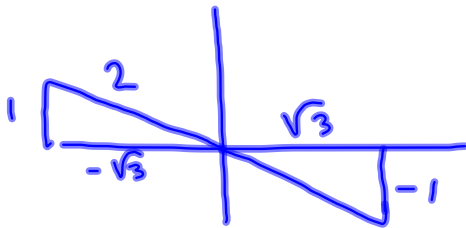


#2b $\operatorname{arccot}(-\sqrt{3})$ A bit of a zinger.
Pic for angle whose cotangent is $-\sqrt{3}$



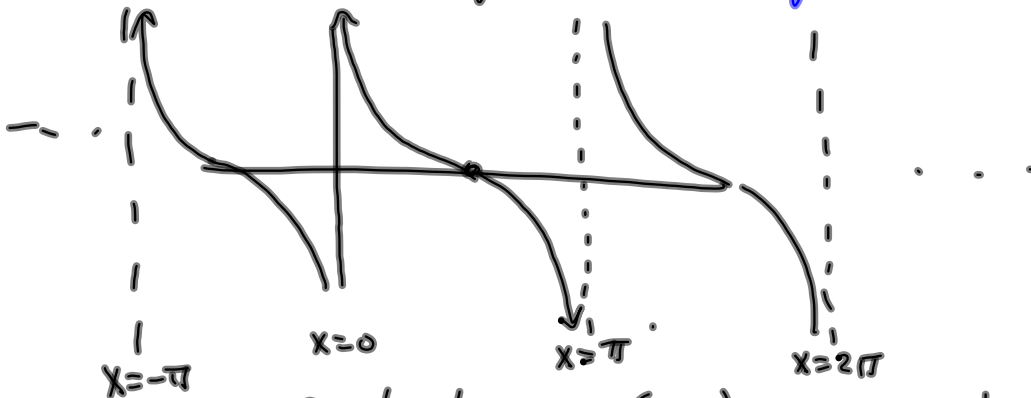
Your calculator does
 $\arctan(x)$
 $\tan^{-1}(x)$
But no $\operatorname{arccot}(x)$
no $\cot^{-1}(x)$.

So you could find
 $\arctan\left(-\frac{1}{\sqrt{3}}\right) = -\frac{\pi}{6}$

However, $\mathcal{R}(\arctan(x)) = \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

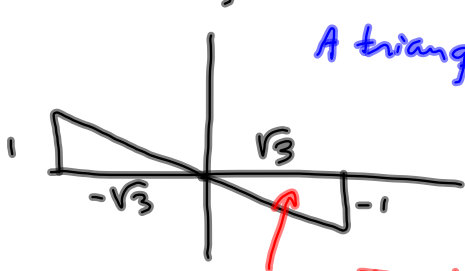
what's the $\mathcal{R}(\operatorname{arccot}(x))$?

Go back to its graph: (the graph of $\cot(x)$)



Restrict x to $(0, \pi)$ to keep it 1-to-1.

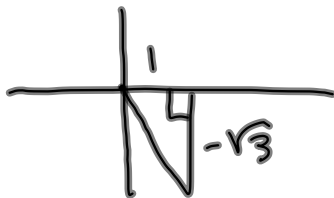
We might have a use for cofunction identities



A triangle w/ $\arctan(-\frac{1}{\sqrt{3}})$
has cotangent of $-\sqrt{3}$

No. $-\frac{\pi}{6} \notin \mathcal{R}(\operatorname{arccot}(x))$

Punch out $\tan^{-1}(-\sqrt{3}) = -\frac{\pi}{3}$

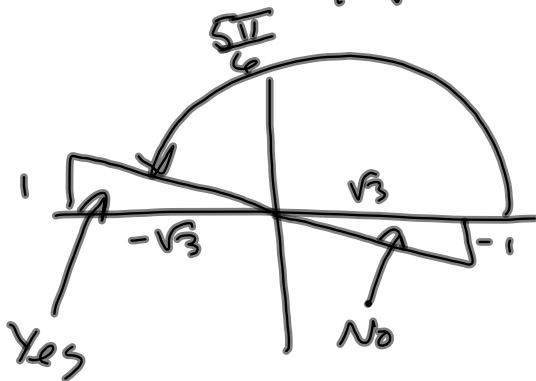


Cofunction:

$$\cot\left(\frac{\pi}{2} - \theta\right) = \tan \theta$$

What's $\frac{\pi}{2} - (-\frac{\pi}{3})$?

$$\frac{5\pi}{6} = \operatorname{arccot}(-\sqrt{3})$$



So one trick for $\operatorname{arccot}(-\sqrt{3})$ is $\frac{\pi}{2} - \arctan(-\sqrt{3})$!

Until we discuss $\mathcal{R}(\operatorname{arccot}(x))$
would've \neq would of $\mathcal{R}(\operatorname{arcsec}(x))$
 $\mathcal{R}(\operatorname{arccsc}(x))$

this $\operatorname{arccot}(x)$ thing is bonus. If I hurt you on #26, I shouldn't've.

- ① Hor stretch/shrink $\sin(ax)$ $x \rightarrow \frac{x}{a}$ *
- ② Ver stretch/shrink $a \sin(x)$ $y \rightarrow ay$
- ③ Hor. Shift $\sin(x-a)$ $x \rightarrow x+a$ *
- ④ Ver. Shift $\sin(x)+a$ $y \rightarrow y+a$

$$g(x) = 4 \sin(2x - \pi) + 7$$

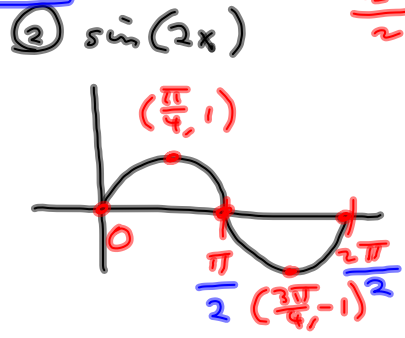
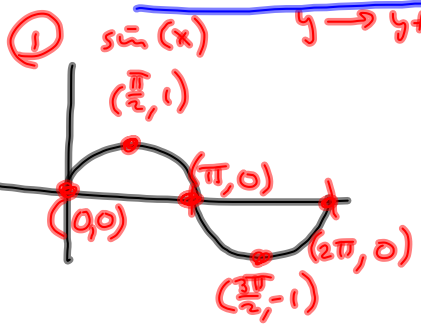
$$4 \sin(2(x - \frac{\pi}{2})) + 7$$

$$2x - \pi = 2(\frac{2x}{2} - \frac{\pi}{2}) = 2(x - \frac{\pi}{2})$$

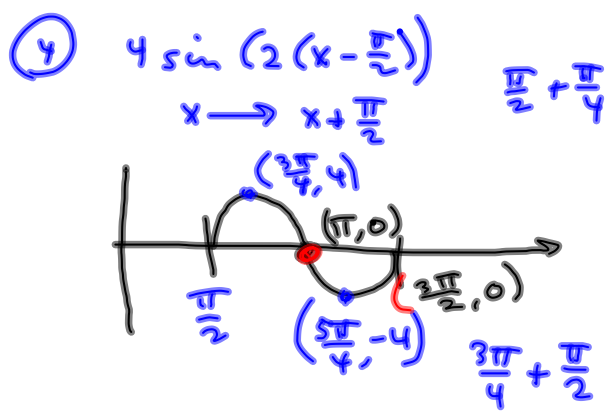
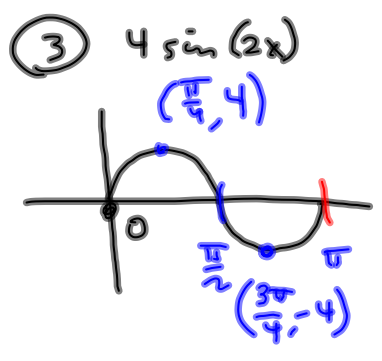
$$f(x) = \sin(x) \xrightarrow{\text{①}} \sin(2x) = f(2x) \xrightarrow{\text{②}} \sin(2(x - \frac{\pi}{2})) = f(2(x - \frac{\pi}{2}))$$

$$\text{③ } 4 \sin(2x) = 4 f(2x) \xrightarrow{\text{④}} 4 \sin(2(x - \frac{\pi}{2})) = 4 f(2(x - \frac{\pi}{2}))$$

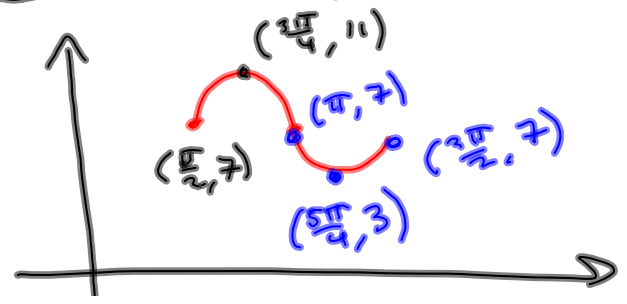
$$\text{⑤ } 4 \sin(2(x - \frac{\pi}{2})) + 7$$



$$\frac{\frac{\pi}{2}}{2} = \frac{\pi}{2} \cdot \frac{1}{2} = \frac{\pi}{4}$$



⑤ $4 \sin(2(x - \frac{\pi}{2})) + 7$



$$f(x) = x^3 - 5x^2 + 7x - 11$$

$$3f(7x-5) - 52$$

$$3f\left(7\left(x - \frac{5}{7}\right)\right) - 52$$

$$\textcircled{1} \quad x \rightarrow \frac{x}{7}$$

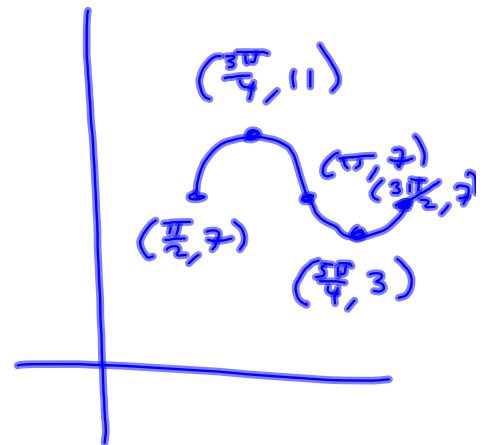
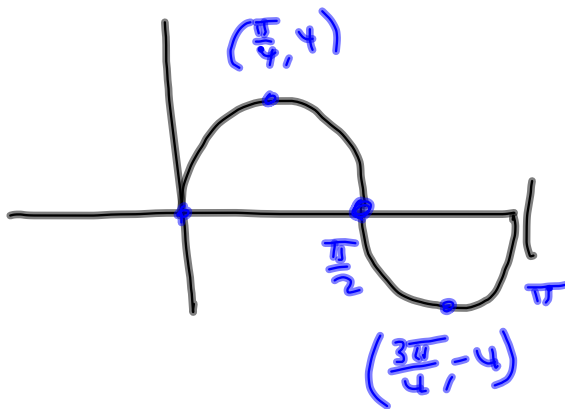
$$\textcircled{2} \quad y \rightarrow 3y$$

$$\textcircled{3} \quad x \rightarrow x + \frac{5}{7}$$

$$\textcircled{4} \quad y \rightarrow y - 52$$

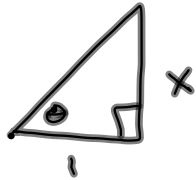
$$\begin{aligned} f(x) &\rightarrow f(7x) \\ &\rightarrow f\left(7\left(x - \frac{5}{7}\right)\right) \end{aligned}$$

$$\begin{aligned}
 g(x) &= 4 \sin(2x - \pi) + 7 \\
 &= 4 \sin\left(2\left(x - \frac{\pi}{2}\right)\right) + 7 \\
 &4 \sin(2x)
 \end{aligned}$$

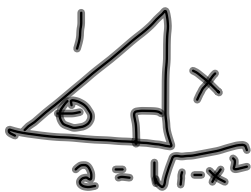


$$\begin{aligned}
 &4 \sin\left(2\left(x - \frac{\pi}{2}\right)\right) + 7 \\
 &\text{Right } \frac{\pi}{2}, \text{ up } 7
 \end{aligned}$$

$$\cot(\arctan(x)) = \frac{1}{x}$$



$$\tan(\arcsin(x)) = \frac{x}{\sqrt{1-x^2}}$$



$$a^2 + x^2 = 1$$

$$a^2 = 1 - x^2$$

$$a = \pm \sqrt{1-x^2}$$

take the pos.



$$\sin(\underbrace{\arccos(x)}_{\theta}) = \sqrt{1-x^2}$$