

$$3 \frac{1}{2} = 3 + \frac{1}{2}$$

$$r = \sqrt{x^2 + y^2} = \sqrt{\left(\frac{7}{2}\right)^2 + (-7)^2}$$

$$= \sqrt{\frac{49}{4} + \frac{961}{4}} = \sqrt{\frac{1010}{4}} = \frac{\sqrt{1010}}{2}$$

1157 is prime,  
so ...

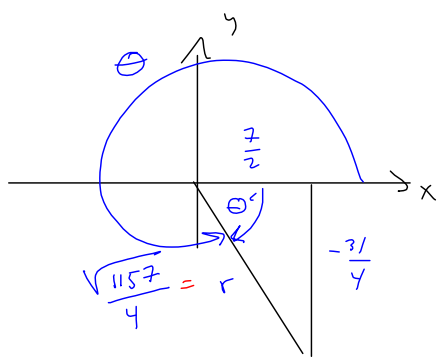
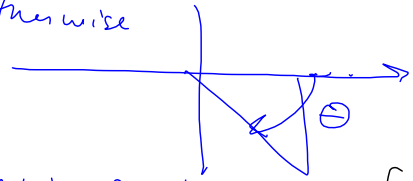
$$\sin \theta = \frac{y}{r} = \frac{-7}{\frac{\sqrt{1157}}{4}} = -\frac{28}{\sqrt{1157}}$$

Radical (root) of the quotient is the quotient of the radicals

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

This is  
 $\frac{y}{x} = \tan \theta$   
dummy

$\theta'$  is the REFERENCE ANGLE  
If we're told that  $0 < \theta < 2\pi$ ,  
then I mailed the picture,  
otherwise



would be legit

Simpl. Rad. Form.

$$\frac{-31}{\sqrt{1157}} \cdot \frac{\sqrt{1157}}{\sqrt{1157}} = \frac{-31\sqrt{1157}}{1157}$$

$$\sin \theta = \frac{y}{r} = \frac{-7}{\frac{\sqrt{1157}}{4}} = -\frac{28}{\sqrt{1157}}$$

Fine by me, unless I SPECIFY simplified radical form.

$$\frac{-7}{\sqrt{1157}} = \sin \theta$$

$$\cos \theta = \frac{x}{r} = \frac{7/2}{\frac{\sqrt{1157}}{4}} = \frac{14}{\sqrt{1157}} = \cos \theta$$

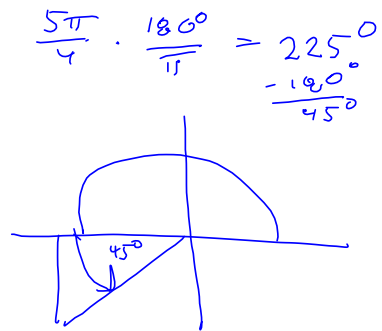
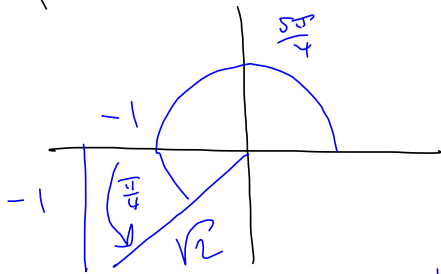
(Half-angle formulas exercises)

$$\tan \theta = \frac{y}{x} = \frac{r \sin \theta}{r \cos \theta} = \frac{\sin \theta}{\cos \theta} = \frac{-7}{14} = \frac{\sqrt{1157}}{14} = \frac{-7}{14} = \tan \theta$$

$$\csc \theta = \frac{1}{\sin \theta} = -\frac{\sqrt{1157}}{28}$$

$$\sec \theta = \frac{1}{\cos \theta} = \frac{\sqrt{1157}}{14} \quad \cot \theta = \frac{1}{\tan \theta} = -\frac{14}{7} = -2$$

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$$\sin \theta = \frac{y}{r} = \frac{\text{opp}}{\text{hyp}} = \frac{-1}{\sqrt{2}} = \sin \theta$$

$$-\frac{\sqrt{2}}{2}$$

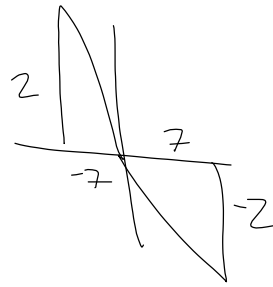
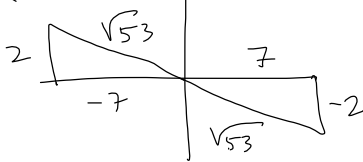
$$\cos \theta = \frac{x}{r} = \frac{-1}{\sqrt{2}} = -\frac{\sqrt{2}}{2}$$

$$\tan \theta = \frac{y}{x} = \frac{-1}{-1} = 1 = \tan \theta$$

$$2 \sqrt{1.414}$$

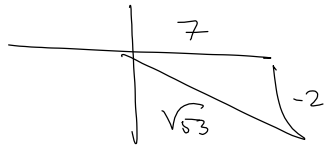
$$1.414 \sqrt{1.000}$$

a)  $\tan \theta = -\frac{2}{7}$



$2^2 + 7^2 = 4 + 49 = 53$

b)  $\cos \theta > 0$



$\sin \theta = \frac{-2}{\sqrt{53}}$

$\csc \theta = -\frac{\sqrt{53}}{2}$

$\cos \theta = \frac{7}{\sqrt{53}}$

$\sec \theta = \frac{\sqrt{53}}{7}$

$\tan \theta = -\frac{2}{7}$

$\cot \theta = -\frac{7}{2}$

c)  $\tan \theta = -\frac{2}{7}$

**TAN<sup>-1</sup>** is inverse tangent, which can be confused with

Inverse of the TRIG OPERATION, tangent.

$\frac{1}{\text{TAN}}$  b/c mathematicians are jerks. I prefer

**arctangent** =  $\tan^{-1}$

Arithmetic inverse w/rt multiplication

$\tan \theta = -\frac{2}{7} \Rightarrow \arctan(\tan \theta) = \arctan(-\frac{2}{7})$

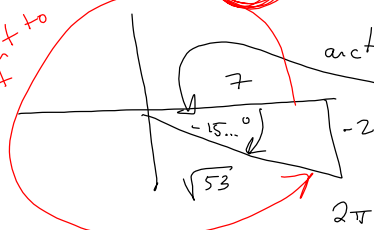
$\tan^{-1}(-2/7)$   
 -0.278299659  
 Ans\*180/π  
 -15.9453959

d)  $\theta \approx -0.278299659$  ?

$\approx -15.9453959$  ?

Not quite

want to measure it counter-clockwise



arctangent says

We want  $\theta \in [0, 2\pi)$

$-0.278... < 0$

$2\pi - 0.278... = \theta$

-0.278299659  
 Ans\*180/π  
 -15.9453959  
 $\tan^{-1}(-2/7)$   
 -0.278299659  
 Ans+2π  
 6.004885648

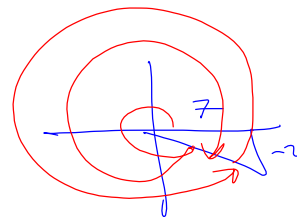
$\theta \approx 6.004885648$

$\theta \approx 6.005$

-15.9453959  
 $\tan^{-1}(-2/7)$   
 -0.278299659  
 Ans+2π  
 6.004885648  
 Ans\*180/π  
 344.0546041

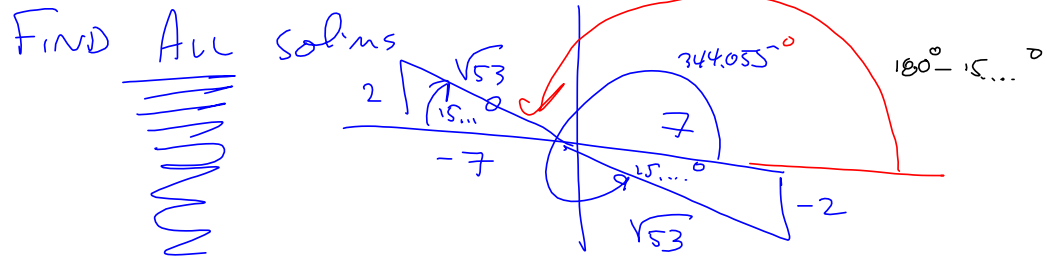
$\theta \approx 344.0546041$

$\theta \approx 344.055^\circ$



4. Answer the questions about the equation  $\tan(\theta) = -\frac{2}{7}$ .
- (5 points) Sketch two triangles that satisfy  $\tan(\theta) = -\frac{2}{7}$ .
  - (5 pts) Suppose that  $\cos(\theta) > 0$ . Find the other five trigonometric functions of  $\theta$ .
  - (5 pts) Assuming  $0 \leq \theta < 2\pi$ , find  $\theta$ , in radians *and* degrees, rounded to 3 decimal places.
  - (5 pts) Give *all* solutions to the equation  ~~$\tan(\theta) = -\frac{2}{7}$~~   $\tan \theta = -\frac{2}{7}$ , in degrees *and* radians, rounded to three (3) decimal places.

Do NOT ASSUME  $\cos \theta > 0$ , any more.



How to find the other solutions?

Method 1:

Observe that the 2 triangles are  $180^\circ$  apart. So to get the 2nd, add/subtract  $180^\circ$  from the 1st one

$$\mathbb{Z} = \{0, \pm 1, \pm 2, \pm 3, \dots\}$$

$$344.055^\circ \pm 180^\circ \cdot 2$$

$$\left\{ 344.055^\circ + 180^\circ n \mid n \in \mathbb{Z} \right\}$$

OR

$$\left\{ 6.005 + n\pi \mid n \in \mathbb{Z} \right\}$$

Method 2:

$$180^\circ - 15\dots^\circ \approx 164.055^\circ$$

$$\text{So } \left\{ 344.055^\circ + 360^\circ n \mid n \in \mathbb{Z} \right\}$$

$$\left\{ 164.055^\circ + 360^\circ n \mid n \in \mathbb{Z} \right\}$$