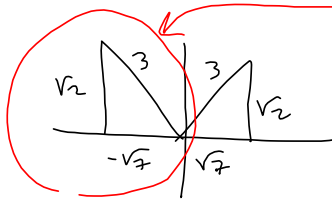


Find $\sin(2u)$, $\cos(2u)$ & $\tan(2u)$, given

$$\sin(u) = \frac{\sqrt{2}}{3} \text{ and } \cos(u) < 0$$

Like #9



$$9 - 2 = 7$$

$$\sin(2u) = 2\sin u \cos u = 2\left(\frac{\sqrt{2}}{3}\right)\left(-\frac{\sqrt{7}}{3}\right) = \boxed{-\frac{2\sqrt{14}}{9} = \sin(2u)}$$

$$\cos(2u) = \cos^2 u - \sin^2 u = \left(-\frac{\sqrt{7}}{3}\right)^2 - \left(\frac{\sqrt{2}}{3}\right)^2 = \frac{7}{9} - \frac{2}{9} = \boxed{\frac{5}{9} = \cos(2u)}$$

$$\Rightarrow \tan(2u) = \frac{\sin(2u)}{\cos(2u)} = \frac{-\frac{2\sqrt{14}}{9}}{\frac{5}{9}} = \boxed{-\frac{2\sqrt{14}}{5} = \tan(2u)}$$

Like #7

$$\sin\left(-\frac{5\pi}{12}\right)$$

(a) $-\frac{5\pi}{12} = \frac{\pi}{12} - \frac{6\pi}{12} = \frac{2\pi}{12} - \frac{7\pi}{12} = \frac{3\pi}{12} - \frac{8\pi}{12}$

$$-\frac{2\pi}{3} + \frac{\pi}{4}$$

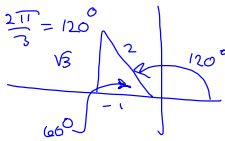
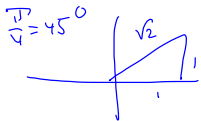
I don't memorize the \pm , here

$$\Rightarrow \sin\left(-\frac{5\pi}{12}\right) = \sin\left(\frac{\pi}{4} - \frac{2\pi}{3}\right) = \sin\left(\frac{\pi}{4}\right)\cos\left(-\frac{2\pi}{3}\right) + \sin\left(-\frac{2\pi}{3}\right)\cos\left(\frac{\pi}{4}\right)$$

cosine is even sine is odd

$$= \sin\left(\frac{\pi}{4}\right)\cos\left(\frac{2\pi}{3}\right) - \sin\left(\frac{2\pi}{3}\right)\cos\left(\frac{\pi}{4}\right)$$

sine is odd

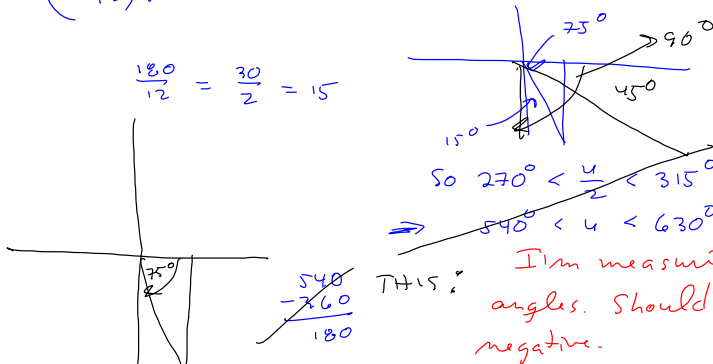


Instead, I use
 $\sin u \cos v + \sin v \cos u$
 to manage odd/even
 when $v < 0$.

$$\text{cut'd...} = \left(\frac{1}{\sqrt{2}}\right)\left(-\frac{1}{2}\right) - \left(\frac{\sqrt{3}}{2}\right)\left(\frac{1}{\sqrt{2}}\right) = \frac{-1 - \sqrt{3}}{2\sqrt{2}} = \sin\left(-\frac{5\pi}{12}\right)$$

(b) $-\frac{5\pi}{12} = \frac{1}{2}\left(-\frac{5\pi}{6}\right) = \frac{1}{2}u = \frac{u}{2}$

$$\left(-\frac{5\pi}{12}\right)\left(\frac{180^\circ}{\pi}\right) = -5(15^\circ) = -75^\circ$$



$$\frac{180}{12} = \frac{30}{2} = 15$$

So $270^\circ < \frac{u}{2} < 315^\circ$
 $\Rightarrow 540^\circ < u < 630^\circ$

I'm measuring positive angles. Should do the negative.

$-90^\circ < -75^\circ < -45^\circ$
 $-180^\circ < -150^\circ = u < -90^\circ \Rightarrow \text{QIII} \Rightarrow$

Don't need.
 Just find Quadrant $\sqrt{\frac{1 - \cos(-\frac{5\pi}{6})}{2}}$

$\frac{u}{2} = -\frac{5\pi}{12}$ $\frac{-5\pi}{12}$ lies in...
 $u = -\frac{5\pi}{6} \cdot \frac{180^\circ}{\pi} = -150^\circ$

$-75^\circ = \frac{u}{2}$
 $-90^\circ < \frac{u}{2} < -45^\circ$
 $-180^\circ < u < -90^\circ$



$u \in \text{QIII}$
 $\cos(u) < 0$ (left half).

So continuing:

$$= -\sqrt{\frac{1 - (-\frac{\sqrt{3}}{2})}{2}}$$

$\sin\left(-\frac{5\pi}{12}\right) = \sin(-75^\circ)$ is negative

$$= -\sqrt{\frac{2 + \sqrt{3}}{4}} = -\frac{\sqrt{2 + \sqrt{3}}}{2} = \sin\left(-\frac{5\pi}{12}\right)$$

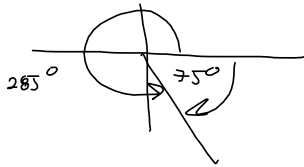
(7b) half-angle identity

$$\sin\left(\frac{u}{2}\right) = \pm \sqrt{\frac{1 - \cos(u)}{2}}$$

Decided by where $\frac{u}{2}$ lives.

$$\sin\left(\frac{19\pi}{12}\right) = \sin\left(\frac{1}{2}\left(\frac{19\pi}{6}\right)\right)$$

$$\frac{19\pi}{12} \cdot \frac{180^\circ}{\pi} = (19)(15)^\circ = 285^\circ$$



$$\text{So } \frac{u}{2} = \frac{19\pi}{12} \in \text{QIV}$$

$$\Rightarrow \sin\left(\frac{u}{2}\right) = -\sqrt{\quad}$$

B1 $d = 10 \text{ cm}$, $s = 500 \text{ m}$ $s = r\theta$
 How many revs?
 $d = 10 \text{ cm} \Rightarrow r = 5 \text{ cm}$
 $(500 \text{ m}) \left(\frac{100 \text{ cm}}{\text{m}} \right) = 50,000 \text{ cm} = s$
 $s = r\theta$
 $\Rightarrow 50,000 = 5\theta$
 $\Rightarrow \frac{50,000}{5} = \theta = 10,000 \text{ radians}$
 $= (10,000 \text{ radians}) \left(\frac{1 \text{ revolution}}{2\pi \text{ radians}} \right) = \frac{5000}{\pi} \text{ revs.}$

B2 starts $x=4$ (4, 110)

 Amp. is half its range?
 $\frac{112}{2} = 56 = 2$
 $116 = \frac{1}{2}T = \text{what goes under } \pi$
 Sec? $T = 116 \cdot 2 = 232$
 want $b\omega = 2\pi$ when $\omega = 232$.
 $232 b = 2\pi$
 $b = \frac{2\pi}{232} = \frac{\pi}{116}$ Sec?
 $\cos\left(\frac{\pi}{116}(x-4)\right)$
 $56 \cos\left(\frac{\pi}{116}(x-4)\right)$
 Now, Midline: Average of high & low
 $\frac{110 + (-2)}{2} = \frac{108}{2} = 54 = y = \text{midline}$
 $\Rightarrow f(x) = 56 \cos\left(\frac{\pi}{116}(x-4)\right) + 54$

B3 $A = \frac{1}{2}r^2\theta$
 $r = 60 \text{ cm}$
 $\theta = 330^\circ = (330^\circ) \left(\frac{\pi}{180^\circ} \right) = \frac{33\pi}{18} = \frac{11\pi}{6}$
 $\Rightarrow A = \frac{1}{2}(60)^2 \left(\frac{11\pi}{6} \right) = \frac{1}{2} \frac{(60)(60)(11\pi)}{6} = 300\pi \text{ cm}^2$

B4 $f(x) = 100 \sin\left(\frac{\pi}{13}x + \frac{11\pi}{13}\right) + 20$
 $\frac{\pi}{13}x + \frac{11\pi}{13} = \frac{\pi}{13}\left(x + \frac{11\pi}{\pi}\right) = \frac{\pi}{13}\left(x + \frac{11}{13} \cdot 13\right) = \frac{\pi}{13}(x+11)$

 Period is twice the 13? $26 = T$ cheat
 $\frac{\pi}{13}x = 2\pi$
 $x = \frac{26\pi}{\pi} = 26$, is how to reason it out. Want to know when $\frac{\pi}{13}x$ reaches 2π to obtain period.
 $11 + 26 = 37$
 $\frac{37 + 11}{2} = \frac{48}{2} = 24$ Amplitude is 100
 $20 + 100 = 120$
 $20 - 100 = -80$
 $\frac{11 + 24}{2} = \frac{35}{2}$
 $\frac{24 + 17}{2} = \frac{41}{2}$