$\qquad$ NO GRAPHING CALCULATORS!!!

I think you know the drill on margins and legibility. I can't give points for what I can't read. Take a minute, at the end, to make sure your work is organized and submitted in proper order.

1. Consider the triangle in the figure. Assume lengths are in centimeters.
a. (10 pts) Use the Law of Cosines to find the length of side a, to 4 decimal places.
b. (10 pts) Use the Law of Sines to find angle $C$ to 4 decimal places.
2. Consider the directed line segment $\overrightarrow{P Q}$ in the figure on the right. I want you to provide some basic facts about the vector $\bar{u}$ :
a. (5 pts) Express the vector $\bar{u}=\overrightarrow{P Q}$ in component form.
b. (5 pts) Compute the magnitude of $\bar{u}$. Leave your answer in simplified radical form.
c. (10 pts) Find the direction angle of $\bar{u}$. Use degrees, rounded

 to 4 places.
3. Let $\bar{u}=\langle-7,5\rangle$.
a. (5 pts) Express $\bar{u}$ as a linear combination of the canonical (standard) unit vectors $\bar{i}$ and $\bar{j}$.
b. (5 pts) What's another word for the sum of 2 vectors?
4. Dad's out walking his dog and his toddler. The dog pulls with 40 pounds of force in the direction of the vector $\bar{u}$. The toddler pulls with 30 pounds of pressure in the direction of the vector $\bar{v}$.

a. (10 pts) Express $\bar{u}$ and $\bar{v}$ in component form.
b. (10 pts) What's the net force, as a vector, on poor Dad?
5. Consider the triangle in the figure on the right.
a. (10 pts) Prove there are 2 triangles that are possible from this ambiguous information.
b. (10 pts) Find the two possible values for Angle C.

6. (10 pts) Find $\sin \left(\frac{u}{2}\right), \cos \left(\frac{u}{2}\right)$ and $\tan \left(\frac{u}{2}\right)$, given that $\cos (u)=-\frac{7}{11}$ and $\sin (u)>0$.

BONUS SECTION: Answer up to 3 questions for up to 15 bonus points.
B1 (5 pts) Build a cosine function that achieves its maximum height of $y=150$ meters at time $x=9$ seconds and its minimum height of $y=-130$ meters at $x=17$ seconds.

B2 (5 pts) Find all solutions of the equation $4 \cos ^{2}(2 x)-1=0$ in the interval $[0,2 \pi)$.
B3 (5 pts) Sketch the graph of $-20 \sin \left(\frac{7 \pi}{22} x-\frac{14 \pi}{11}\right)+53$.

