

Online graphing calculator:

<http://www.meta-calculator.com/online/>

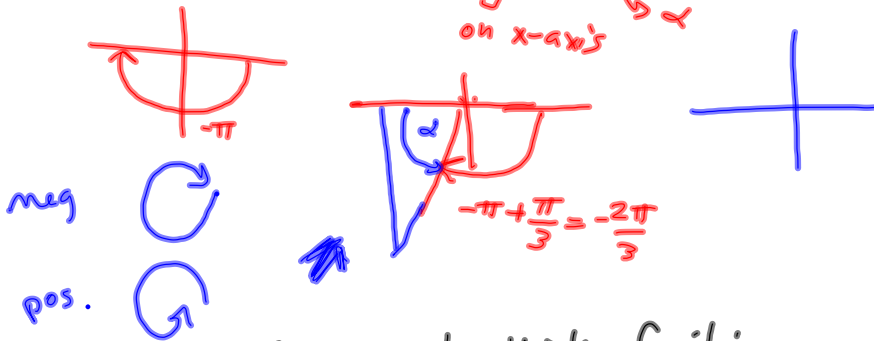
Errata on homework

#s 13b & 63

#13b Look for nearest multiple of π , because your reference angle is always measured from the x-axis $\rightarrow \alpha$

13b should be $\theta = -\frac{2\pi}{3}$

$$-\frac{2\pi}{3} = -\frac{3\pi}{3} + \frac{\pi}{3} = \underbrace{-\pi}_{\text{on x-axis}} + \frac{\pi}{3} \rightarrow \alpha$$



One way to think of it:
Go $+\frac{2\pi}{3}$ & flip it over the x-axis.



Flip it:

$$\frac{2\pi}{3} = \frac{3\pi}{3} - \frac{\pi}{3}$$



#63 - I miscopied 5000 as 500.

Final answer is 9490.227808 $\frac{\text{ft}}{\text{min}}$

Extra: Miles/hr: No reason to go to feet. EXCELLENT.

$$(9490) \left(\frac{\text{ft}}{\text{min}} \right) \left(\frac{1 \text{ mi}}{5280 \text{ ft}} \right) \left(\frac{60 \text{ min}}{1 \text{ hr}} \right)$$

$$\frac{9490 \cdot 60}{5280}$$

$$\frac{4745}{44}$$

evalf(%)

107.8409091

!?!? 108 $\frac{\text{miles}}{\text{hr}}$!?!?

Area of Sector of a circle.

I think of it always working proportional to a full circle.

$$\text{Area of a disc} = \pi r^2$$

Angle to go all the way around = 2π

Area of disc in terms of the angle :

$$\pi r^2 = \frac{1}{2} \cdot 2\pi r^2$$

$\frac{1}{2}$ -way around the circle :

$$\frac{\frac{1}{2} (2\pi r^2)}{2} = \frac{1}{2} (\pi r^2)$$

$\frac{1}{3}$ around

$$\frac{\pi r^2}{3}$$

$$\frac{\frac{1}{2} (2\pi r^2)}{3}$$

$$= \frac{1}{2} \left(\frac{2\pi}{3} r^2 \right)$$

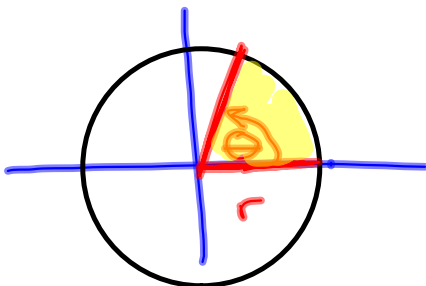
$\frac{1}{3}$ way around

⋮

In general, Area = $\frac{1}{2} \theta r^2$

$$= \frac{1}{2} r^2 \theta$$

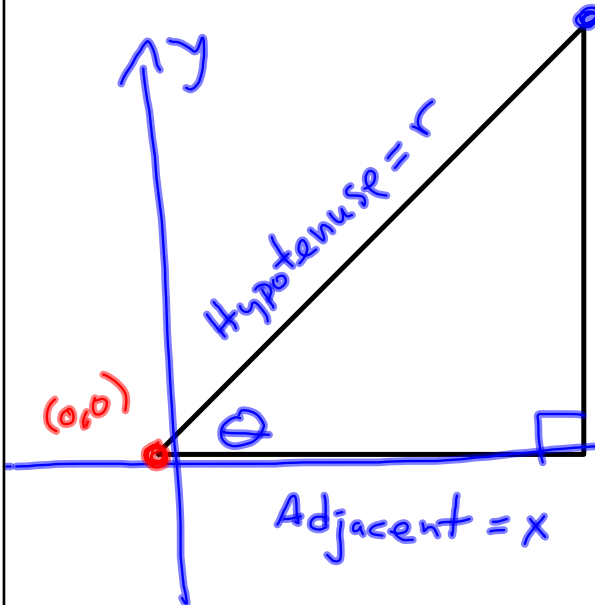
$$\text{Area} = \frac{1}{2} r^2 \theta$$



θ has to be in radians for this to work.

Today, we define trig functions.

$$(x, y) = (r \cos \theta, r \sin \theta)$$



OPPOSITE = y

If $r=1$, then

$$(x, y) = (\cos \theta, \sin \theta)$$

is $\int 1, 2$.

$\int 1, 2$ #5

2-5 all, 7-49 odds

$$\sin \theta = \frac{\text{OPPOSITE}}{\text{HYPOTENUSE}} = \frac{y}{r}$$

$$\cos \theta = \frac{\text{ADJACENT}}{\text{HYPOTENUSE}} = \frac{x}{r}$$

$$\tan \theta = \frac{\text{OPPOSITE}}{\text{ADJACENT}} = \frac{y}{x} = \text{Slope!}$$

$$\Rightarrow \begin{aligned} r \sin \theta &= y \\ y &= r \sin \theta \end{aligned}$$

$$\text{e, } x = r \cos \theta$$