

(4)

$$3\tan^3(x) - 3\tan^2(x) - \tan(x) + 1 = 0$$

$$3u^3 - 3u^2 - u + 1 = 0$$

$$3u^2[u-1] - 1[u-1] = 0$$

$$[u-1](3u^2-1) = 0$$

$$(u-1)(\sqrt{3}u-1)(\sqrt{3}u+1) = 0$$

$(\sqrt{3}u)^2 - 1^2$

$$u-1=0$$

OR

$$3u^2 - 1 = 0$$

$$u=1$$

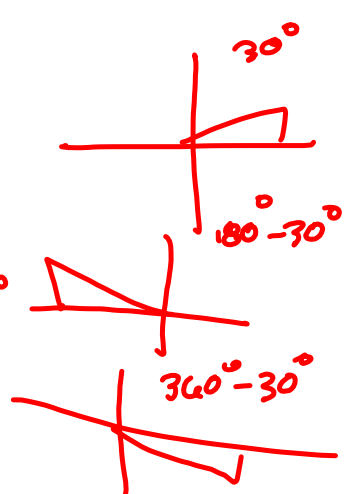
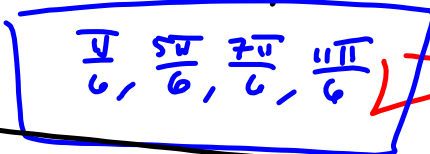
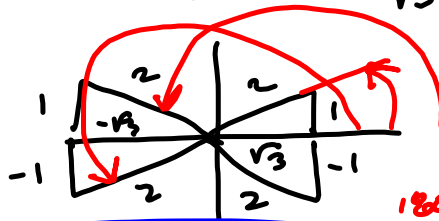
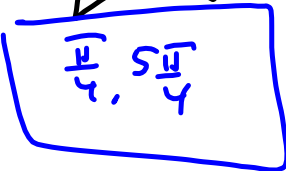
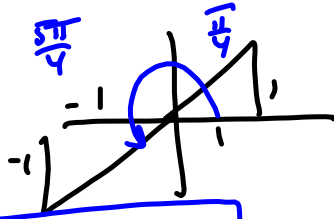
$$3u^2 = 1$$

$$\tan u = 1$$

$$u^2 = \frac{1}{3}$$

$$u = \pm \sqrt{\frac{1}{3}} = \pm \frac{1}{\sqrt{3}}$$

$$\tan x = \pm \frac{1}{\sqrt{3}}$$



$$x \in \left\{ \frac{\pi}{6}, \frac{\pi}{4}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{5\pi}{4}, \frac{11\pi}{6} \right\}$$

(b) All solms

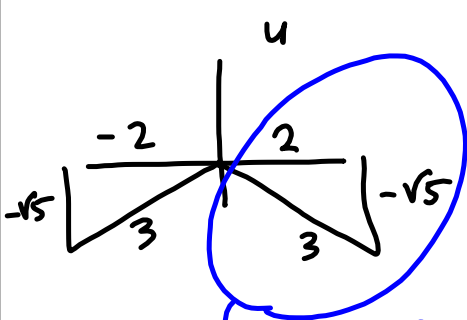
$$\begin{array}{l}
 \frac{\pi}{6} + 2n\pi \\
 \frac{\pi}{4} + 2n\pi \\
 \frac{5\pi}{6} + 2n\pi \\
 \frac{7\pi}{6} + 2n\pi \\
 \frac{3\pi}{4} + 2n\pi \\
 \frac{11\pi}{6} + 2n\pi
 \end{array}
 \begin{array}{l}
 \rightarrow \frac{\pi}{6} + n\pi \\
 \rightarrow \frac{\pi}{4} + n\pi \\
 \rightarrow \frac{5\pi}{6} + n\pi \\
 \rightarrow \frac{7\pi}{6} + n\pi \\
 \rightarrow \frac{3\pi}{4} + n\pi \\
 \rightarrow \frac{11\pi}{6} + n\pi
 \end{array}
 \begin{array}{l}
 \rightarrow \frac{\pi}{4} + n\pi \\
 \rightarrow \frac{5\pi}{6} + n\pi \\
 \forall n \in \mathbb{Z}
 \end{array}$$

$$\left\{ \frac{\pi}{6} + n\pi, \frac{\pi}{4} + n\pi, \frac{5\pi}{6} + n\pi \mid n \in \mathbb{Z} \right\}$$

$$\left\{ x + n\pi \mid x = \frac{\pi}{6}, \frac{\pi}{4}, \frac{5\pi}{6}, n \in \mathbb{Z} \right\}$$

$$\left\{ x + n\pi \mid x \in \left\{ \frac{\pi}{6}, \frac{\pi}{4}, \frac{5\pi}{6} \right\}, n \in \mathbb{Z} \right\}$$

③ $\sin(u) = -\frac{\sqrt{5}}{3}$ and $\tan(u) < 0$



$$\sqrt{3^2 - (-\sqrt{5})^2}$$

$$\sqrt{9-5} = \sqrt{4} = 2$$

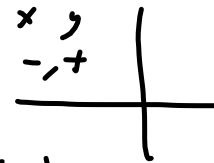
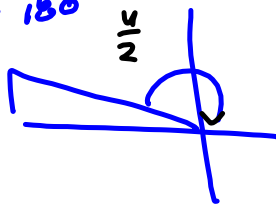
so $270^\circ < u < 360^\circ$

$\frac{3\pi}{2} < u < 2\pi$

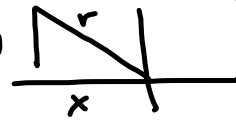
$120^\circ < \frac{u}{2} < 180^\circ$
QII

$\frac{3\pi}{4} < \frac{u}{2} < \pi$

$$\sin\left(\frac{u}{2}\right) = \sqrt{\frac{1-\cos u}{2}}$$



$$= \sqrt{\frac{1 - \frac{2}{3}}{2}} = \sqrt{\frac{\frac{1}{3}}{2}} = \sqrt{\frac{1}{6}} = \frac{1}{\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}}$$



$$= \frac{\sqrt{6}}{6} = \sin\left(\frac{u}{2}\right)$$

$$1 - \frac{2}{3} = \frac{1}{3} = \frac{1}{3} \cdot \frac{3}{3} = \frac{3-2}{3} = \frac{1}{3}$$

$$\frac{1}{3} = \frac{1}{3} \cdot \frac{1}{2} = \frac{1}{6}$$

$$\cos\left(\frac{u}{2}\right) = -\sqrt{\frac{1+\cos u}{2}}$$

$$= -\sqrt{\frac{1 + \left(\frac{2}{3}\right)}{2}} = -\sqrt{\frac{\frac{5}{3}}{2}} = -\sqrt{\frac{5}{6}} = -\frac{\sqrt{5}}{\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}}$$

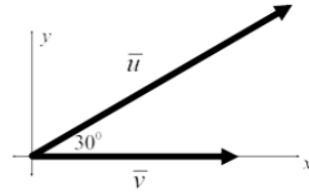
$$= -\frac{\sqrt{30}}{6} = \cos\left(\frac{u}{2}\right)$$

$$\tan\left(\frac{u}{2}\right) = \frac{\sqrt{6}}{6} \cdot \left(-\frac{6}{\sqrt{30}}\right) = -\frac{\sqrt{6}}{\sqrt{30}} = -\sqrt{\frac{6}{30}} = -\sqrt{\frac{1}{5}}$$

$$= -\frac{\sqrt{5}}{5} = \tan\left(\frac{u}{2}\right)$$

Test 3 Spring '17

4. Forces with magnitudes $\|\vec{u}\| = 90$ N and $\|\vec{v}\| = 60$ N are acting on a hook, as shown in the figure.
- (5 pts) Express \vec{u} and \vec{v} in component form.
 - (5 pts) Express the resultant force, in component form.
 - (5 pts) Find the direction angle of the resultant force, in degrees, rounded to 4 decimal places.



5. Let $f(x) = 5x^3 - 23x^2 + 77x - 39$

(a) $f(\theta)$

$$\vec{u} = 90 \langle \cos 30^\circ, \sin 30^\circ \rangle$$

$$= 90 \left\langle \frac{\sqrt{3}}{2}, \frac{1}{2} \right\rangle$$

$$= \langle 45\sqrt{3}, 45 \rangle = \vec{u}$$

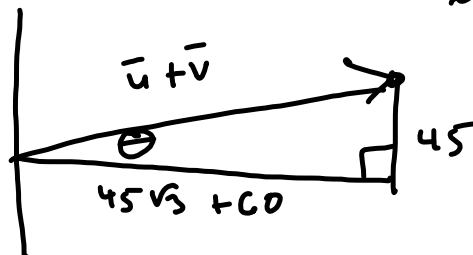
$$\vec{v} = \langle 60, 0 \rangle$$

(b) $\vec{u} + \vec{v} = \langle 45\sqrt{3}, 45 \rangle + \langle 60, 0 \rangle$

$$= \langle 45\sqrt{3} + 60, 45 \rangle = \vec{u} + \vec{v}$$

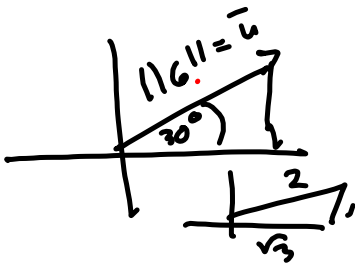
(c) $\theta = \arctan\left(\frac{45}{45\sqrt{3} + 60}\right) \approx 18.06753728^\circ$

$$\approx 18.0675^\circ$$

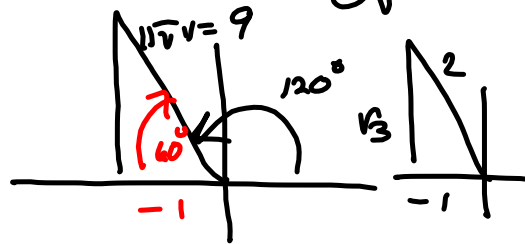


From the Test 3 sitting in
Chapter 4 videos.

$$\|\vec{u}\| = 6, \theta_{\vec{u}} = 30^\circ$$



$$\|\vec{v}\| = 9, \theta_{\vec{v}} = 120^\circ$$

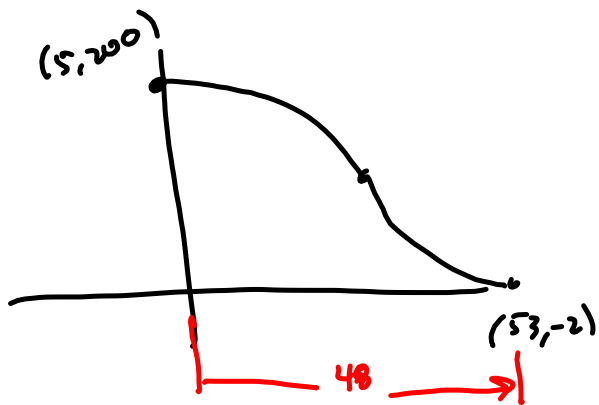


$$\vec{u} = 6 \langle \cos 30^\circ, \sin 30^\circ \rangle$$

$$= \left\langle \frac{6\sqrt{3}}{2}, \frac{6}{2} \right\rangle = \boxed{\langle 3\sqrt{3}, 3 \rangle = \vec{u}}$$

$$\vec{v} = 9 \langle \cos 120^\circ, \sin 120^\circ \rangle$$

$$= \boxed{\left\langle -\frac{9}{2}, \frac{9\sqrt{3}}{2} \right\rangle = \vec{v}}$$



$\frac{1}{2}$ -period
 1 period: $T = 96$
 $\cos(bx)$

want
 $bx = 2\pi$ when
 $x = 96$

$$96b = 2\pi$$

$$b = \frac{2\pi}{96} = \frac{\pi}{48}$$