

**Vocabulary:** Fill in the blanks.

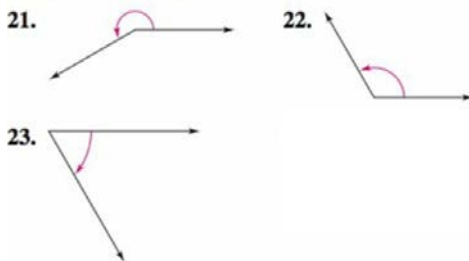
Write out the entire statement.

- Two angles that have the same initial and terminal sides are \_\_\_\_\_.
- One \_\_\_\_\_ is the measure of a central angle that intercepts an arc equal to the radius of the circle.
- Two positive angles that have a sum of  $\pi/2$  are \_\_\_\_\_ angles, whereas two positive angles that have a sum of  $\pi$  are \_\_\_\_\_ angles.
- The angle measure that is equivalent to a rotation of  $\frac{1}{360}$  of a complete revolution about an angle's vertex is one \_\_\_\_\_.
- The \_\_\_\_\_ speed of a particle is the ratio of the arc length to the time traveled, and the \_\_\_\_\_ speed of a particle is the ratio of the central angle to the time traveled.
- The area  $A$  of a sector of a circle with radius  $r$  and central angle  $\theta$ , where  $\theta$  is measured in radians, is given by the formula \_\_\_\_\_.

**Estimating an Angle** In Exercises 7–10, estimate angle to the nearest one-half radian.



**Estimating an Angle** In Exercises 21–24, estimate the number of degrees in the angle.



**Converting from Degrees to Radians** In Exercises 35 and 36, rewrite each angle in radian measure as a multiple of  $\pi$ . (Do not use a calculator.)

35. (a)  $120^\circ$  (b)  $-20^\circ$   
 36. (a)  $-60^\circ$  (b)  $144^\circ$

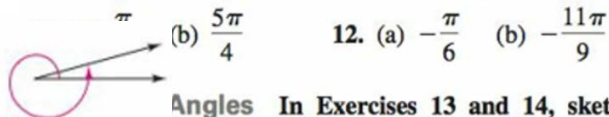
**Converting from Degrees to Radians** In Exercises 39–42, convert the angle measure from degrees to radians. Round to three decimal places.

41.  $0.54^\circ$  42.  $345^\circ$

**Converting from Radians to Degrees** In Exercises 43–46, convert the angle measure from radians to degrees. Round to three decimal places.

43.  $\frac{5\pi}{11}$  44.  $\frac{15\pi}{8}$  45.  $-4.2\pi$

**Determining Quadrants** In Exercises 11 and 12, determine the quadrant in which each angle lies.



**Angles** In Exercises 13 and 14, sketch each angle in standard position.

13. (a)  $\frac{\pi}{3}$  (b)  $-\frac{2\pi}{3}$  14. (a)  $\frac{5\pi}{2}$  (b) 4

**Finding Coterminal Angles** In Exercises 15 and 16, determine two coterminal angles (one positive and one negative) for each angle. Give your answers in radians.

16. (a)  $\frac{2\pi}{3}$  (b)  $-\frac{9\pi}{4}$

**Complementary and Supplementary Angles** In Exercises 17–20, find (if possible) the complement and the supplement of each angle.

17. (a)  $\frac{\pi}{3}$  (b)  $\frac{\pi}{4}$  18. (a)  $\frac{\pi}{12}$  (b)  $\frac{11\pi}{12}$   
 19. (a) 1 (b) 2 20. (a) 3 (b) 1.5

**Converting from Radians to Degrees** In Exercises 37 and 38, rewrite each angle in degree measure. (Do not use a calculator.)

37. (a)  $\frac{3\pi}{2}$  (b)  $\frac{7\pi}{6}$  38. (a)  $-\frac{7\pi}{12}$  (b)  $\frac{5\pi}{4}$

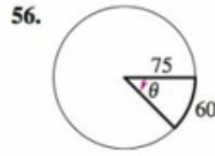
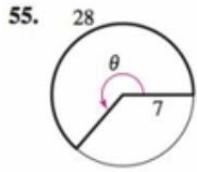
**Finding Arc Length** In Exercises 51 and 52, find the length of the arc on a circle of radius  $r$  intercepted by a central angle  $\theta$ .

51.  $r = 15$  inches,  $\theta = 120^\circ$  52.  $r = 3$  meters,  $\theta = 150^\circ$

**Finding the Central Angle** In Exercises 53 and 54, find the radian measure of the central angle of a circle of radius  $r$  that intercepts an arc of length  $s$ .

53.  $r = 80$  kilometers,  $s = 150$  kilometers  
 54.  $r = 14$  feet,  $s = 8$  feet

**Finding an Angle** In Exercises 55 and 56, use the given arc length and radius to find the angle  $\theta$  (in radians).

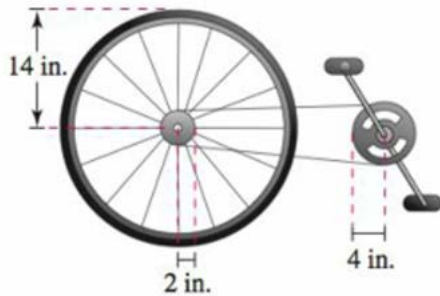


**66. Angular Speed** A car is moving at a rate of 65 miles per hour, and the diameter of its wheels is 2 feet.

- (a) Find the number of revolutions per minute the wheels are rotating.
- (b) Find the angular speed of the wheels in radians per minute.

**68. Speed of a Bicycle** . . . . .

The radii of the pedal sprocket, the wheel sprocket, and the wheel of the bicycle in the figure are 4 inches, 2 inches, and 14 inches, respectively. A cyclist is pedaling at a rate of 1 revolution per second.



- (a) Find the speed of the bicycle in feet per second and miles per hour.
- (b) Use your result from part (a) to write a function for the distance  $d$  (in miles) a cyclist travels in terms of the number  $n$  of revolutions of the pedal sprocket.
- (c) Write a function for the distance  $d$  (in miles) a cyclist travels in terms of the time  $t$  (in seconds). Compare this function with the function from part (b).