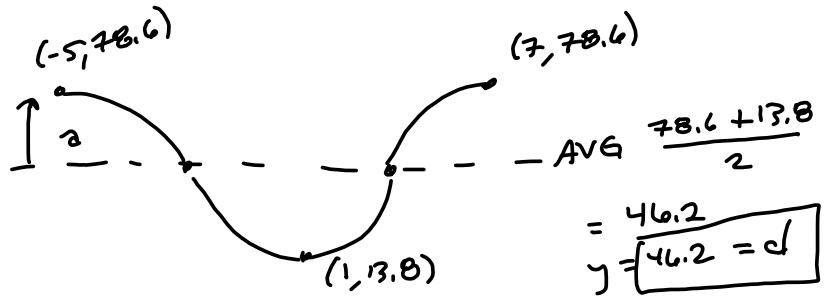
$\approx 32.2 \cos(.5(t-7)) + 46.2$

32.4

WebAssign Answer:

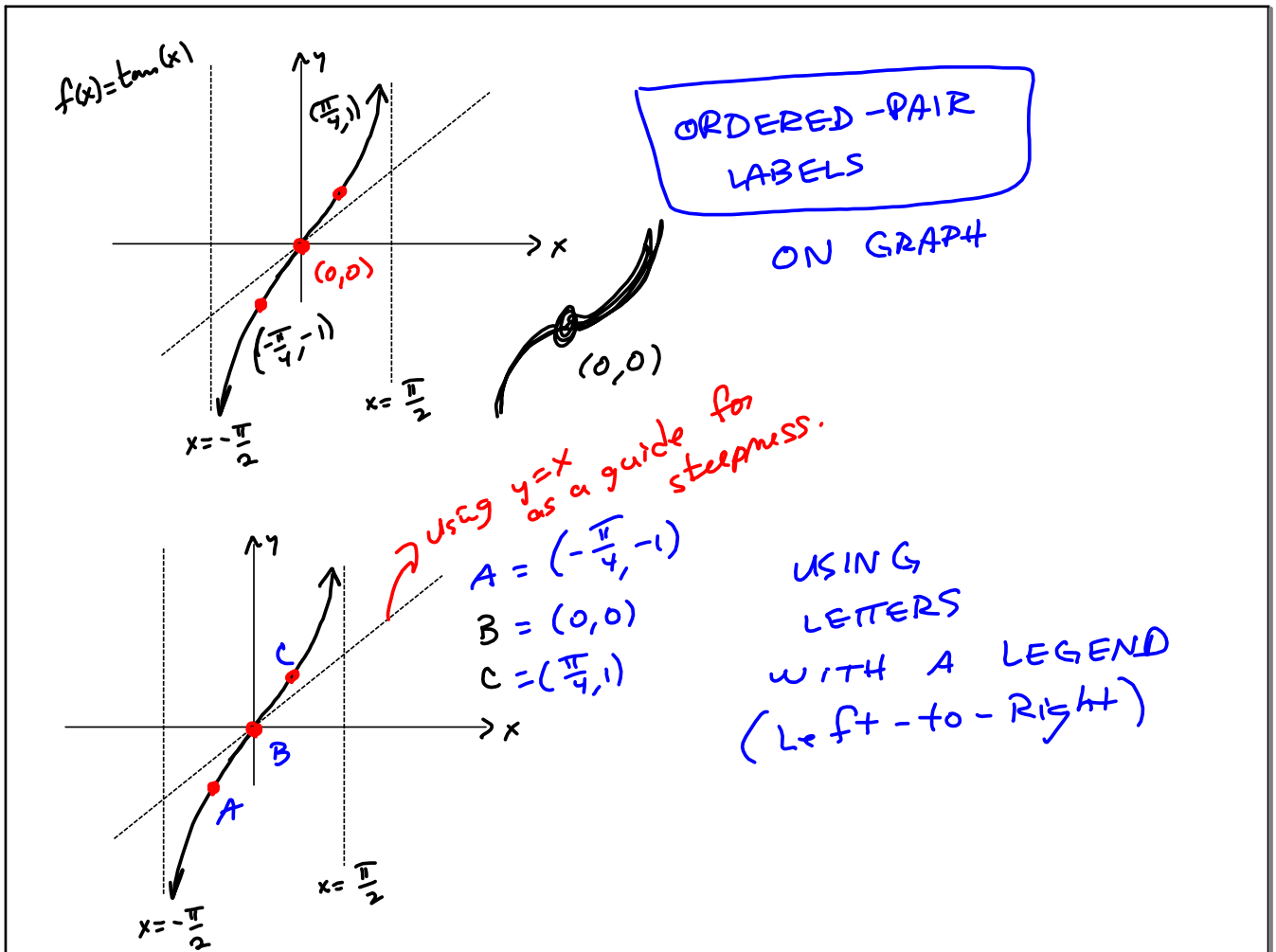


They're flipping it, for no good reason



Ans/2	92.40000000
$\pi/12$	46.20000000
Ans*7	.26179939
	1.83259571

Ans*7	.26179939
$\pi/12*2$	1.83259571
Ans*7	.52359878
	3.66519143

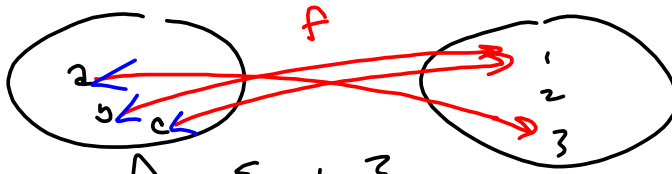


Did we do Inverse Trig, like arcsine ($\sin^{-1}(x)$)
 $\sin^{-1}(x)$

We kind of did, because I've already used " \sin^{-1} " key on my calculator.

$y = f(x)$ is a function means
 For each x in a set, $y = f(x)$ is a unique number in another set.
 Domain Range.

f is a function means f is a rule that assigns to each x in one set (Domain) to a unique y in another set (Range)



Domain = $D = \{a, b, c\}$

Range = $R = \{1, 3\}$

f is NOT 1-to-1.

Vertical Line Test

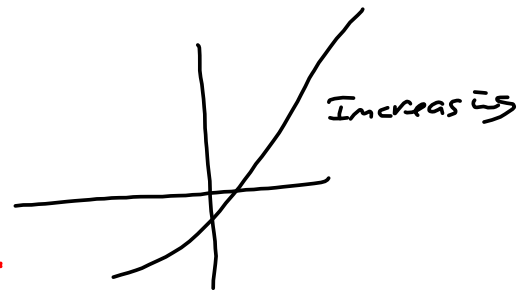
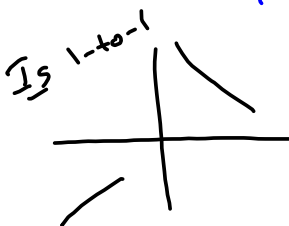
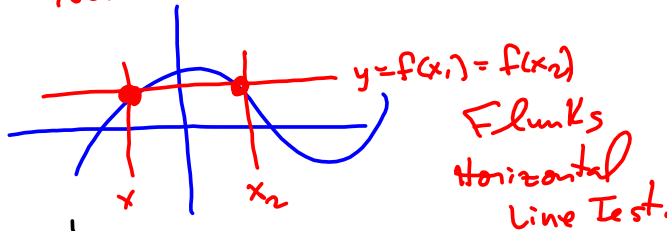
f is 1-to-1 Means

f is a function such that each $y \in R$ is assigned to exactly one x in the Domain.

$f(x_1) = f(x_2) \Rightarrow x_1 = x_2$
 $x_1 \neq x_2 \Rightarrow f(x_1) \neq f(x_2)$

HORIZONTAL LINE TEST

NOT 1-to-1:



$$y = f(x)$$

$$\sin(x) = \frac{\sqrt{3}}{2}$$

$$x = f^{-1}(y)$$

$$\sin^{-1}(\sin(x)) = \sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = \frac{\pi}{3} \text{ or } 60^\circ$$

Now, these trig functions are not 1-to-1.
So, just like x^2 , we restrict the domain.

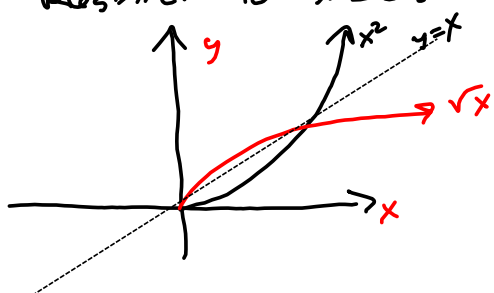
$$y = x^2 = y \Rightarrow$$

$x = \pm\sqrt{y}$ is not an inverse function

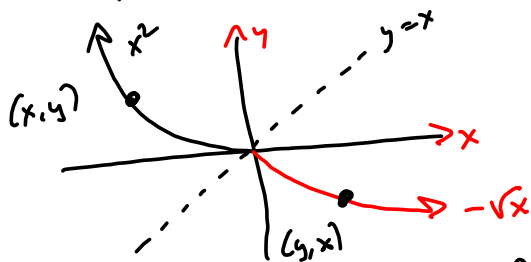
Restrict to $x \geq 0$.

$$f(x) = x^2 \quad \downarrow$$

$$f^{-1}(x) = +\sqrt{x}$$



Restrict to $x \leq 0$:

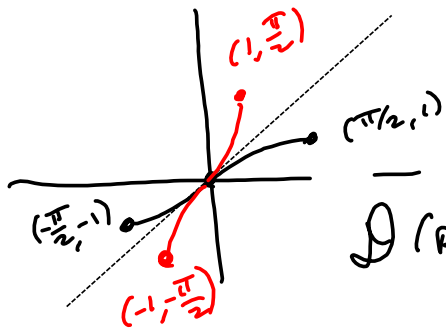


$$f(x) = x^2$$

$$f^{-1}(x) = -\sqrt{x}$$

$f^{-1}(x)$: Reflect $f(x)$ about $y=x$
SWAP x & y !

Restricted sine:



$\sin(x)$
Restricted

$D(\text{Restricted Sine}) = [-\frac{\pi}{2}, \frac{\pi}{2}] = R(\arcsin(x))$

$\arcsin(x) = \sin^{-1}(x)$

$R(\text{Restricted}) = [-1, 1] = D(\arcsin(x))$

PRACTICAL

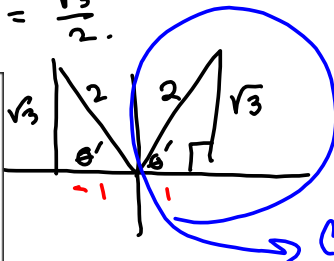
Find all sol'ns $x \in [0, 2\pi]$ of

$\sin(x) = \frac{\sqrt{3}}{2}$

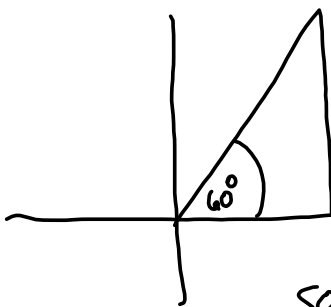
$\theta' = \text{Reference Angle}$

$\pi/6$	3.66519143
$\sin^{-1}(\sqrt{3}/2)$.52359878
$\sin^{-1}(\sqrt{3}/2)$	1.04719755
$\sin^{-1}(\sqrt{3}/2)$	60.00000000

That says



Calculator's \sin^{-1} can only see this one. YOU must use the reference angle & logic to get the other sol'n.



So



So, $x = 60^\circ, 120^\circ$

$180^\circ - 60^\circ = 120^\circ$