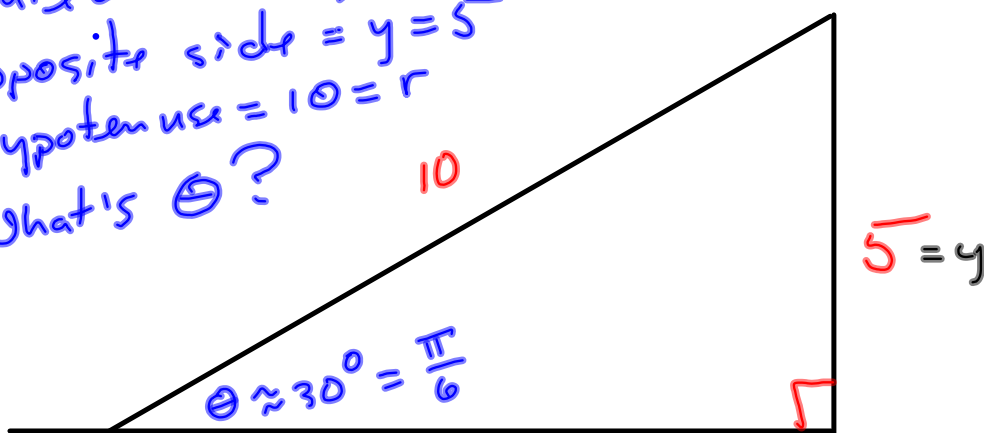


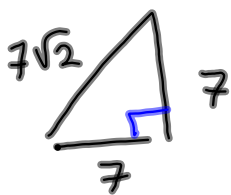
Build a triangle with  
 opposite side =  $y = 5$   
 hypotenuse =  $10 = r$   
 what's  $\theta$ ?



we'll explore some others, like

$$x = 7, y = 7 \Rightarrow r = ?, \theta = ?$$

Pythagorus says  $r = \sqrt{7^2 + 7^2} = \sqrt{2(7^2)}$



is what to remember.

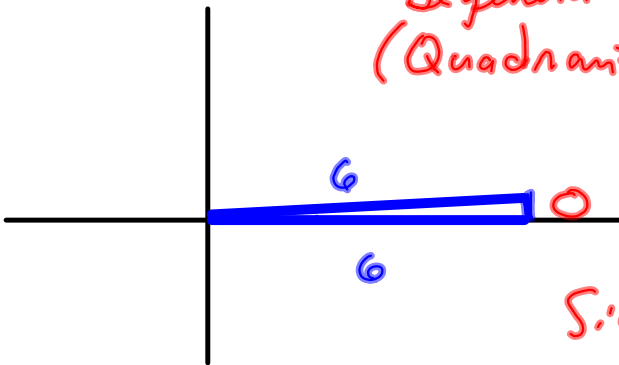
1, 2 #s 2-5 all, 7-49 odds.

Triangle with  $x = 6, r = 6$

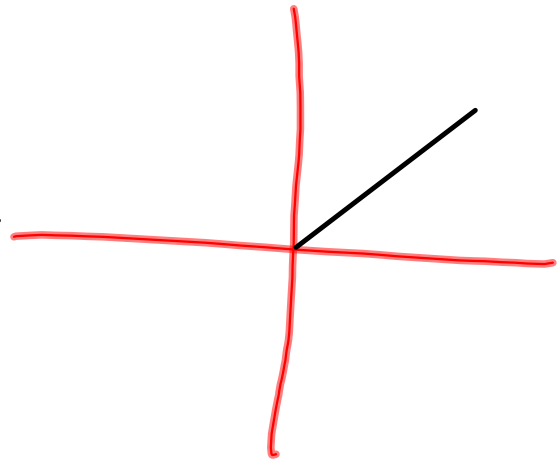
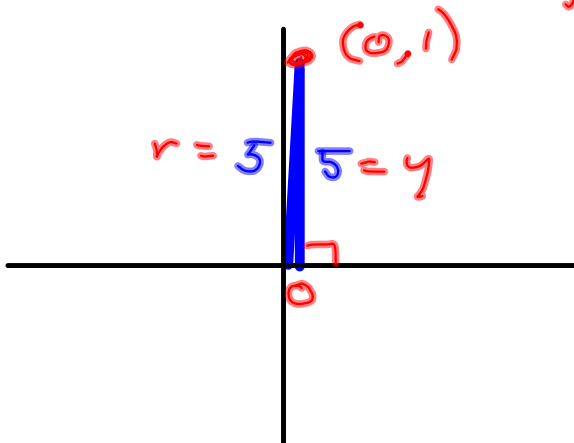
what's  $y$ ?  $y = 0$

what's  $\theta$ ?  $\theta = 0$

Degenerate triangle  
(Quadrantal)



Similarly  
 $y = 5, r = 5$



Name

122-G11

1.1

$$\theta = \frac{163\pi}{6}$$

2 angles coterminal  
one  $\alpha$  pos, one  $\beta$  neg,  
Both Between  $-2\pi$  &  $+2\pi$

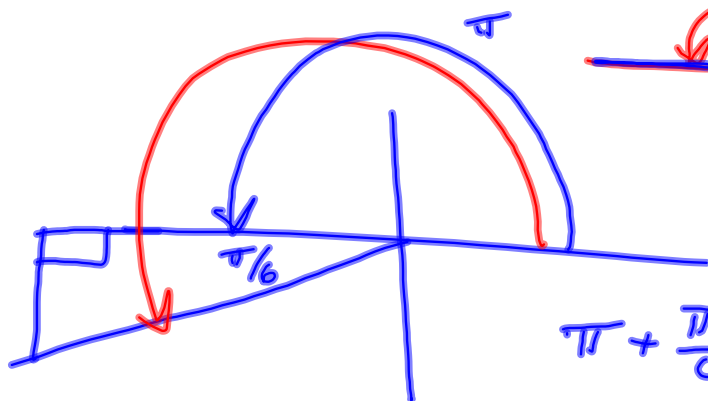
$$\frac{163}{6} = 27 + \frac{1}{6}$$

$$\begin{array}{r} 27 \times 6 \\ \hline 6 \overline{) 163.00} \end{array}$$

$$\Rightarrow \frac{163}{6}\pi = \left(27 + \frac{1}{6}\right)\pi$$

$$= 27\pi + \frac{\pi}{6}$$

odd multiple of  $\pi$  +  $\frac{\pi}{6}$



Reference triangle

$30^\circ - 60^\circ$

$$\pi + \frac{\pi}{6} = \frac{2\pi}{6} = \alpha$$

Now, for  $\beta$ :

$$\frac{7\pi}{6} - 2\pi = \frac{7-12}{6}\pi$$

$$= \left[-\frac{5\pi}{6} = \beta\right]$$

Same question for  $4635^\circ$ . Make  
 $-360^\circ < \alpha, \beta < 360^\circ$ ,  $\alpha > 0$ ,  $\beta < 0$

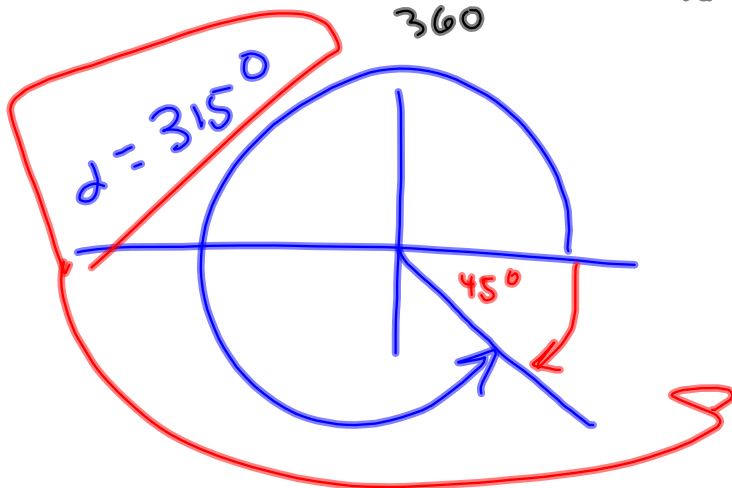
$$\frac{4635}{360} = 12. \text{ stuff}$$

$$(12)(360) = 4320$$

$$\begin{array}{r} 4635 \\ -4320 \\ \hline 315 \end{array}$$

This says  $4635 = (12)(360) + 315$

$$\frac{4635}{360} = 12 \frac{315}{360}$$



This is  
 $4635^\circ$  when  
we "mod out"  
by  $360^\circ$ .

$$\begin{array}{l} \beta = 315 - 360 \\ = -45^\circ = \beta \end{array}$$