

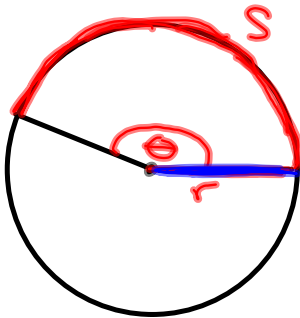
S 1.1 #s 1-6, 7-57 odds, 60, 63, 69.

All
write
out
questions

Due ~~Monday~~
Wednesday

Recall

$$\theta = \frac{s}{r} \text{ in radians}$$



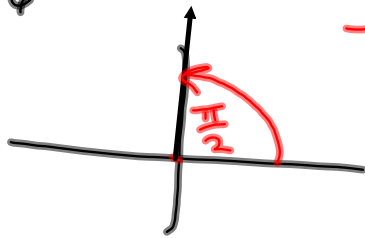
Radians relate angles
to corresponding arc
length, via the radius.

radian measure = ratio, $\frac{\text{arc length}}{\text{radius}}$

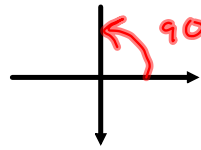
2π radians all the way 'round the circle:

$$\frac{2\pi r}{r} = 2\pi \text{ radians. See?}$$

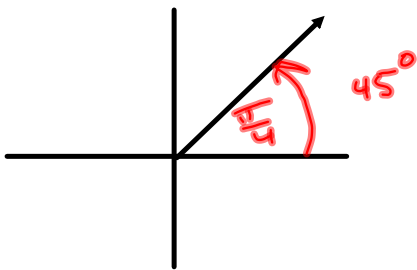
$$\frac{2\pi}{4} = \frac{1}{4} \text{ around} = \underline{\frac{\pi}{2} = 90^\circ}$$



COMMON
(over-used)
1st quad-
rant angles.



$$\frac{2\pi}{8} = \frac{1}{8} \text{ around} = \underline{\frac{\pi}{4} \text{ radians} = 45^\circ}$$



$$\frac{\pi}{2} = 90^\circ$$

$$\frac{\pi}{6} = \frac{\pi}{2} = 30^\circ$$

$$\frac{2\pi}{6} = \frac{1}{6} \text{ around} = \underline{\frac{\pi}{3} = 60^\circ}$$

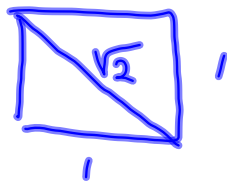
$$\frac{\pi}{3} = 2 \cdot \frac{\pi}{6} = 60^\circ$$

$$\frac{2\pi}{12} = \frac{1}{12} \text{ around} = \underline{\frac{\pi}{6} = 30^\circ}$$

2π radians $\approx 2 \cdot 3.14 = 6.28$ radians
to go around the circle.

A little more than 6 radians to go
full circle.

$$1 \text{ radian} \approx 57.2957951^\circ$$



$$180 + 90 = 270$$

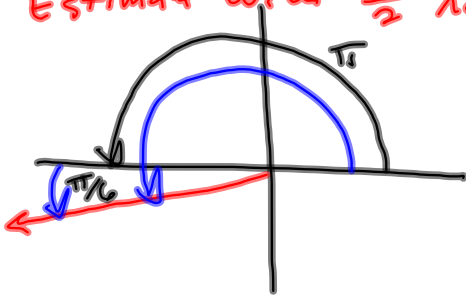
$$\begin{array}{l} \text{QII} \\ \frac{\pi}{2} < \theta < \pi \\ 90^\circ < \theta < 180^\circ \end{array}$$

$$\begin{array}{l} \text{QI} \\ 0 < \theta < \frac{\pi}{2} \\ 0 < \theta < 90^\circ \end{array}$$

$$\begin{array}{l} \text{QIII} \\ \pi < \theta < \frac{3\pi}{2} \\ 180^\circ < \theta < 270^\circ \end{array}$$

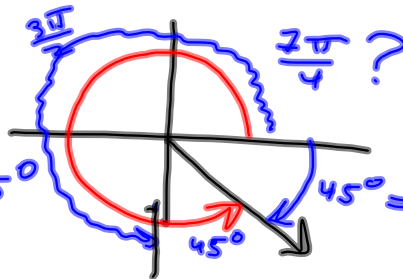
$$\begin{array}{l} \text{QIV} \\ \frac{3\pi}{2} < \theta < 2\pi \\ 270^\circ < \theta < 360^\circ \end{array}$$

Estimate w/in $\frac{\pi}{2}$ radians



use one of $\frac{\pi}{6}, \frac{\pi}{3}, \frac{\pi}{4}, \frac{\pi}{2}$ as your touchstones.

$$\pi + \frac{\pi}{6} = \frac{7\pi}{6}$$



$$360^\circ - 45^\circ = 315^\circ$$

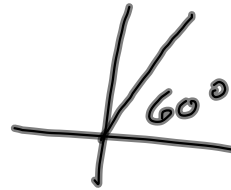
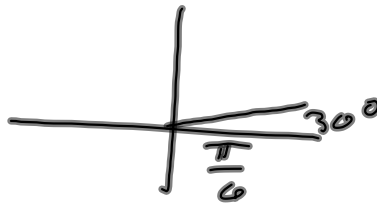
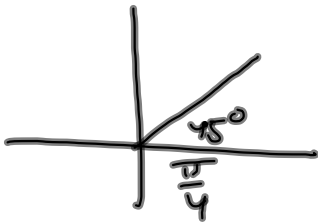
$$2\pi - \frac{\pi}{4} = \frac{7\pi}{4}$$

$$\frac{8\pi}{4} - \frac{\pi}{4} = \frac{7\pi}{4}$$


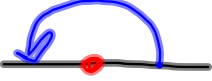

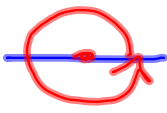
$\frac{\pi}{4} =$ Reference Angle

$$\frac{3\pi}{2} + \frac{\pi}{4} = \frac{7\pi}{4}$$

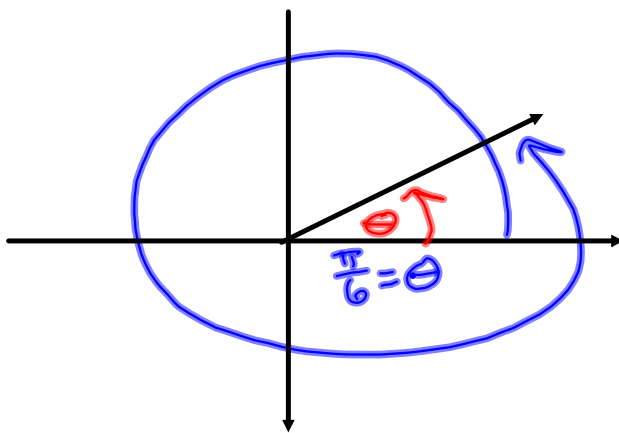
$$270^\circ + 45^\circ = 315^\circ$$



Special: Quadrantal Angles!

Degrees	90°	180°	270°	360°
Radians	$\frac{\pi}{2}$	π	$\frac{3\pi}{2}$	2π
				

Coterminal Angles. "Representation is not unique."



Same picture for an ∞ number of angles
 $\theta + 2\pi$ is coterminal with θ .

$$\frac{\pi}{6} + 2\pi = \frac{\pi}{6} + \frac{12\pi}{6} = \frac{13\pi}{6}$$

are also coterminal.
 $\frac{\pi}{6} - 2\pi = -\frac{11\pi}{6}$ is also coterminal with $\frac{\pi}{6}$.

See #s 29, 30

$$\frac{\pi}{6} + 17 \cdot 2\pi = \frac{\pi}{6} + 34\pi = \frac{204\pi}{6} + \frac{\pi}{6} = \frac{205\pi}{6}$$

is ALSO coterminal.

$\theta + 2n\pi$ is coterminal with θ , for any integer n .

