

WebAssign access is thru D2L to get registered.

After you're registered, you can don't need the D2L. Just go to [webassign.net](http://webassign.net) and log in directly.

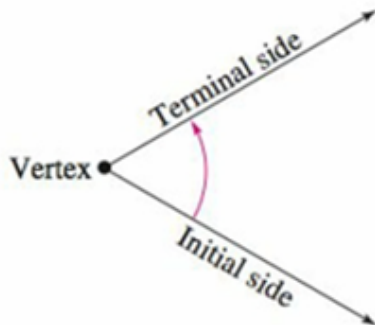
D2L will be our "home base" for e-mail, announcements, dropping off Writing Projects (More on those, Thursday).

But you should be able to do EVERYTHING ELSE with [webassign.net](http://webassign.net)

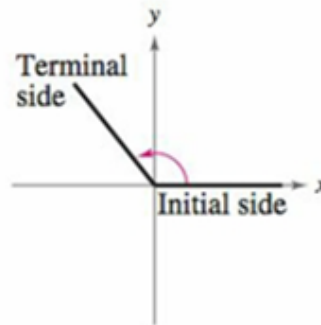
and

[harryzaims.com](http://harryzaims.com)

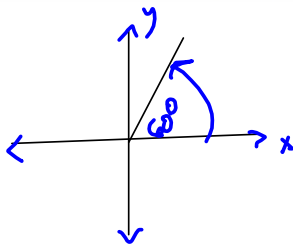
## Section 1.1 - Radian and Degree Measure



Angle  
Figure 1.1



Angle in standard position  
Figure 1.2



360° to go full circle.

## RADIAN MEASURE

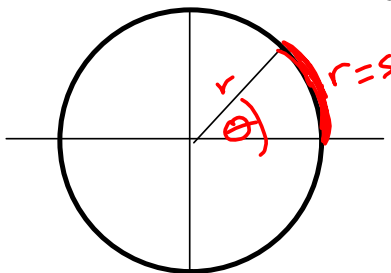
One Radian is the angle corresponding to an arc length  $s$  equal to the radius  $r$

Radian measure is the ratio of arc length to radius

$$\theta = \Theta = \text{Angle in radians} = \frac{s}{r}$$

So when  $s = r$ ,  $\theta = 1$

$$\theta = \frac{s}{r} = 1 \text{ radian} \approx 57^\circ$$



$$\theta = 1 !$$

An **angle** is determined by rotating a ray (half-line) about its endpoint. The starting position of the ray is the **initial side** of the angle, and the position after rotation is the **terminal side**, as shown in Figure 1.1. The endpoint of the ray is the **vertex** of the angle. This perception of an angle fits a coordinate system in which the origin is the vertex and the initial side coincides with the positive  $x$ -axis. Such an angle is in **standard position**, as shown in Figure 1.2. Counterclockwise rotation generates **positive angles** and clockwise rotation generates **negative angles**, as shown in Figure 1.3. Angles are labeled with Greek letters such as

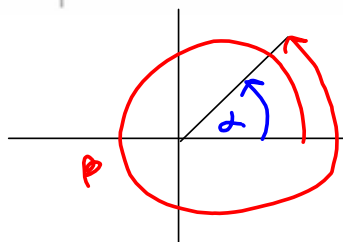
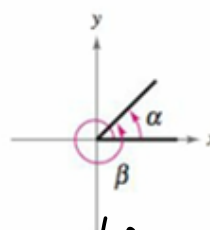
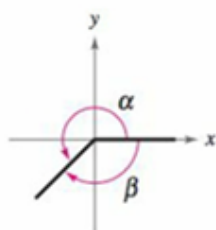
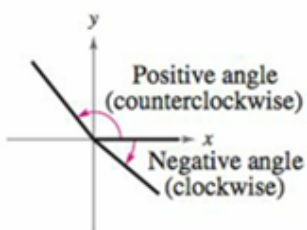
$\alpha$  (alpha),  $\beta$  (beta), and  $\theta$  (theta)

as well as uppercase letters such as

$A$ ,  $B$ , and  $C$ .

In Figure 1.4, note that angles  $\alpha$  and  $\beta$  have the same initial and terminal sides. Such angles are **coterminal**.

$\gamma$  gamma  $\omega$  omega  
 $\delta$  delta  $\xi$  xi  
 $\epsilon$  epsilon



$\alpha$  &  $\beta$  are coterminal  
 They end at the ray.

$$\alpha = 45^\circ = \frac{\pi}{4}$$

$$\beta = 360^\circ + 45^\circ = 405^\circ = \frac{9\pi}{4}$$

$$2\pi + \frac{\pi}{4} = \frac{(8+1)\pi}{4}$$

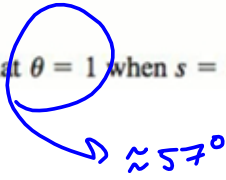
No symbol after? Means "Radians."

**Definition of Radian**

One **radian** is the measure of a central angle  $\theta$  that intercepts an arc  $s$  equal in length to the radius  $r$  of the circle. See Figure 1.5. Algebraically, this means that

$$\theta = \frac{s}{r}$$

where  $\theta$  is measured in radians. (Note that  $\theta = 1$  when  $s = r$ .)



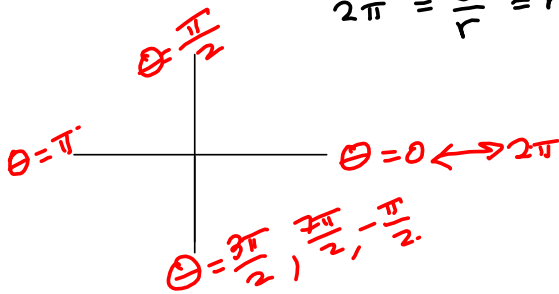
What angle, in radians, corresponds to going full circle?

Buehler? Buehler?

Daniel says  $2\pi$ . He's Right!

What's the circumference of a circle of radius  $r$ ?

Mayo says  $2\pi r = s \implies 2\pi = \frac{s}{r} = \text{radian measure of going full circle}$



$$\frac{2\pi \text{ radians}}{1 \text{ revolution}} = \frac{360^\circ}{1 \text{ revolution}} \implies$$

$$\frac{\pi}{180^\circ} = \frac{2\pi \text{ radians}}{360^\circ} = \frac{1 \text{ rev}}{1 \text{ rev}} = 1$$

Converting radians to degrees & conversely

If you're given 2.3 radians, to "see" it,

convert  $(2.3 \text{ radians}) \left( \frac{180^\circ}{\pi \text{ radians}} \right) \approx 131.7802929^\circ$

Approximate.

= -vs-  $\approx$   
I'm a stickler!

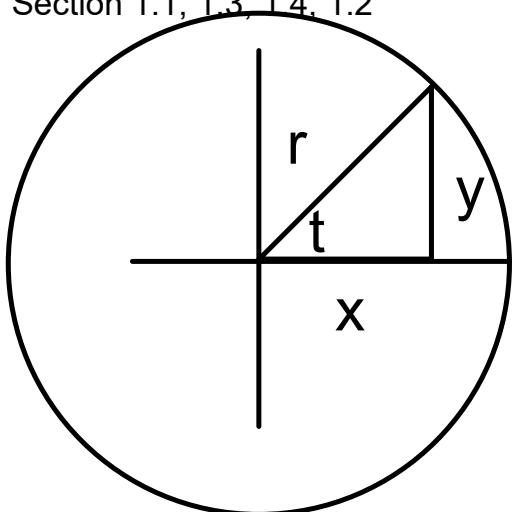
```
2.3*180/pi
131.7802929
```

My name is Steve Mills (Harry)

WebAssign!!!!

Did you find the WebAssign OK?

Section 1.1, 1.3, 1.4, 1.2



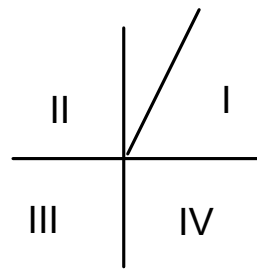
$$\sin(t) = y/r$$

$$\cos(t) = x/r$$

$$\tan(t) = y/x$$

12-point unit circle is...

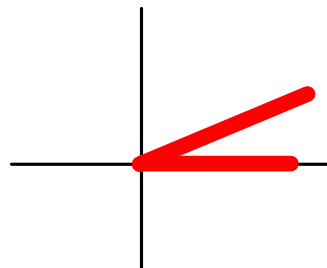
Bleah!



Heuristic learning is when you learn in the context of problem-solving.

Resources on [harryzaims.com](http://harryzaims.com)

When doing homework, have 2 [harryzaims.com](http://harryzaims.com) windows open, one for the notes to locate the exercise and the other for video. IF YOU NEED THAT KIND OF HELP ON AN EXERCISE.



$$s = rt$$

$$s = \text{arc length}$$

$$r = \text{radius}$$

$$t = \text{angle in radians}$$

$$t = s/r$$

$$t = s \text{ when radius} = 1.$$

Circumference of a circle of radius  $r$  is  $2\pi r$

When  $r = 1$ , then circumference =  $2\pi$

and the number of RADIANS is ALSO  $2\pi$  !!!

That's where  $s = rt$  comes from

and  $s = t$ , when  $r = 1$ , which is really cool!

One full revolution is 360 degrees

One full revolution is  $2\pi$  radians

To convert radians to degrees, multiply by  $180/\pi$

to do the reverse, multiply by  $\pi/180$  !

You can get dain bramage from the Cengage guy's talk about the bicycle and converting from rpm to linear speed.

<https://harryzaims.com/122/122-fall-21/notes/>

<https://harryzaims.com/122/122-fall-21/lectures/>



**970-290-0550**

