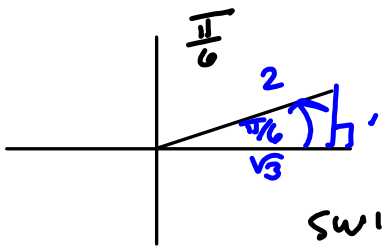
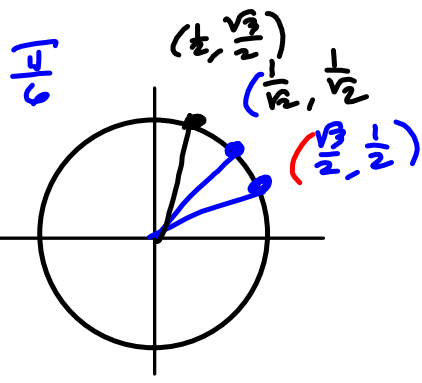


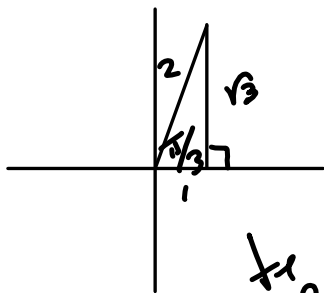
1st quadrant trig values:

$0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}$

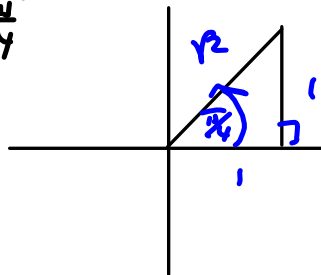
sohcahtoa



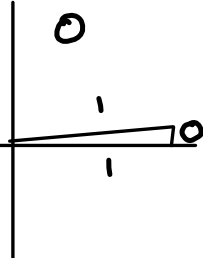
SWIDT?



$\frac{\pi}{4}$



Degenerate  
triangles  
for quadrants  
 $\frac{\pi}{2}$  for quadrants.

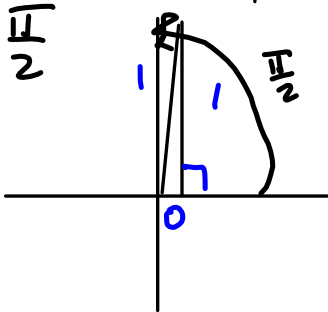


$\sin(0) = \frac{0}{1} = 0$

$\cos(0) = \frac{1}{1} = 1$

$\tan(\theta) = \frac{0}{1} = 0$

$\cot \theta = \frac{1}{0}$  ~~A~~

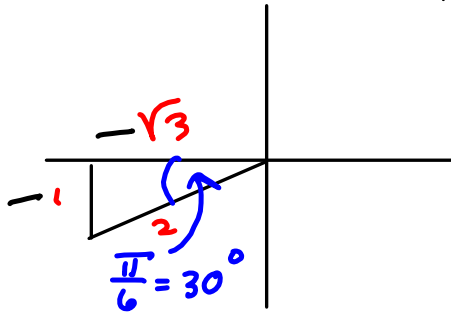
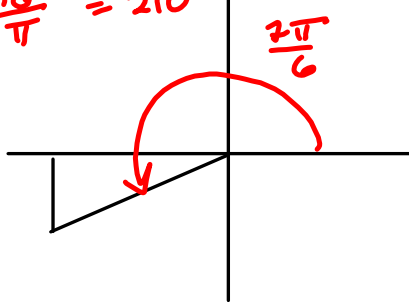


$\sin \frac{\pi}{2} = 1$

$\cos \frac{\pi}{2} = \frac{0}{1} = 0$

$\tan \frac{\pi}{2} = \frac{1}{0}$  ~~A~~

$$\frac{7\pi}{6} \cdot \frac{180^\circ}{\pi} = 210^\circ$$



$$\sin \frac{7\pi}{6} = -\frac{1}{2}$$

$$\cos \frac{7\pi}{6} = -\frac{\sqrt{3}}{2}$$

$$\tan \frac{7\pi}{6} = \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

Division ↓

$$\frac{1}{\sqrt{3}}$$

$$1.732 \overline{) 1.00000}$$

$$\frac{\sqrt{3}}{3}$$

$$3 \overline{) 1.732} \quad \text{Ezer.}$$

$$\sqrt{3}$$

$$1.5^2 = 2.25$$

$$1.6^2 = 2.56$$

$$1.7^2 = 2.89$$

$$1.8^2 = 3.24$$

$$1.75^2$$

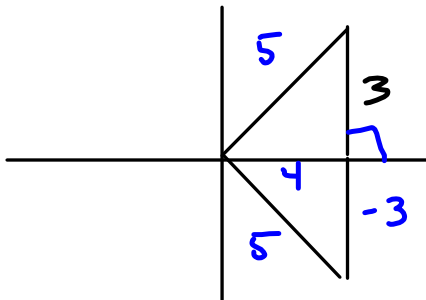
$\sqrt{x}$

$$\frac{f(x+h) - f(x)}{h} = \frac{\sqrt{x+h} - \sqrt{x}}{h} =$$

$$= \left( \frac{\sqrt{x+h} - \sqrt{x}}{h} \right) \left( \frac{\sqrt{x+h} + \sqrt{x}}{\sqrt{x+h} + \sqrt{x}} \right) = \frac{x+h-x}{h(\sqrt{x+h} + \sqrt{x})}$$

$$= \frac{h}{h(\sqrt{x+h} + \sqrt{x})} \xrightarrow{h \rightarrow 0} \frac{1}{\sqrt{x} + \sqrt{x}} = \frac{1}{2\sqrt{x}}$$

$\cos \theta = \frac{4}{5}$  picture



Pythagoras "see"

$$a^2 + b^2 = c^2$$

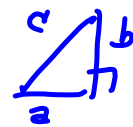
$$4^2 + b^2 = 5^2$$

$$25 - 16 = b^2$$

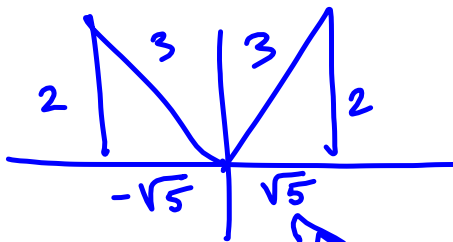
$$9 = b^2$$

$$\pm 3 = b$$

Take the positive.



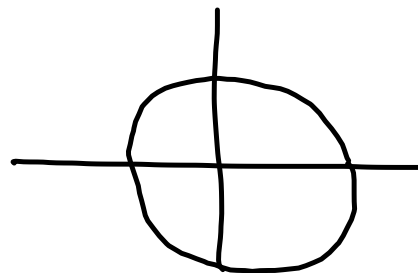
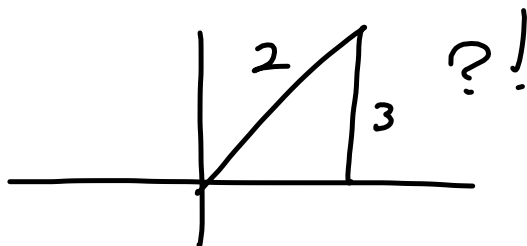
$$\sin \theta = \frac{2}{3}$$

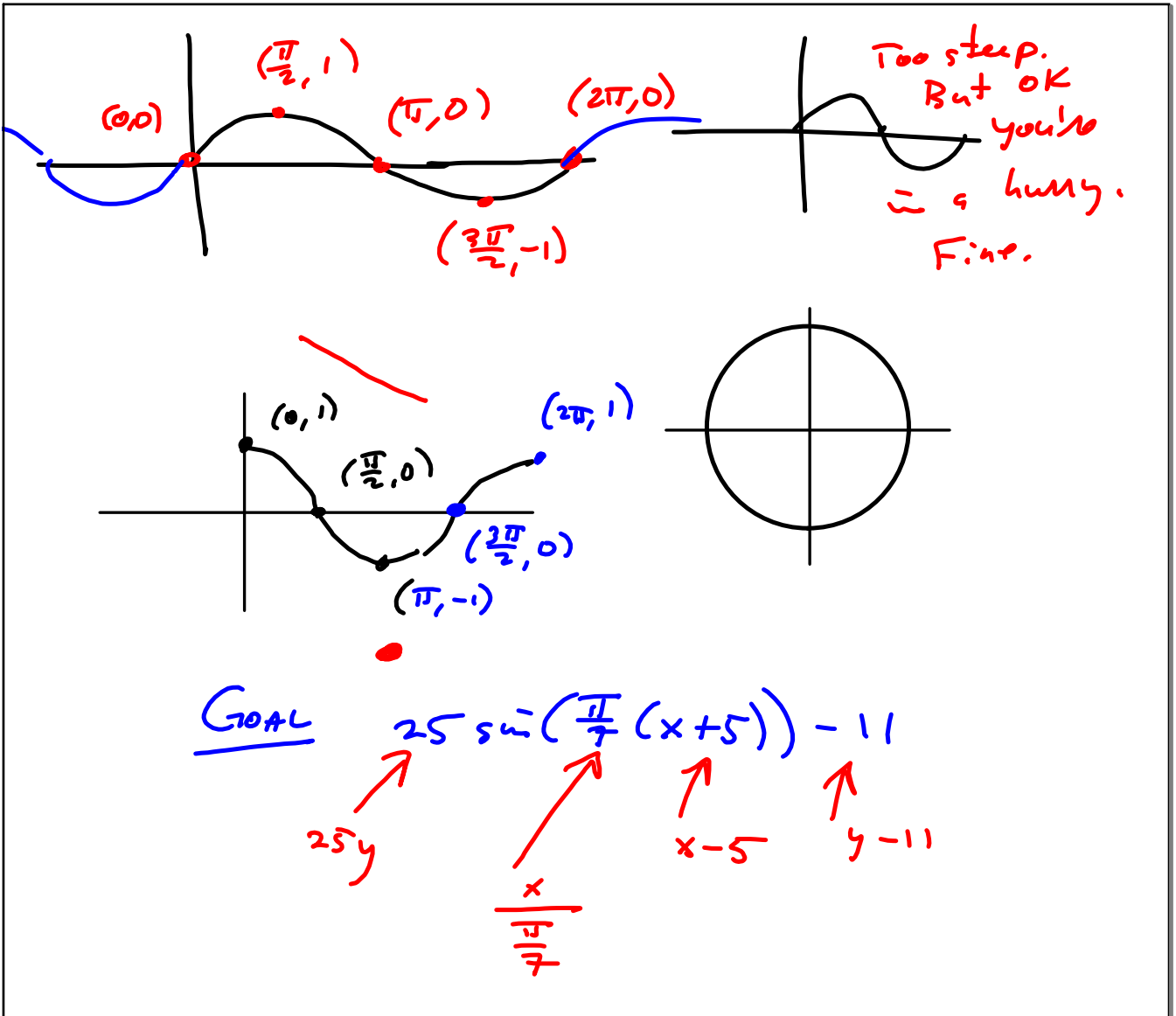


Pythag....

$$3^2 - 2^2 = 9 - 4 = 5 = b^2$$

$\sin \theta = \frac{3}{2}$  Never!





S 1.2 #54 Prove the identity

$$\sin^2 \theta =$$

$$\sin^2 \theta - \cos^2 \theta = 2\sin^2 \theta - 1$$

proof

$$\sin^2 \theta - \cos^2 \theta = \sin^2 \theta - (1 - \sin^2 \theta)$$

$$= \sin^2 \theta - 1 + \sin^2 \theta = 2\sin^2 \theta - 1 \quad \square$$

Pythagorean Identity

$$\cos^2 \theta + \sin^2 \theta = 1$$

55

$$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = \sec \theta \csc \theta$$

proof  $\frac{\sin \theta}{\cos \theta} \cdot \frac{\sin \theta}{\sin \theta} + \frac{\cos \theta}{\sin \theta} \cdot \frac{\cos \theta}{\cos \theta}$

$$= \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta} = \frac{1}{\sin \theta \cos \theta} = \frac{1}{\sin \theta} \cdot \frac{1}{\cos \theta}$$

$$= \csc \theta \sec \theta \quad \square$$